A Causal Channel Model for the Terahertz Band

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Abstract—Impulse response is vital for wireless communication analysis and modeling. This paper considers the impulse response of the terahertz band (THz band: 0.1–10 THz) for short range (1–100 cm) wireless communication. Earlier works derived the impulse response from transmittance by assuming a linear phase, which corresponds to a line-of-sight (LoS) propagation delay to a receiver. However, the linear phase leads to a symmetric impulse response before and after the LoS propagation delay. Physically, it is impossible for a signal to arrive before the LoS propagation delay since this violates causality. To address this issue, this study derives a phase function leading to an impulse response that satisfies causality. The validity of the derived model is verified with experimental THz band measurements (up to 2 THz), which show excellent agreement with the results predicted by the theory. From the impulse response, coherence bandwidth is found for both the entire THz band and its subbands. The results show significant variations in the coherence bandwidth as a function of the center frequency. Knowledge of these variations supports selection of the proper center frequency for wireless communications in the THz band.

Index Terms—Causality, channel models, impulse response, molecular absorption, terahertz band.

I. INTRODUCTION

THE demand for ever high data rates in wireless communication systems is increasing exponentially, and it is predicted that they will reach 10 Gb/s for wireless local area networks [1], [2]. The terahertz band (THz band: 0.1–10.0 THz) is an encouraging candidate for ultra-high-speed communication [2], [3]. Traditional wireless communication systems operate at significantly lower frequencies, such as in the ultra high frequency band (UHF: 300 MHz–3 GHz), where extensive investigations on channel modeling have been made [4]. In contrast to the UHF band, the effect of molecular absorption needs to be considered in the THz band [5].

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Molecular absorption and its impact on transmittance of the channel were studied in [5]. Transmittance gives information about the fraction of the radiation capable of propagating through the channel and is modeled with the Beer–Lambert law. Thus, the Beer–Lambert law directly gives the molecular absorption loss in the channel [5]. Molecular absorption depends on the composition of a medium, relative humidity (RH), pressure, and temperature, and it causes frequency-selective fading for wideband signals.

To develop wireless communication techniques for the THz band, the impulse response is required. One reasonable approach to obtain impulse response is to use transmittance with only amplitude information and no phase information. In [3], [6], and [7], a linear phase was added to the transmittance and the impulse response was obtained by inverse Fourier transform (IFT). However, the impulse response based on a linear phase, or with no phase shift at all, does not satisfy causality. In [8], a method to obtain the received signal in the time domain was introduced. However, the impulse response as a time-domain channel model was not investigated, and the maximum frequency was around 2 THz. In addition, the distance considered in [8] was hundreds of meters. In contrast, we focus on the full terahertz band (0.1–10.0 THz) and consider communication distances suitable for short-range wireless communication (less than 1 m).

In [9], time domain channel model for line-of-sight path is derived from frequency response with spreading loss, and molecular absorption. Unlike previous studies [3], [6], [7] that use linear phase criterion, we obtain the phase component of the impulse response based on minimum phase, leading to a physically valid *causal impulse response*. A similar approach has been used in the field of spectroscopy [10]. More specifically, a minimum phase is obtained from the amplitude response of the channel by calculating the refractive index of the medium. The refractive index is obtained as a Hilbert transform from the absorption coefficient of the Beer–Lambert law. To the best of our knowledge, we are the first to utilize this method to obtain the impulse response with minimum phase for terahertz communication channels. We show the validity of the derived impulse response by comparing its results to experimental data.

In addition, we evaluate the coherence bandwidth with a given center frequency in a limited frequency band (LFB) scenario. In this scenario, bandpass filters (BPFs) are implemented at both the transmitting and the receiving ends. Frequencies with deep fading in the UHF band depend on a multipath environment and are typically random. In the THz band, the deep fades are caused by not only a multipath environment but also molecular absorption. Molecular absorption occurs in the resonance

TABLE I
KEY QUANTITIES USED IN THIS PAPER

Quantity	Symbol	Unit
Absorption coefficient	k_a	cm^{-1}
Distance of m th path	z_m	cm
Frequency	f	Hz
Pressure	p	hPa
Temperature	T	K
Speed of light	c	cm/s
Angle of incident wave of m th path	θ_m	deg
Rough surface height standard derivation	σ	cm

frequencies of molecules in the transmission medium and is an approximately deterministic phenomenon [11]. Therefore, the impact of molecular absorption on the coherence bandwidth is deterministic.

We further derive channel power loss, which represents power loss with a coherence bandwidth constraint determined by a target-flat frequency bandwidth. The channel power loss is useful for designing wireless communication techniques for the THz band.

The rest of this paper is organized as follows. Section II briefly describes the utilized propagation model for the THz band. In Section III, we derive the impulse response with the minimum phase. Section IV shows some numerical examples and studies the coherence bandwidth and the power loss of the THz channels. Section V concludes this paper.

II. CHANNEL MODEL

We assume a multipath channel model in which there is a LoS path and reflected paths between a transmitter and a receiver. Spreading loss and molecular absorption are considered as the dominant loss mechanisms in free space. Reflected paths are derived from Kirchhoff's theory [2], [3]. Antenna characteristics are not considered in the model. Key variables and constants used in this paper are summarized in Table I.

A. Channel Model in the Frequency Domain

The multipath channel consists of the LoS path and the reflected path. The frequency response of the multipath channel $H(f)$ is defined by

$$H(f) = \sum_{m=1}^M H_m(f, z_m) \quad (1)$$

where f , z_m , and $H_m(f, z_m)$ are the frequency, the distance of the m th path, and the frequency response of the m th path, respectively. The frequency response $H_1(f, z_1) = H_{1,\text{los}}(f, z_1)$ corresponds to the LoS path and $H_m(f, z_m) = H_{m,\text{refl}}(f, z_m)$ for $m \neq 1$ corresponds to the m th reflected path.

We can describe $H_m(f, z_m)$ as follows:

$$H_m(f, z_m) = |H_m(f, z_m)| \exp(j\phi_m(f, z_m)) \quad (2)$$

where ϕ_m is the phase component of the m th path. Conventional phase derivation and our proposed phase derivation will be shown in Section III.

1) *LoS path*: The propagation distance between the transmitter and the receiver is set to z_1 cm. The transmittance $|H_{1,\text{los}}(f, z_1)|^2$ is defined as

$$|H_{1,\text{los}}(f, z_1)|^2 = \frac{P_{\text{los}}(f, z_1)}{P(f, z_1 = 0)} \quad (3)$$

where f is the frequency, $P(f, z_1 = 0)$ represents the transmitted signal power, $P_{\text{los}}(f, z_1)$ is the received signal power, and $H_{1,\text{los}}(f, z_1)$ is the frequency response. As can be seen in (3), the transmittance contains the amplitude component of the frequency response, but not the phase component. By considering the spreading loss and the molecular absorption loss, the transmittance (3) can be calculated as [5]

$$|H_{1,\text{los}}(f, z_1)|^2 = [A_{\text{abs}}(f, z_1) \times A_{\text{spread}}(z_1)]^{-1} \quad (4)$$

where $A_{\text{spread}}(z_1)$ is the spreading loss and $A_{\text{abs}}(f, z_1)$ is the molecular absorption loss. The spreading loss in the LoS path for an ideal isotropic transmitter is $A_{\text{spread}}(z_1) = 4\pi z_1^2$. The molecular absorption loss $A_{\text{abs}}(f, z_1)$ can be described by the line absorption loss $A_{la}(f, z_1)$ and the continuum absorption loss $A_{ca}(f, z_1)$ as given in [11]:

$$A_{\text{abs}}(f, z_1) = A_{la}(f, z_1) \times A_{ca}(f, z_1) \quad (5)$$

with $A_{la}(f, z_1)$ and $A_{ca}(f, z_1)$ given by

$$A_{la}(f, z_1) = \exp\left(\sum_s k_{la}^s(f) z_1\right)$$

and

$$A_{ca}(f, z_1) = \exp\left(\sum_{s'} k_{ca}^{s'}(f) z_1\right) \quad (6)$$

where s and s' are indices for molecular species and the source of the continuum absorption, respectively, and k_{la} and k_{ca} are the line absorption coefficient and the continuum absorption coefficient, respectively. We utilize the *am* model [11], with the famous HITRAN catalog [12], to calculate the line absorption and continuum absorption coefficient.

2) *Reflected path*: The power spectrum $|H_{m,\text{refl}}(f, z_m)|^2$ of the reflected path is given by

$$|H_{m,\text{refl}}(f, z_m)|^2 = |H_{m,\text{los}}(f, z_m) \cdot R(f)|^2 \quad (7)$$

where $H_{m,\text{los}}(f, z_m)$ and $R(f)$ are the frequency response of the m th path for the LoS path and the reflection coefficient, respectively. According to Kirchhoff's theory, the reflection coefficient $R(f)$ for a rough surface is given by

$$R(f) = \gamma_{\text{TE}}(f) \cdot \rho(f) \quad (8)$$

where $\gamma_{\text{TE}}(f)$ is the smooth surface reflection coefficient from the Fresnel equation for the transverse electric (TE) part of the electromagnetic (EM) wave and $\rho(f)$ is the Rayleigh roughness factor. Without loss of generality, this paper considers the TE part of the EM wave; the transverse magnetic (TM) part can be

Fig. 1. Channel models for (a) the FFB and (b) the LFB scenarios.

obtained by a similar approach. The smooth surface reflection coefficient is described by

$$\gamma_{TE}(f) = \frac{n_i \cos \theta_m - n_t \sqrt{1 - \left(\frac{n_i}{n_t} \sin \theta_m\right)^2}}{n_i \cos \theta_m + n_t \sqrt{1 - \left(\frac{n_i}{n_t} \sin \theta_m\right)^2}} \quad (9)$$

where n_i , n_t , and θ_m are the refractive index of the air, the reflector, and incident angle of m th path, respectively [13]. The refractive index of the reflector n_t is frequency dependent. But so is n_i , actually. The rough surface effect is characterized by the Rayleigh roughness factor $\rho(f)$ as

$$\rho(f) = \exp\left(-\frac{8\pi \cdot f^2 \cdot \sigma^2 \cdot \cos^2 \theta_m}{c^2}\right). \quad (10)$$

We assume that the height of the rough surface has a Gaussian distribution with standard deviation σ . This assumption is valid for many indoor building materials [14].

B. Channel Model in the Time Domain

Two scenarios to obtain the impulse response are considered. In the first scenario, called the full frequency band (FFB) scenario, the impulse response is characterized by the full THz band. In the second scenario, called the LFB scenario, the BPF is employed to focus on a certain frequency band. The block diagrams of the FFB and LFB scenarios are shown in Fig. 1.

The received signal $y(t)$ at time t can be obtained by the convolution between the transmitted signal $x(t)$ and the impulse response, $h(\tau)$, as

$$\begin{aligned} y(t) &= \int_{-\infty}^{\infty} \sum_{m=1}^M h_m(\tau, z_m) x(t - \tau) d\tau \\ &= \int_{-\infty}^{\infty} h(\tau) x(t - \tau) d\tau \end{aligned} \quad (11)$$

where $h_m(\tau, z_m)$ is the impulse response of the m th path. The impulse response $h(\tau)$ is described as $h^{\text{FFB}}(\tau)$ in the FFB scenario and $h^{\text{LFB}}(\tau)$ in the LFB scenario.

Fig. 2. (a) Transmittance $|H_{1,los}(f, z_1)|^2$ as a function of frequency. (b) Impulse response $h_L^{\text{FFB}}(\tau)$ for $M = 1$ for the direct path from the conventional approach as a function of delay τ . Distance $z = 10$ cm, pressure $p = 1010$ hPa, RH = 69.6%, and temperature $T = 298.55$ K.

III. DERIVATION OF THE PHASE COMPONENT

Two criterion to obtain the phase component in the frequency response are shown in this section. The first criterion is linear phase and the second criterion is minimum phase. In the linear phase, the phase component is determined by the time shift and the frequency. On the other hand, in minimum phase, we employ Kramers–Kronig relation to determine the phase component.

A. Linear Phase

In the linear phase criterion, the phase component is set by $\phi_{L,m}(f, z_m) = -2\pi f z_m / c$. In this case, the frequency response $H_L(f)$ is given by

$$\begin{aligned} H_L(f) &= \sum_{m=1}^M H_{L,m}(f, z_m) \\ &= \sum_{m=1}^M |H_m(f, z_m)| \exp(j\phi_{L,m}(f, z_m)) \end{aligned} \quad (12)$$

where $|H_m(f, z_m)|$ is the square root of the power spectrum of the m th path found using (4) and (7). The impulse response $h_L^{\text{FFB}}(\tau)$ is obtained by

$$h_L^{\text{FFB}}(\tau) = \mathcal{F}^{-1}[H_L(f)] \quad (13)$$

where $\mathcal{F}^{-1}[\cdot]$ denotes the IFT operator.

If the channel has perfectly flat power spectrum with the linear phase, signal only experiences a time shift and it is perfectly causal after the time shift. In the general case, however, this is not always true. If the real and imaginary parts of the function are independent, such as in the case of real valued functions (zero phase), or linear phase imposed on real valued function, the resultant IFT is not causal (except for the special case of constant functions as discussed above). In this paper, we are concerned with THz frequencies (0.1–10 THz). In this case, the received signals will experience fading due to molecular absorption and the power spectrum is, therefore, never flat (unless we look at some narrow band within this range). Therefore, the impulse response based on the linear phase cannot fulfill the causality if the channel experiences the frequency selectivity due to the molecular absorption.

For instance, Fig. 2(a) shows the transmittance calculated with (4) as a function of frequency. Parameters used in this figure are distance $z_1 = 10$ cm, pressure $p = 1010$ hPa, RH = 69.6%, and temperature $T = 298.55$ K. We also show the corresponding impulse response based on the linear phase shift calculated with (12)–(13) in Fig. 2(b). We can see that the main problem with the linear phase is that it causes a symmetric response around the zero (which is the propagation delay in the case of linear phase, and $\tau = 0.33356$ ns in this example). This effectively causes a response at the receiver before the arrival of the main peak. Therefore, utilization of the causal phase component should be considered in the calculation of the impulse response to ensure that the response is correct at the receiver.

B. Minimum Phase

Impulse response with causality of the m th path satisfies

$$h_{C,m}^{\text{FFB}}(\tau) = \begin{cases} h_{C,m}^{\text{FFB}}(\tau, z_m), & \tau \geq \tau_m \\ 0, & \tau < \tau_m \end{cases} \quad (14)$$

where τ_m is the propagation delay of the m th path and given by $\tau_m = z_m/c$. The frequency response of $h_{C,m}^{\text{FFB}}(\tau, z_m)$ is given by

$$\begin{aligned} H_m(f, z_m) &= \int_{\tau_m}^{\infty} h_{C,m}^{\text{FFB}}(\tau, z_m) e^{-j2\pi f\tau} d\tau \\ &= e^{-j2\pi f\tau_m} \int_0^{\infty} h_{C,m}^{\text{FFB}}(\tau + \tau_m, z_m) e^{-j2\pi f\tau} d\tau. \end{aligned} \quad (15)$$

$H'_m(f, z_m)$ is defined as *causal frequency response* in this paper and is given by

$$H'_m(f, z_m) = \int_0^{\infty} h_{C,m}^{\text{FFB}}(\tau + \tau_m, z_m) e^{-j2\pi f\tau} d\tau \quad (16)$$

which leads to

$$H_m(f, z_m) = e^{-j2\pi f\tau_m} H'_m(f, z_m). \quad (17)$$

Let $\exp[-\alpha_m(f, z_m)]$ and $\phi_{C,m}(f, z_m)$ denote the amplitude and phase components of $H'_m(f, z_m)$, respectively, i.e., $\exp[-\alpha_m(f, z_m)] = |H'_m(f, z_m)| = |H_m(f, z_m)|$ and $\phi_{C,m}(f, z_m) = \arg(H'_m(f, z_m))$. Then, $H'_m(f, z_m)$ is given by [10], [11]

$$H'_m(f, z_m) = \exp[-\alpha_m(f, z_m) + j\phi_{C,m}(f, z_m)]. \quad (18)$$

$\alpha_m(f, z_m)$ and $\phi_{C,m}(f, z_m)$ are Hilbert transform pairs from the Kramers–Kronig relation [10], [11]. Therefore, the impulse response $h_{C,m}^{\text{FFB}}(\tau, z_m)$ satisfies causality. Hence, $\phi_{C,m}(f, z_m)$ is given by

$$\phi_{C,m}(f, z_m) = \frac{1}{\pi} \text{PV} \int_{-\infty}^{\infty} \frac{\alpha_m(f', z_m)}{f - f'} df' \quad (19)$$

where PV represents Cauchy principal value [15]. The criterion to set the phase component in (19) is defined as minimum phase in this paper. Given $|H_m(f, z_m)|$, $H_m(f, z_m)$ is available based on (17)–(19). Finally, the impulse response with the

minimum phase of the multipath is given by

$$h_C^{\text{FFB}}(\tau) = \mathcal{F}^{-1} \left[\sum_{m=1}^M H_m(f, z_m) \right]. \quad (20)$$

From the above relation, the impulse response with minimum phase is calculated as follows. First, $\alpha_m(f, z_m)$ is obtained from (4) or (7) and then substituted in (19). Finally, (20) is obtained from (17), calculated using (18).

In the LFB scenario, the impulse response with the minimum phase $h_C^{\text{LFB}}(\tau)$ can be obtained by

$$h_C^{\text{LFB}}(\tau, f_c) = \int_{-\infty}^{\infty} h_C^{\text{FFB}}(\tau') h_{rc}(\tau - \tau', f_c) d\tau' \quad (21)$$

where $h_{rc}(\tau, f_c)$ represents the effect of the BPFs. We employ root raised cosine filters $h_{\text{rrc}}(\tau, f_c)$ as the BPF at both transmitter and receiver. Let h^{LFB} indicate the impulse response involving h^{FFB} and the BPFs. The effect of the BPFs $h_{rc}(\tau, f_c)$ is given by [16]

$$\begin{aligned} h_{rc}(\tau, f_c) &= 2\pi^2 f_o \text{sinc}(2\pi f_o \tau) \frac{\cos(2\pi f_o \tau)}{\pi^2 - (4\pi f_o \tau)^2} \\ &\quad \times \cos(2\pi f_c \tau) \end{aligned} \quad (22)$$

where $f_o = (\pi B)/(2\pi + 4.853a)$, a is the roll-off coefficient of BPF, B is the transmission band, and f_c is the center frequency. In the LFB scenario, f_c and B determine the target frequency band. In practice, the filter response must be delayed and truncated to satisfy causality [17]–[19]. Therefore, we truncate the extreme ends of the above filter response and delay the response such that the first time-domain component is at time zero after the truncation.

IV. NUMERICAL AND EXPERIMENTAL RESULTS

In this section, we will show the validity of the impulse response with minimum phase, the coherence bandwidth, and the power loss for the LFB scenario.

The common parameters used in all the numerical evaluations are as follows: pressure $p = 1010$ hPa, RH = 69.6%, and temperature $T = 298.55$ K, unless otherwise indicated. The roll-off coefficient $a = 1$ for h_{rc} .

A. Comparison Between Measurement and Analysis

To validate the impulse response with minimum phase, a comparison of the received pulse based on measurements and the received pulse based on analysis is performed. The measurements were made at distance $z_1 = 62.5$ cm, temperature $T = 295.15$ K, and pressure $p = 1015.9$ hPa. Measurements were conducted by terahertz time domain spectroscopy (THz-TDS) technique using the TeraVil-EKSPLA T-spec spectrometer. The experimental measurement setup is shown in Fig. 3. The measurement setup consists of the pump source, the laser delay lines, the medium control, and the signal measurement block. The delay lines are for obtaining THz pulse shape in time domain. The medium control is for setting channel medium. In order to measure THz signal in a LoS there is no sample at the sample location. The emitter focus on the detector in THz optics

Fig. 3. Terahertz time domain spectroscopy setup.

Fig. 4. Received pulse comparison between the measurement result at RH = 52% and analytically obtained result based on the minimum phase in the time-domain.

in Fig. 3 with a beam width of approximately 2 cm at the sample location.

There were two measurements, one at RH = 52% and the other at RH = 6%. The received pulse at RH = 6% is used as the transmitted signal $x(t)$, since molecular absorption is small. The received pulse is obtained analytically by the transmitted signal and either by the impulse responses with minimum phase (h_C^{FFB}) or the impulse response with linear phase (h_L^{FFB}) [8].

Comparison between the received pulses at RH = 52% is shown in Figs. 4 and 5. The analytically obtained pulse from h_C^{FFB} agrees well with the received pulse from the measurement data and it satisfies causality, as shown in Fig. 4. The analytically obtained received pulse from h_L^{FFB} implies that causality is not satisfied as shown in Fig. 5. Although the difference between the analytically obtained received pulse from h_L^{FFB} and the measurement result is relatively large, it is not very significant. This is because the frequency response does not have much frequency selectivity. This can be seen in Fig. 6, where the power spectrum at RH = 6% and RH = 52% correspond to the transmitted power spectrum and received power spectrum, respectively.

For comparison in a frequency band with significant frequency selectivity, we must carry out the measurement in a higher frequency band, such as 1.5 THz, which is difficult due to limitations of the measurement equipment. Alternatively, we compare the analytically received pulses provided by h_C^{FFB} and

Fig. 5. Received pulse comparison between the measurement result at RH = 52% and analytically obtained result based on the linear phase in the time-domain.

Fig. 6. Comparison between transmitted power spectrum at RH = 6% and received power spectrum at RH = 52% with bandwidth 0.9 THz at 0.4 THz. Distance $z_1 = 62.5$ cm, temperature $T = 295.15$ K, and pressure $p = 1015.9$ hPa.

h_L^{FFB} in Fig. 7. Here, the power spectrum has the most power from 1 THz to 2 THz, and we can see frequency selectivity in Fig. 7(b). Fig. 7(a) shows the analytically obtained received pulses based on h_C^{FFB} and h_L^{FFB} . Due to frequency selectivity, the effect of the delay wave is significant in h_C^{FFB} . In addition, the difference between h_C^{FFB} and h_L^{FFB} is now significant, indicating the validity and importance of h_C^{FFB} for the practical THz pulse shape. In addition, the result indicates that only h_C^{FFB} satisfies causality.

We also evaluate the importance of the minimum phase in energy detection based wireless communication scenario. Specifically, the effect of leak power due to delayed component in the received signal is evaluated in the case of Fig. 7. Gaussian pulse for transmitted signal and On-Off keying modulation are assumed. The transmitted signal in case of one pulse transmission is plotted in Fig. 8. The received signals of the impulse response with linear phase and the impulse response with minimum phase are plotted in Figs. 9 and 10, respectively. At the receiver, the energy detector is employed and the time duration for detecting the pulse is set to $T = 1.025$ ps according to the

Fig. 7. Comparison between the linear phase result and minimum phase result with bandwidth 2.2 THz at 1.5 THz at RH = 52%. (a) Received pulse in time domain (b) Transmitted power spectrum, RH = 6% and received power spectrum, RH = 52%. Distance $z_1 = 62.5$ cm, temperature $T = 295.15$ K, and pressure $p = 1015.9$ hPa.

Fig. 8. Transmitted Gaussian pulse with bandwidth 2.2 THz at 1.5 THz.

Fig. 9. Received pulse obtained from linear phase at RH = 52% with bandwidth 2.2 THz at 1.5 THz. Distance $z_1 = 62.5$ cm, temperature $T = 295.15$ K, and pressure $p = 1015.9$ hPa.

transmitted signal in Fig. 8. Since the arrival time $\tau_m = 2083.3$ ps, the energy detection output E_{main} is given by

$$E_{\text{main}} = \int_{\tau_m}^{\tau_m + T} |y(t)|^2 dt. \quad (23)$$

We define E_{main} as main power which contributes for the energy detection. We also define the leak power as

$$E_{\text{leak}} = \int_{\tau_m + T}^{\tau_m + 2T} |y(t)|^2 dt. \quad (24)$$

Fig. 10. Received pulse obtained from minimum phase at RH = 52% with bandwidth 2.2 THz at 1.5 THz. Distance $z_1 = 62.5$ cm, temperature $T = 295.15$ K, and pressure $p = 1015.9$ hPa.

Fig. 11. Multipath scenario ($M = 2$) with LoS and reflected path.

This leak power corresponds to intersymbol interference power. In order to evaluate the significance of the impulse response, we use main power to leak power ratio (MLR) since MLR has to be used to design the symbol time duration (T), and countermeasures to the intersymbol interference, such as error correcting coding, equalization. In this case, MLR for linear phase and minimum phase are 23.78 dB and 9.61 dB, respectively. This result indicates that the significance of the minimum phase for the impulse response derivation.

B. Impulse Response for Multipath

We assume a two path model, where one is a LoS path (solid arrow) and the other one is a reflected path (dashed arrow) as shown in Fig. 11. In this scenario, the height of both transmitter antenna and receiver antenna, the distance of the LoS path, and the distance of the second path are r , z_1 , and z_2 , respectively. θ_m is the angle of the incident wave to the reflector. We assume that the reflector is made of plaster, which is usually used in walls and its refractive index n_t is 2.24. The reflector has the rough surface height standard deviation $\sigma = 0.0088$ cm. In our multipath simulation, the parameters are as follows: $n_i = 1$, $r = 1$ cm, and $z_1 = 1 - 100$ cm.

Figs. 12 and 13 show impulse responses for multipath environments for two distances: $z_1 = 10$ cm and $z_1 = 80$ cm, respectively. In these figures, relative time = 0 corresponds to the time when the first wave arrives and the 6.6 ps and 0.8 ps markers are the relative arrival times of the reflected wave, which is given by $\tau_2 - \tau_1$, in Figs. 12 and 13 (dashed lines). The difference between the LoS path distance z_1 and the reflected path distance z_2 decreases when z_1 increases. At the same time, spreading loss and molecular absorption loss increase as the LoS path distance z_1 increases. The reflected path also suffers

Fig. 12. Impulse response for multipath environment in $z_1 = 10$ cm.

Fig. 13. Impulse response for multipath environment in $z_1 = 80$ cm.

from spreading loss and molecular absorption. Therefore, the absolute energy of the reflected path is smaller for 80 cm. However, the relative impact may be smaller for the 10 cm case compared to the 80 cm case.

C. Coherence Bandwidth

In this section, we show coherence bandwidth for the FFB and LFB scenarios. The coherence bandwidth W^{Coh} of a causal channel is, in general, given by the inverse of the root mean square delay spread τ_{rms} [16], [20]

$$W^{\text{Coh}} = 1/\tau_{\text{rms}}. \quad (25)$$

The root mean square delay spread τ_{rms} is defined by [16], [20]

$$\tau_{\text{rms}} = \sqrt{\frac{\int (\tau - \bar{\tau})^2 |h(\tau)|^2 d\tau}{\int |h(\tau)|^2 d\tau}} \quad (26)$$

where $h(\tau)$ is the impulse response and $\bar{\tau}$ is mean delay time defined by [16], [20]

$$\bar{\tau} = \frac{\int \tau |h(\tau)|^2 d\tau}{\int |h(\tau)|^2 d\tau}.$$

In the UHF band, multipath channel is caused by obstacles between a transmitter and a receiver. Specifically, the transmitted signal is reflected by the obstacles in the propagation environment. Thus, the reflected signals reach the receiver through different paths. Each path has a different delay that causes a different phase shift. The difference in the phase shifts results either in constructive or destructive fading in the frequency response. Therefore, the coherence bandwidth, which represents an approximately flat frequency bandwidth, is determined by the delay time of each path. Since the delay time is random, the

Fig. 14. Coherence bandwidth for impulse response with the minimum phase for a distance z_1 ranging from 1 to 100 cm.

coherence bandwidth in the LFB scenario in the UHF band is also random [21].

The THz band multipath channel affected by not only reflected signals but also molecular absorption. Reflected signals with random delays result in random fading in the frequency domain. In addition, molecular absorption depends on the pressure, temperature, RH, and the distance between the transmitter and receiver. Fading due to molecular absorption is approximately deterministic because of the vast numbers of molecules in the air. THz band channels have both random and deterministic fading characteristics. Thus, the behavior of the coherence bandwidth is complex. Since the coherence bandwidth corresponds to average flat bandwidth, this information is useful when designing short-range THz band wireless communication systems.

1) *Coherence Bandwidth for FFB*: The coherence bandwidth $W_{\text{FFB,los}}^{\text{Coh}}(z_1)$ of the LoS path is plotted with a solid line with circles and the coherence bandwidth $W_{\text{FFB,multi}}^{\text{Coh}}(z_1)$ of the multipath is plotted as a solid line in Fig. 14. The dashed line represents the coherence bandwidth for the multipath without molecular absorption in Fig. 14. The multipath without molecular absorption implies $A_{\text{abs}}(f, z_m) = 1$ in (4). In the calculation of the coherence bandwidth, the components that are less than -30 dB from the peak value are not considered. A similar approach was adopted in [22].

The coherence bandwidth for the multipath without molecular absorption is wider than $W_{\text{FFB,los}}^{\text{Coh}}(z_1)$ and $W_{\text{FFB,multi}}^{\text{Coh}}(z_1)$. Furthermore, $W_{\text{FFB,los}}^{\text{Coh}}(z_1)$ and $W_{\text{FFB,multi}}^{\text{Coh}}(z_1)$ show a similar behavior. Thus, we find that the impact of molecular absorption is dominant on the coherence bandwidth in the FFB scenario. $W_{\text{FFB,los}}^{\text{Coh}}$ and $W_{\text{FFB,multi}}^{\text{Coh}}$ decrease as the distance z_1 increases. In the range of 1–20 cm, $W_{\text{FFB,los}}^{\text{Coh}}$ and $W_{\text{FFB,multi}}^{\text{Coh}}$ decrease rapidly, but above 40 cm the coherence bandwidths converge.

To give a reason for this behavior, we plotted transmittances for the LoS paths at distances $z_1 = 2$ cm, 10 cm, and 80 cm in Fig. 15. It can be observed that the molecular absorption loss increases significantly with distance according to the Beer–Lambert law, resulting in a narrower $W_{\text{FFB}}^{\text{Coh}}$ as z_1 increases. The dominant molecular absorption loss at the higher distances causes the above coherence bandwidths to converge. In addition, the flat bandwidth is observed to be dependent on frequency.

Fig. 15. Comparison of $1/A_{\text{abs}}$ for distance $z_1 = 2, 10$, and 80 cm for the frequency range $3\text{--}3.4$ THz.

Fig. 16. Comparison between coherence bandwidths for $B = 0.05$ THz at 10 cm.

2) *Coherence Bandwidth for LFB*: We evaluate the achievable coherence bandwidth $W_{\text{LFB,los}}^{\text{Coh}}$ in the LFB scenario for the LoS path and $W_{\text{LFB,multi}}^{\text{Coh}}$ for the multipath channel in Figs. 16–19. $W_{\text{LFB,los}}^{\text{Coh}}$ and $W_{\text{LFB,multi}}^{\text{Coh}}$ are obtained from $h_{\text{C},1}^{\text{LFB}}$ and $h_{\text{C}}^{\text{LFB}}$, respectively, for a given center frequency f_c and the required transmission band B .

In Figs. 16–19, $W_{\text{LFB,los}}^{\text{Coh}}$ and $W_{\text{LFB,multi}}^{\text{Coh}}$ as functions of the center frequency f_c are plotted with different BPFs, i.e., $B = 0.05$ and 0.3 THz, respectively. In this case, coherence bandwidths $W_{\text{ref}}^{\text{Coh}}(B)$ of the BPF (without channel, only with BPFs) are 0.0983 THz and 0.5895 THz, respectively. These are plotted in dashed lines in these figures. The distance z_1 is set to 10 cm in Figs. 16 and 17 and to 80 cm in Figs. 18 and 19. In these figures, the coherence bandwidths for FFB $W_{\text{FFB,los}}^{\text{Coh}}$ with 10 cm and 80 cm are also plotted.

First, we show the common features of the LoS path and multipath. We can see that $W_{\text{LFB,los}}^{\text{Coh}}$ and $W_{\text{LFB,multi}}^{\text{Coh}}$ change significantly when f_c changes. This is due to the frequency selective molecular absorption loss and multipath fading.

Fig. 17. Comparison between coherence bandwidths for $B = 0.3$ THz at 10 cm.

Fig. 18. Comparison between coherence bandwidths for $B = 0.05$ THz at 80 cm.

Increasing the bandwidth and distance leads to fewer frequencies that can be close to $W_{\text{ref}}^{\text{Coh}}(B)$. The upper bound of $W_{\text{LFB,los}}^{\text{Coh}}$ is approximately equal to $W_{\text{ref}}^{\text{Coh}}(B)$ since B limits the coherence bandwidth of $W_{\text{LFB}}^{\text{Coh}}$. $W_{\text{ref}}^{\text{Coh}}(B)$ is limited by the required transmission band and is therefore independent of $W_{\text{FFB,los}}^{\text{Coh}}$.

Second, we focus on the frequency band where multipath fading is dominant. Below 1 THz in Figs. 16 and 17, multipath is the most significant effect. In this frequency band, there is only a little effect from molecular absorption [see Fig. 2(a)]. Accordingly, the coherence bandwidth $W_{\text{LFB,multi}}^{\text{Coh}}$ is

Fig. 19. Comparison between coherence bandwidths for $B = 0.3$ THz at 80 cm.

Fig. 20. Power spectrum of reflected wave without spreading loss for $z_1 = 10$ cm.

approximately equal to $W_{\text{LFB, multi}}^{\text{Coh, no}}$. $W_{\text{LFB, multi}}^{\text{Coh, no}}$ is the coherence bandwidth without molecular absorption in multipath. As mentioned above, the multipath model without molecular absorption means $A_{\text{abs}} = 1$. Fig. 20 shows the power spectrum of the reflected wave at 10 cm. The peak power of the reflected wave lies below 1 THz, where also the multipath effect is the strongest.

Finally, we show the results for the frequency band where molecular absorption is dominant. Figs. 18 and 19 show that molecular absorption is dominant in frequencies above 1 THz. Fig. 21 shows the power spectrum of the reflected wave at 80 cm. From this figure, we can see that the reflected paths affect the entire THz band. However, a distance between notches of $W_{\text{LFB, multi}}^{\text{Coh, no}}$ is wider than $W_{\text{LFB, multi}}^{\text{Coh}}$ in Figs. 18 and 19; therefore, $W_{\text{LFB, multi}}^{\text{Coh}}$ is very similar to $W_{\text{LFB, multi}}^{\text{Coh}}$ at 80 cm.

D. Channel Power Loss

We investigate channel power loss in this section. Here, we assume the LFB scenario and an impulse-based transmitted signal.

Fig. 21. Power spectrum of reflected wave without spreading loss for $z_1 = 80$ cm.

Fig. 22. Channel power loss for $B = 0.05$ THz in the LoS path for a distance range 1–100 cm.

We define the channel power loss $\Phi(z_1, f_c, B)$ as

$$\Phi(z_1, f_c, B) = \begin{cases} P_{\text{loss}}(z_1, f_c, B), & \left(W_{\text{LFB}}^{\text{Coh}}(z_1, f_c, B) \geq W_{\text{target}}^{\text{Coh}}(B) \right. \\ & \left. \& P_{\text{loss}}(z_1, f_c, B) \leq P_{\text{loss}}^{\text{target}} \right) \\ 0, & \text{(otherwise)} \end{cases} \quad (27)$$

where $W_{\text{target}}^{\text{Coh}}(B)$ denotes a target coherence bandwidth and, without loss of generality, it is assumed to be $0.9W_{\text{ref}}^{\text{Coh}}(B)$. P_{loss} is the energy loss due to spreading, molecular absorption loss, and multipath fading. $P_{\text{loss}}^{\text{target}}$ is the target power loss and, it is assumed to be 60 dB. $\Phi(z_1, f_c, B)$ represents the power loss with a given distance z_1 and frequency band (f_c and B). In addition, $\Phi(z_1, f_c, B) = 0$ indicates that the coherence bandwidth does not satisfy $W_{\text{target}}^{\text{Coh}}(B)$ and/or that the power loss exceeds $P_{\text{loss}}^{\text{target}}$. On the other hand, $\Phi(z_1, f_c, B) > 0$ indicates that both $W_{\text{target}}^{\text{Coh}}(B)$ and $P_{\text{loss}}^{\text{target}}$ are satisfied.

Results for the channel power loss for the LoS path with $B = 0.05$ and 0.3 THz are shown in Figs. 22 and 23, respectively. Target coherence bandwidths for $B = 0.05$ and 0.3 THz are 0.0884 THz and 0.5306 THz, respectively. In Figs. 22 and 23, the colored area represents the power loss P_{loss} (in dB) as a function of distance and center frequency and the white areas in the figure represent $\Phi(z_1, f_c, B) = 0$.

We can see that P_{loss} mostly depends on the center frequency. The feasible frequency bands, achieving $\Phi(z_1, f_c, B) \neq 0$, significantly decrease as B increases, as shown in Figs. 22 and 23. In addition, the feasible frequency bands decrease gradually when the distance z_1 is increased. This behavior is caused by molecular absorption loss as shown in Section IV-C2.

Fig. 23. Channel power loss for $B = 0.3$ THz in the LoS path for a distance range 1–100 cm.

Fig. 24. Channel power loss for $B = 0.05$ THz in the multipath for a distance range 1–100 cm.

Fig. 25. Channel power loss for $B = 0.3$ THz in the multipath for a distance range 1–100 cm.

Results for the channel power loss in the multipath channel with $B = 0.05$ and 0.3 THz are shown in Figs. 24 and 25, respectively. Target coherence bandwidths are the same as in the case of LoS path. Colored area and white area in Figs. 24 and 25 have the same meaning as in Figs. 22 and 23, respectively. Feasible frequency bands in the multipath are decreased compared to those in the LoS path case owing to distortion and power loss by multipath fading.

To show the relationship between P_{loss} and communication performance, Fig. 26 shows the bit error rate (BER) for P_{loss} . Simulation parameters were as follows. The distance and signal-to-noise ratio (SNR) are 10 cm and 36 dB, respectively. The transmitted signals are Gaussian pulses whose center frequencies are 0.1–9.9 THz, and bandwidth is 0.05 THz. We assume On–Off keying as the modulation technique. To detect the symbol, an energy detector is utilized [23].

There are two reasons for the increase in the BER. One is the decrease in the received signal power due to molecular absorption and multipath fading. The other is intersymbol interference caused by frequency selectivity [21].

Fig. 26. BER versus channel power loss for $B = 0.05$ THz at 10 cm.

V. CONCLUSION

In this study, we introduced impulse response with minimum phase as a time-domain channel model in the THz band. We mainly focused on short-range wireless communications, and thus distances less than 100 cm were considered. We employed the Hilbert transform to obtain the phase component from transmittance containing only the amplitude component. Numerical evaluation showed that the obtained impulse response satisfies causality. In addition, experimental measurements showed the validity of the proposed method.

We also investigated coherence bandwidth of the THz band in both the LFB and FFB scenarios. Unlike in the UHF band, coherence bandwidth of the THz band is mostly deterministic as the numerical results showed a strong frequency dependence for the coherence bandwidth. We also showed channel power loss, which represents available power loss with a constraint in terms of target coherence bandwidth. The channel power loss is useful for selecting proper frequency bands for short-range wireless communication.

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