Multi-static spatial and angular studies of polar mesospheric summer echoes combining MAARSY and KAIRA

Jorge L. Chau1, Derek McKay2,3, Juha P. Vierinen2, Cesar La Hoz2, Thomas Ulich3, Markku Lehtinen3, and Ralph Latteck1

1Leibniz Institute of Atmospheric Physics at the University of Rostock, Kühlungsborn, Germany
2University of Tromsø, The Arctic University of Norway, Tromsø, Norway
3Sodankylä Geophysical Observatory, Sodankylä, Finland

Correspondence: Jorge L. Chau (chau@iap-kborn.de)

Received: 26 February 2018 – Discussion started: 28 March 2018
Revised: 24 May 2018 – Accepted: 28 May 2018 – Published: 6 July 2018

Abstract. Polar mesospheric summer echoes (PMSEs) have been long associated with noctilucent clouds (NLCs). For large ice particles sizes and relatively high ice densities, PMSEs at 3 m Bragg wavelengths are known to be good tracers of the atmospheric wind dynamics and to be highly correlated with NLC occurrence. Combining the Middle Atmosphere ALOMAR Radar System (MAARSY) and the Kilpisjärvi Atmospheric Imaging Receiver Array (KAIRA), i.e., monostatic and bistatic observations, we show for the first time direct evidence of limited-volume PMSE structures drifting more than 90 km almost unchanged. These structures are shown to have horizontal widths of 5–15 km and are separated by 20–60 km, consistent with structures due to atmospheric waves previously observed in NLCs from the ground and from space. Given the lower sensitivity of KAIRA, the observed features are attributed to echoes from regions with high Schmidt numbers that provide a large radar cross section. The bistatic geometry allows us to determine an upper value for the angular sensitivity of PMSEs at meter scales. We find no evidence for strong aspect sensitivity for PMSEs, which is consistent with recent observations using radar imaging approaches. Our results indicate that multi-static all-sky interferometric radar observations of PMSEs could be a powerful tool for studying mesospheric wind fields within large geographic areas.

1 Introduction

The strong radar echoes over polar latitudes during the summer were first reported by Ecklund and Balsley (1981). Since then these echoes, known as polar mesospheric summer echoes (PMSEs) (e.g., Hoppe et al., 1988), have been the subject of active research. Currently there is a general consensus that they are generated by atmospheric turbulence and require the presence of free electrons and charged ice particles (e.g., Kelley and Ulwick, 1988; Havnes et al., 1996; Lie-Svendsen et al., 2003a, b; Rapp and Lübken, 2004). The scattering theories have been improved in the last decade to include events that were not supported before. For example, Varney et al. (2011) improved the previous work of Rapp et al. (2008) to explain the PMSE observations with the Poker Flat Incoherent Scatter Radar (PFISR). Namely, they arrived to an expression that shows that PMSE radar cross section (RCS) depends on electron density when it is much smaller than ice density. In the reverse case, PMSE RCS is proportional mainly to ice density.

The connection between noctilucent clouds (NLCs) and PMSEs has been established by many authors, e.g., Hoppe et al. (1990), Nussbaumer et al. (1996), Stebel et al. (2000), and Kaifler et al. (2011). The common element in PMSEs and NLCs is the presence of ice particles in the summer polar mesosphere. A difference is that only the electrically charged population of the particles have a role in the radar scattering mechanism regardless of their size. However, only particles of size greater than about 40 nm contribute to the brightness of NLCs regardless of whether they are charged or not. Another important difference is that NLCs cover a
large part of the sky and they are visible even to the naked eye, which facilitates the study of their large-scale horizontal behavior with various types of all-sky cameras. In contrast, PMSEs can be studied only inside a very limited region determined by the radar antenna beamwidth, typically a few km wide in the transverse (horizontal) direction using the main beam. Thus, NLCs provide means to investigate the large-scale behavior of the polar mesosphere. Observations with a variety of optical instruments have shown that NLCs present a variety of horizontal scales, from meters to hundreds of kilometers, and are typically confined to layers of less than 1 km thickness (e.g., Fiedler et al., 2009; Baumgarten and Fritts, 2014). From the temporal and spatial evolution of these structures, atmospheric waves and instabilities can be studied (e.g., Fritts et al., 2014, and references therein).

Given the understanding of PMSE occurrence, recent efforts have been devoted to study their long-term behavior (e.g., Latteck and Bremer, 2017) and angular dependence (e.g., Czechowsky et al., 1988; Huaman and Balsley, 1998; Smirnova et al., 2012; Sommer et al., 2016) and using them as tracers for atmospheric dynamics (e.g., Balsley and Riddle, 1984; Fritts et al., 1990; Hoppe and Fritts, 1995; Stober et al., 2013). Following the relation with NLCs, simultaneous PMSE observations with spatially separated monostatic systems have been associated to drifting structures (e.g., Bremer et al., 1996; Belova et al., 2007; Rapp et al., 2008). However, these previous studies were not able to determine the size and separation of such drifting structures. Recently, Sommer and Chau (2016), using radar imaging, have reported PMSE horizontal structures with sizes around 1 km, which is not surprising given that even smaller structures have been observed in NLCs. Moreover, these findings support the hypothesis of Sommer et al. (2016) that the radar cross section of PMSEs does not vary significantly as a function of observing angle (aspect sensitivity). This implies that the scattering originates from localized isotropic structures instead of anisotropic horizontally stratified structures. If the high aspect sensitivity were the norm for PMSEs, our observations reported here would not have been possible.

In this paper we present the results obtained using the Middle Atmosphere ALOMAR Radar System (MAARSY) (16.04° E, 69.30° N) and the Kilpisjärvi Atmospheric Imaging Receiver Array (KAIRA) (20.76° E, 69.07° N) in northern Scandinavia. MAARSY is a powerful all-digital phase array radar that was specially built to study PMSEs and lower atmospheric dynamics (Latteck et al., 2012b). Kaira was designed to study different kinds of atmospheric and ionospheric phenomena (Vierinen et al., 2013; McKay-Bukowski et al., 2015). Kaira can be used as an all-sky imaging receiver for cosmic radio emissions to study D-region absorption (McKay et al., 2015) and as a phased array radar receiver (Virtanen et al., 2014) for nearby radar and radio transmitters, such as the EISCAT very high frequency (VHF) radar (European Incoherent Scatter Scientific Association), MAARSY, or several nearby specular meteor radars.

Our paper is organized as follows. We first cover some aspects of PMSE scattering theory with special emphasis on meter scales and Bragg wavelength dependence. Then we describe the experiment configuration and present important aspects of the bistatic geometry, e.g., the effective Bragg wavelength. The monostatic and bistatic experimental results are shown and combined in Sect. 4. We proceed to discuss the horizontal sizes and separations of the identified structures and the conservative angular dependence values derived. Finally we present our conclusions, emphasizing the possibility of using observations of this kind to both gain more insight on PMSE spatial–temporal features and potentially use PMSE scattering as a way of obtaining improved regional wind field measurements.

2 PMSE scattering theory at meter scales

The expected radar cross section of PMSE has been studied by many authors trying to explain observations at different radar frequencies under different natural as well as artificial (ionospheric modification using high-frequency radio waves) conditions (e.g., Hill et al., 1999; Rapp and Lübken, 2004; La Hoz et al., 2006; Rapp et al., 2008; Varney et al., 2011). The most recent work in the subject by Varney et al. (2011), following the work of Hill (1978) and Rapp et al. (2008), shows that RCS is a strong function of electron density only when electron density is much smaller than ice density. Otherwise it is mainly controlled by ice density. This improvement to previous theories was motivated by PMSE observations with the Poker Flat Incoherent Scatter Radar (PFISR) during night and during aurora.

To help in the presentation and interpretation of our results, here we briefly show expressions relevant for our Bragg wavelengths of interest, i.e., around 3 m. From Eq. (44) in Varney et al. (2011), the PMSE RCS as a function of Bragg wavenumber, i.e., $k_B = 2\pi/\lambda_B$, is

$$
\eta(k_B) \propto k_B^{-3} \exp\left(-\frac{q K_s k_B^2}{S_c}\right),
$$

where $S_c = v_a/D_e$ is the Schmidt number, $K_s = (v_a^3/\epsilon)^{1/4}$ is the Kolmogorov microscale, $v_a$ is the kinematic viscosity of air (m$^2$s$^{-1}$), $D_e$ is the diffusion coefficient of electrons (m$^2$s$^{-1}$), and $\epsilon$ is the energy dissipation rate of turbulence (Wkg$^{-1}$). For a turbulent velocity spectrum with a Gaussian shape and width (or turbulence intensity) $\sigma_v$ (m s$^{-1}$), $\epsilon = F \sigma_v^2$, where $F$ is a factor that varies typically between 8 and 10, depending on the actual atmospheric conditions (e.g., Hocking, 1985; La Hoz et al., 2006).

The expected dependence of PMSE RCS at meter scales is shown in Fig. 1a. The figure shows the expected PMSE RCS for two simulations as a function of $k_B$. The simulations have
In the second simulation, we fix \( \sigma \) ical PMSE altitudes (i.e., 85 km). We have assumed \( N \) of interest.

but has a clear dependence on \( \lambda \). Schmidt number RCS is independent of turbulence intensity, with a wavenumber dependence shown in Eq. (1). Note that for high experiments. The black solid and dashed curves represent Bragg  

\[ \text{RCS} \propto \lambda^2 \exp(-\lambda^2) \]

\( \lambda_B \) are shown in black (Varney et al., 2011, Eq. 44). In the case of \( \lambda_B \), five cases are shown (see text for details). The two vertical dashed lines represent the wavenumbers of interest, i.e., bistatic middle point (smaller) and MAARSY monostatic (larger).

been obtained with a model used by La Hoz et al. (2006), which is based on the seminal work of Hill (1978). Moreover, we have used Model 2 of Hill (1978) as suggested by Hill et al. (1999). In the first simulation, we keep \( S_c = 3 \) constant and vary the turbulence intensity (\( \sigma_v \)) (dashed lines). In the second simulation, we fix \( \sigma_v = 1.1 \) m s\(^{-1} \) and vary \( S_c \). The vertical dashed-dot-dashed lines represent the lowest and largest (MAARSY monostatic) wavenumbers we will explore in this study with bistatic and monostatic radar experiments. The black solid and dashed curves represent Bragg wavenumber dependence shown in Eq. (1). Note that for high Schmidt number RCS is independent of turbulence intensity, but has a clear dependence on \( \lambda_B^2 \) for the Bragg wavelengths of interest.

In all cases, the simulations have been conducted for typical PMSE altitudes (i.e., 85 km). We have assumed \( N_e = 3 \times 10^{-9}, h_H = 0.2, v_a = 0.567, D_{\text{ne}} = 0.567, \sigma_{\text{ne}} = 1000, \) and \( \chi = 2.6 \times 10^{12} \). Here \( N_e \) is electron density in e m\(^{-3} \), \( \sigma_{\text{ne}} \) scale length of an electron density byte-out in meters, and \( \chi \) the dissipation rate of electron density variance in m\(^{-6} \) s\(^{-1} \). \( h_H \) is the Havnes parameter given by \( Z_d N_d / N_e \) (Verheest, 2000), where \( Z_d \) is the charge dust density and \( N_d \) the dust number density.

Figure 1b shows relative RCSs as a function of turbulence intensity for different simulations at MAARSY’s wavenumber in a monostatic configuration, i.e., \( 2\pi / 2.8 \) m, namely for (a) a small \( S_c \) (900) (green), (b) a small \( S_c \) (3) (dashed black), (c) turbulence without ice at 70 km (orange), (d) a fixed \( \sigma_v = 1.1 \) for a wide range of \( S_c \) (blue), and (e) a fixed \( \sigma_v = 4.0 \) for large \( S_c \) (from 100 to 5000) (red triangles). We have intentionally removed the absolute RCS from Fig. 1b, since we want to emphasize the qualitative features of these results. The salient features at about 2.8 m Bragg wavelength that can be deduced from Fig. 1b are as follows:

1. The RCS varies significantly as a function of \( S_c \) when \( S_c \) is not too large (e.g., \( S_c < 100 \)). In our simulation with \( \sigma_v = 1.1 \) (blue) the variation is more than 6 orders of magnitude.
Figure 2. Sketch of PMSE observations with MAARSY as transmitter and KAIRA and MAARSY as receivers. MAARSY main lobe and side lobes are represented by the vertical and tilted yellow triangles, respectively. The region of PMSEs is depicted with clouds of different sizes and colors located in a narrow region. The white arrows represent the expected Bragg vectors of the MAARSY–KAIRA detections (see text for more details).

2. At low $S_c$, the RCS varies strongly with turbulence intensity (dashed black), in a manner similar to turbulence without ice. As a reference, we are showing the expected RCS with $S_c = 1$ but at 70 km instead of 85 km (orange). Note the increase of RCS with increasing $\sigma_v$.

3. Once the $S_c$ is high (e.g., $>100$), the RCS varies very little (red triangles).

4. At high $S_c$, the RCS decreases with turbulence intensity (green line). This is an unexpected result, since this behavior cannot be reproduced by expressions or results shown in previous works (e.g., Rapp et al., 2008; Varney et al., 2011). This result indicates that for a given Schmidt number there is a region, $k_B \gg k_T$, where the RCS does increase with increasing turbulence intensity, and $k_B \ll k_T$, where the RCS decreases with increasing turbulence intensity, where $k_T$ is the Bragg wavenumber of this transition. Note that our simulations have been obtained by numerically integrating Hill’s theoretical results without approximations.

3 Experiment description

As mentioned above, the results presented in this paper have been obtained using MAARSY and KAIRA in northern Scandinavia. The distance between the two systems is approximately 190 km. MAARSY was used for transmission and reception operating at 53.5 MHz, i.e., a radar wavelength of 5.61 m. KAIRA was used for reception only. Figure 2 shows an schematic view of the experiment. As reference, we show the directions of the Bragg vectors of the bistatic geometry, i.e., KAIRA receptions, with white arrows, which all point to the middle point between MAARSY and KAIRA. Note that the Bragg wavelengths will be different for different vectors, being the largest over the middle point (i.e., $\sim 4.15$ m) and the smallest for a monostatic configuration (i.e., 2.8 m). Below we describe the specific configuration for each system as well as the main geometrical parameters of the MAARSY–KAIRA configuration. In a conventional bistatic configuration without scanning (as is the case here) neglected antenna side lobes, only one Bragg vector contributes to the received bistatic signal. The KAIRA data gathered during this experiment show otherwise, as the received signals at KAIRA have contributions originating from the MAARSY’s antenna side lobes in a wide range of directions, each with different Bragg wavevectors represented by the white arrows in Fig. 2; see below.

3.1 MAARSY configuration

MAARSY consists of 433 crossed-polarized three-element Yagi antennas. On transmission, right-circular polarization is used, the beam can be steered from pulse-to-pulse every 1 ms, and different sections of the antenna can be used. On reception there are 16 complex channels available. One of these channels receives from all 433 antenna elements, while the other 15 can be selected to receive from different por-
tions of the antenna. General details of the system are given
by Latteck et al. (2012a). An example of MAARSY’s flex-
ibility on transmission and reception can be found in Sommer
and Chau (2016), where narrow and wide beams were used
on transmission, and 15 different groups of 7 antennas each
(called hexagons) were used on reception.

For this campaign MAARSY was run with a comple-
mimentary code using 2 µs baud width, 5 % duty cycle of the avail-
able power, and an interpulse period of 1 ms. Only one nomi-
nally vertically pointing direction was used on both trans-
mission and reception. Ideally the signal is expected to come
from the main beam; however, depending on the strength of the
atmospheric target, echoes could come also from side
lobes (see below). Complex voltages for the added signal
of all 433 elements were recorded. To allow synchronization
with KAIRA, a 1 pulse-per-second GPS pulse and a GPS-
disciplined rubidium clock were used. The data were ana-
alyzed offline to obtain spectra and spectral moments.

3.2 KAIRA configuration

KAIRA is a dual array of omnidirectional VHF radio anten-
as in northern Finland. It consists of two closely located
arrays working in the bands between 10 and 80 MHz and be-
tween 110 and 250 MHz, using LOFAR antenna and digital
signal-processing hardware. Here we have used the former,
which is called the lower band array (LBA). The LBA consis-
ts of 48 crossed inverted-V dipole antennas. Each of the
signal channels, i.e., 96 including the two linear polarizations,
is directly sampled. After sampling the signals are pro-
cessed and combined in a variety of possibilities that could
combine frequency bands, antenna elements, and antenna
pointing directions; each such configuration is referred to as
a “beamlet”. The specific characteristics of KAIRA and the
results, as stand-alone and as receiver for other transmitters,
can be found in McKay-Bukowski et al. (2015).

The part of the experiment that we used in this paper con-
sisted of 5 beamlets all of them using all 48 LBA anten-
as pointing over MAARSY, i.e., −80° azimuth, and 68.20°
zenith, with different center frequencies around 53.55 MHz,
and a frequency width of 195.312 kHz, allowing an effec-
tive sampling of ∼1 µs. Complex voltages for each beam-
let were recorded and later combined, decoded, arranged in
range, and spectrally analyzed.

The whole experiment during this campaign consisted of
61 beamlets: 14 beamlets using 7 single selected anten-
as and 2 subbands around 32.55 MHz, 35 beamlets using
the same 7 antennas as before but with 5 subbands around
53.5 MHz, 10 beamlets using two pointing directions over
MAARSY and 5 subbands around 53.5 MHz, and 2 beamlets
in riometer mode using two different pointing directions. The
experiment was conducted for almost 3 days around 12 Au-
gust 2016. The main purpose of the experiment was to apply
the MMARIA (Multi-static, Multi-frequency Agile Radar
Investigations of the Atmosphere) (e.g., Stober and Chau,
2015; Chau et al., 2017) in KAIRA, using MAARSY and
the Andenes specular meteor radar working at 32.55 MHz
as transmitters, respectively. Unfortunately, for the purpose
of this work, only 5.5 h of the subbands around MAARSY
were recorded, mainly due to the high data volume. There
were 14 TB of data recorded during these 3 days. The results
related to the MMARIA approach and the 32.55 MHz will be
left for a future effort.

3.3 Bistatic geometry and considerations

The scattering of interest will be given by the Bragg wave-
length components, i.e., λB, where |kBi| = 2π/λB and kBi =
ki − ks and ki and ks are the incident and scattered wavenum-
bers with magnitudes 2π/λ, where λ is the radar wavelength.
The Bragg wavelength and the radar wavelength are related by
λB = λ/(2cos(θB/2)), where θB is the scattering angle,
i.e., the angle between ki and ks.

In Fig. 3, we show contour plots of selected parameters of
the bistatic geometry at an altitude of 85 km, as a func-
tion of longitude and latitude. Specifically, we show (a) the
normalized antenna gain of MAARSY, (b) the normalized
antenna gain of KAIRA, (c) the total range, (d) the Bragg
wavelength, (e) horizontal distance with respect to middle
point, and (f) the local scattering angle, i.e., the angle with
respect to the local coordinate system taking into account the
goed form of the Earth. By total range we mean the distance
from transmitter to scattering center plus the distance from
scattering center to receiver. In monostatic systems the range
to the scattering center is half the total range. The MAARSY
and the middle point between MAARSY and KAIRA are in-
dicated by a square and a triangle, respectively. Note that,

![Contour plots of selected parameters of the bistatic geometry at an altitude of 85 km.](image-url)
Contrary to monostatic configurations, the contours are not symmetric with respect to the center point.

A simple version of the radar equation, assuming that the target fills the radar beam, satisfies the Born approximation, and is located in the far field, is given by

$$P_t = P_i \frac{G_t}{4\pi R_i^2} \sqrt{2} \sin^2 \delta,$$

where $\eta$ is the radar scattering cross section, $P_t$ is the received power, $P_i$ is the transmitted power, $G_t$ the transmitted antenna pattern, $A_r$ the receiver effective antenna area, $V$ is the scattering volume, $\delta$ is the polarization angle, and $R_i$ and $R_s$ are the incident and scattered ranges, respectively. Given that on transmission a right-circular polarization was used, and on reception the power of two orthogonal linear polarizations were employed, $\sin^2 \delta = 0.5 + 0.5 \cos^2 \theta_B$.

Taking into account the antenna patterns and replacing $A_r = G_t \lambda^2/(4\pi)$, the bistatic backscatter power at a given total range $R_0$ is given by

$$P_t(R_0) = \frac{\lambda^2}{16\pi^3} \int_{R_0-c\tau/2}^{R_0+c\tau/2} \frac{1}{8\pi} \eta(k_B, h)(1 + \cos^2 \theta_B) G_r(\theta_x, \theta_y) G_t(\theta_x, \theta_y) \frac{d\Omega}{R_i^2(R_s)^2} d\Omega dR_s,$$

where $G_r$ is the receiver antenna pattern, $R_0 = R_i + R_s$, $\theta_x, \theta_y$ are the direction cosines with respect to the receiver, $c$ the speed of light, and $\tau$ the pulse width. Note that we are assuming that $\eta$ has only a dependence on Bragg vector ($k_B$) and altitude ($h$), which is suitable for PMSEs. In addition, we assume that the transmitted pulse and the receiver bandwidth have perfect square shapes.

The main characteristics of the monostatic and bistatic observations over MAARSY are summarized in Table 1. Note that the expected difference in sensitivity between monostatic and bistatic, assuming isotropic scattering and volume filling and considering range differences, is $\approx 26.9$ dB.

### Table 1. Experimental parameters over MAARSY.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>MAARSY–MAARSY</th>
<th>MAARSY–KAIRA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Geometry</td>
<td>Monostatic</td>
<td>Bistatic</td>
</tr>
<tr>
<td>Transmitter elements</td>
<td>433</td>
<td>433</td>
</tr>
<tr>
<td>Receiving elements</td>
<td>433</td>
<td>48</td>
</tr>
<tr>
<td>Peak power</td>
<td>800 kW</td>
<td>800 kW</td>
</tr>
<tr>
<td>$\lambda_B$</td>
<td>2.8 m</td>
<td>3.3 m</td>
</tr>
<tr>
<td>PMSE mean range</td>
<td>85 km</td>
<td>294 km</td>
</tr>
<tr>
<td>Received power</td>
<td></td>
<td></td>
</tr>
<tr>
<td>relative to monostatic</td>
<td>0 dB</td>
<td>$-26.9$ dB</td>
</tr>
</tbody>
</table>

4 Experimental results

In this section we present the results of the monostatic and bistatic observations conducted with MAARSY and KAIRA on 12 August 2016. In addition, we show the parameters that result from combining both systems.

#### 4.1 MAARSY monostatic observations

Figure 4 shows the spectral parameters of 5.5 h of observations during this campaign: (a) signal-to-noise ratio (SNR), (b) mean Doppler shift (Hz), and (c) spectral width (Hz).
spheric echoes for a few weeks at the beginning of PMSE season.

Another important feature in Fig. 4a is the variability of SNR in both time and space. We will show later that such variability is mainly due to horizontal variability and not to in situ temporal variability.

4.2 KAIRA bistatic observations

The corresponding KAIRA results are shown in Fig. 5. The spectral parameters are similar to those shown for MAARSY in Fig. 4, but instead of altitude they are shown as a function of total range. This time they were obtained every 20 s, and without any coherent integration. The spectra have been estimated using 1000 FFT points and 10 incoherent integrations. In the case of KAIRA we have used two conservative criteria to select the data, i.e., an SNR threshold of $-10$ dB and a coherence threshold of 0.25. By coherence we mean the coherence between the signals in both linear polarizations without subtracting the noise in the denominator. As a reference, we are plotting the corresponding height on the right, assuming that all the echoes are observed over MAARSY. Clearly echoes below 290 km in range do not come from regions over MAARSY since they would have come from much lower heights.

To our surprise, we were able to observe echoes from ranges that do not correspond to PMSEs illuminated overhead MAARSY, i.e., at ranges closer than 290 km. The echoes, apparently originating from heights lower than the PMSE heights, are clearly connected to the strongest echoes, which are located at the true PMSE heights. The only plausible explanation is that these echoes are normal PMSEs at normal PMSE altitudes, which are illuminated by the side lobes of the MAARSY transmitter beam and originate from a larger geographic area. This time the intensity of the echoes is clearly observed to vary with time. Moreover, in the case of Doppler shift, it is mainly negative, varying with time and range. In the case of range, there is a systematic dependence, being smaller at closer ranges. As in the case of MAARSY, the spectral widths are relatively small over MAARSY (total range farther than 290 km) and vary significantly at closer ranges, particularly after 07:30 UT.

Around 05:40 UT we are plotting a black parabolic line over the observed KAIRA PMSEs (pointed by the black arrow). This line has been obtained assuming that a scattering center was originally located at 85 km in altitude at the middle point between KAIRA and MAARSY and drifted horizontally at a constant velocity. The velocity used is 68 m s$^{-1}$ (from KAIRA to MAARSY), which is obtained from the Doppler shift measurements (see below). The agreement between the observed PMSE range–time behavior and this simple model is excellent, implying that the PMSE structures are drifting with the background horizontal wind.

4.3 Combined KAIRA–MAARSY PMSE measurements

Now we combine both measurements in this section. The peak values in range after a three-point smoothing in time of the monostatic (MAARSY) and bistatic (KAIRA) data, obtained from the same volume (overhead MAARSY), are shown in Fig. 6a, in red and green, respectively. In the case of monostatic results, altitudes between 80 and 87 km have been considered, while in the bistatic case, total ranges between 287 and 297 km were considered. The horizontal velocity over MAARSY (in the direction KAIRA–MAARSY, being positive towards KAIRA) is shown in blue (right axis). The horizontal velocity component in the direction MAARSY–KAIRA has been obtained from KAIRA’s Doppler shift (Fig. 5b) and MAARSY’s vertical velocity (Fig. 4b).

We can see that in general there is a good correspondence between the two SNR time variations, particularly when MAARSY signals are strong. To observe this feature better, in Fig. 6b we plot MAARSY vs. KAIRA peak values in range used in Fig. 6a. In this plot we can identify an approximate difference in signal between the two of $-30$ dB, i.e., where KAIRA SNR is equal to zero, which we have marked with a vertical dashed line.

Given that the spectral widths shown in Fig. 6c show a weak dependence with respect to SNR for the majority of
Figure 6. Combined MAARSY and KAIRA measurements: (a) median SNR over MAARSY as observed with MAARSY and KAIRA, and over the middle point; (b) MAARSY vs. KAIRA SNR scatter plot; and (c) bivariate distribution of MAARSY SNR vs. spectral width. The dashed lines indicate MAARSY’s 30 dB SNR as a reference. In panel (a), the mean horizontal wind over MAARSY in the direction MAARSY–KAIRA is shown in blue.

5 Discussion

We start our discussion by arguing that KAIRA observations come from scattering regions with high Schmidt numbers. By looking at the PMSE simulations, a wide range of RCSs (more than 6 orders of magnitude) for a constant turbulence intensity can be obtained by varying $S_c$ (see Fig. 1b). In the 5 h presented, MAARSY’s observed PMSE SNR show

echoes, we present a 2-D histogram of MAARSY’s SNR and spectral widths with the counts in log scale. The great majority of echoes have a strong variability in SNR with small changes in spectral width. A smaller but detectable population is characterized by an SNR that increases with increasing spectral width. Taking into account the PMSE simulations shown in Fig. 1b, we superimpose lines over these two populations and label them as “ice dominated” (blue) and “turbulence dominated” (black), respectively. One can argue that the part of Fig. 6c where spectral width (proxy for turbulence intensity) increases with increasing RCS agrees with the part of Fig. 1b for small $S_c$ (black dashed line with $S_c = 3$). The other part of Fig. 1, that covers the majority population, where narrow spectral widths can produce any value of RCS, seems to agree with the horizontal line of Fig. 1b. From this simple plot, we assume in the remainder of the paper that most KAIRA detections come from scattering regions with high Schmidt numbers. We are again marking the SNR threshold of 30 dB identified before.

Note that the spectral widths have not been corrected by any effects, like beam or shear broadening. Therefore, these values represent upper values of atmospheric turbulence intensity.

Having defined an empirical SNR difference between KAIRA bistatic and MAARSY monostatic of $\sim 30$ dB, in Fig. 7 we show the parameters resulting from combining both observations: (a) vertical structure and (b) vertical velocity after using a MAARSY SNR threshold of 30 dB, (c) vertical structure over MAARSY as observed with KAIRA, and (d) inferred horizontal velocity from KAIRA and MAARSY Doppler shifts. The thresholded MAARSY SNR results show that the echoes come from a narrow region in altitude, appearing and disappearing in time. After 07:00 UT a second narrow region appears at lower altitudes, with larger RCS. The corresponding vertical velocity does not show a distinct altitude dependence. In the case of KAIRA, the observed structures are wide in range, as expected, due to the convolution of a narrow layer with a wide receiver beam.

In the case of the horizontal velocity, the estimates are consistent when a single drifting structure occurs, e.g., between 05:15 and 07:15 UT. When more structures occur simultaneously, the estimated horizontal velocity gets more complicated, e.g., at total ranges smaller than 280 km and times around 04:30 and 08:00 UT. Assuming that PMSE structures over MAARSY have horizontally drifted with the obtained horizontal velocities, we have indicated 100 km segments in Fig. 7a with white lines, namely for faster flows the segments are shorter in time, e.g., around 06:00 UT.
Figure 7. Derived PMSE parameters from combining MAARSY and KAIRA observations, using a SNR threshold of 30 dB in MAARSY observations: (a) vertical structure, (b) vertical velocity, (c) vertical structure as observed from KAIRA, and (d) horizontal velocity along MAARSY–KAIRA direction (positive towards KAIRA). Approximate distances of 100 km are indicated in panel (a) with white lines. See text for details.

a variability of more than 50 dB (i.e., more than 5 orders of magnitude in RCS). Such variability cannot be attributed to changes in other parameters, e.g., electron density, atmospheric viscosity, ice density, and density gradients. However, they can be easily obtained by having coexistent ice particles with different radii \( r_A \) and therefore generating different \( S_c \), i.e., \( r_A = \sqrt{S_c}/6.5 \) (e.g., Cho et al., 1992; Rapp and Lübken, 2003). Therefore, given that KAIRA observations correspond to MAARSY SNR greater than \( \sim 30 \) dB, i.e., \( \eta > 5 \times 10^{-14} \text{ m}^{-1} \), we claim that such common observations arise from high \( S_c \). Previous multi-wavelength studies have been also focused on PMSEs with high \( S_c \) (e.g., Hoppe et al., 1990; Belova et al., 2007; Naesheim et al., 2008; Rapp et al., 2008; Li et al., 2010; Li and Rapp, 2011).

High \( S_c \) means that the observations occur in the viscous–convective subrange and therefore the PMSE RCS will have a \( k_{B}^{-3} \) (or \( \lambda_{B}^{-3} \)) dependence at the Bragg wavelengths of interest, i.e., \( \lambda_{B} < 3 \text{ m} \). In other words, we are ruling out a higher dependence on \( \lambda_{B} \) at the wavelengths of interest, since such dependence will require small \( S_c \) (see Fig. 1a). Our PMSE measurements fall in the region between the green and red continuous lines in Fig. 1a, i.e., covering \( S_c \) between 100 and 900 within a narrow region of RCS that spans about half an order of magnitude. The red curve (\( S_c = 900 \)) is still in the power law regime, while the green curve (\( S_c = 100 \)) is going down into the exponential regime.

Following these considerations, we now discuss the results related to PMSE drifting structures and to the PMSE angular dependence, separately. In addition, we briefly discuss other observed features and future plans.

5.1 PMSE drifting structures

The half-parabolic structures seen in Fig. 5a are typical signatures of horizontally drifting structures. We have verified that this is the case by overlaying the expected trajectory (total range vs. time) of a structure drifting at a constant velocity at 85 km altitude, and the match is perfect. To continue the analogy of a typical drifting echo, e.g., airplanes, the left half of the parabolic signature is not observed given that the KAIRA receiver beam points towards MAARSY (see Fig. 3b). Therefore the left structures, i.e., between KAIRA and the middle point, are below KAIRA’s sensitivity.

The horizontal distance between the middle point and MAARSY at 85 km is \( \sim 90 \) km. Our results also show that these PMSE structures with high \( S_c \) have a limited volume of approximately 5–15 km of horizontal extent in the KAIRA–MAARSY direction. Moreover, these PMSE “clouds” (limited-volume structures) present horizontal separations ranging from 20 to 60 km. These approximate distances and sizes have been obtained from Fig. 7a, specifically from comparing the SNR structures with the over-plotted 100 km estimated horizontal sections. It is important to stress that the horizontal structures we have identified are for PMSEs with high \( S_c \). A more sensitive bistatic radar configuration would have observed PMSEs all the time, i.e., without spatial gaps, but with varying RCSs.

The obtained horizontal and vertical features of PMSEs with high \( S_c \) are consistent with NLC structures as known from observations with lidar, airglow imagers, and ground-based NLC photography. For example, using lidars the NLC half-power full-width in height is approximately 1 km (e.g., Fiedler et al., 2009). Drifting NLC bright clouds with horizontal separations between 10 and 40 km are also typical of NLC observations (e.g., Baumgarten and Fritts, 2014, Fig. 2). A sketch of what we are observing can already be found in Fig. 2. PMSE clouds drift from the middle point between KAIRA and MAARSY to MAARSY. These clouds are of different sizes and have different separations. KAIRA is only able to observe the light brown clouds (PMSE with high \( S_c \)), while MAARSY alone (i.e., monostatic) can observed the light brown and also the blue clouds (PMSE with lower \( S_c \)). So, the empty regions observed by KAIRA are not really empty; they are filled by blue clouds that are “invisible” to KAIRA.

NLC observations with high-resolution cameras from the ground imply that even horizontal features with smaller scales should be measured by radar, less than 1 km, and even at meter scales (e.g., Baumgarten and Fritts, 2014). Such
scales, less than a kilometer, are not possible in the current configuration. Recently, Sommer and Chau (2016) have been able to identify horizontal structures with sizes around 1 km using radar imaging and antenna compression techniques. We are planning to improve this resolution by using a combination of compressed sensing (Harding and Milla, 2013) and multi-input multiple output (MIMO) techniques (Urco et al., 2018).

The drifting nature of PMSE structures has been hypothesized before and sometimes characterized by simultaneous measurements at sites separated by 100–150 km (e.g., Bremer et al., 1996; Rapp et al., 2008). Our measurements are the first to show directly such drifting PMSE structures with high $S_c$ as well as the limited-volume horizontal sizes and separations of few tens of kilometers between them.

Although our results are encouraging to further understand the temporal and spatial characteristics of PMSEs and their relation to atmospheric dynamics and chemistry responsible of such characteristics, more detailed observations are needed. In our particular case, the whole PMSE region has experienced almost the same horizontal wind with a strong component in the KAIRA–MAARSY direction. This is not necessarily always the case; sometimes strong wind shears are observed. For example using an EISCAT VHF tristatic experiment, Mann et al. (2016) observed that the upper part of PMSE moved in the opposite direction from the lower part. In that case, our observations would have shown the left–right part of the parabola for structures going towards KAIRA–MAARSY; assuming that the limited-volume structures are maintained and move primarily in the KAIRA–MAARSY direction.

5.2 PMSE angular and wavelength dependence

A byproduct of our observations is the possibility of studying the angular dependence of PMSE. As indicated in Fig. 3f, our bistatic configuration allows for measurements with zenith angles ranging from 0° (middle point) to ~33° (over MAARSY). To follow the previous literature, here we also characterized the angular dependence as follows

$$\eta(\theta) \propto \exp\left(-\frac{\sin^2 \theta}{2\sin^2 \theta_S}\right).$$

Before 2014, we would not have expected to observe these echoes given the high aspect sensitivity values reported in the literature, i.e., $\theta_S = 2–3^\circ$, particularly when so-called spaced antenna methods were employed (e.g., Zecha et al., 2001; Smirnova et al., 2012). Using a combination of vertical and oblique beams, the resulting values vary significantly, i.e., $\theta_S = 5–15^\circ$ (e.g., Czeczowski et al., 1988; Huaman and Balsley, 1998; Zecha et al., 2001). Sommer et al. (2016), using many months of MAARSY multi-beam data, have hypothesized that PMSEs are statistically due to localized isotropic scattering structures. Moreover, their hypothesis has been supported by Sommer and Chau (2016) who observed PMSE structures with sizes around 1 km, i.e., smaller than the illuminated volume. Encouraged by the latter observations, we decided to add the MAARSY PMSE observations to the originally planned MMARIA campaign with KAIRA, i.e., the results we present here.

To determine the angular dependence, first we calculate the expected angular dependence, assuming isotropic scattering. Moreover, we are assuming a narrow layer in altitude, centered at 85 km with a Gaussian width of 1 km. The expected received power is obtained after numerically integrating Eq. (3), taking into account a range sampling of 300 m and $k_B^{-3}$ dependence in $\eta$. We have simulated two scenarios: (a) assuming ideal antenna patterns like those shown in Fig. 3 (Model 1) and (b) using a MAARSY antenna pattern with a random uniformly distributed amplitude varying from 0.2 to 1 in all 433 elements (Model 2). Model 2 simulates an extreme case of an antenna array with unmatched antenna elements. Measuring the actual power levels of the antenna side lobes is not an easy task. In both cases the range dependence has been already considered.

In Fig. 8a we show the resulting normalized received power as a function of total range for Model 1 and Model 2 with black solid and dashed lines, respectively. The main difference between the two is the expected received power arising from the side lobes, i.e., the closer ranges. We compare the model profiles with three power profiles obtained from measurements: measurement 1, along the black curve shown in Fig. 5a; measurement 2, average power between 06:40 and 07:25 UT; and measurement 3, average power between 07:30 and 08:30 UT. The resulting measurement profiles are shown in red, green, and blue, respectively. In all three cases, the profiles have been self-normalized to their peak value, which corresponds to measurements over MAARSY.

Figure 8. (a) Normalized power cuts as a function of total range for three different time periods in Fig. 5a in red, green, and blue. The expected relative power for an isotropic scattering is indicated in black. (b) Power ratio between measurements and isotropic power. Fitted curves centered at 0° are indicated in dashed-dotted lines.
Assuming that the same scattering center drifts from KAIRA to MAARSY and remains unchanged during this time (a few tens of minutes), we proceed to analyze their angular dependence by comparing the measurements to the model outputs. The received power ratios, measurements over models, are shown in Fig. 8b, with Model 1 in solid lines and with Model 2 in dashed lines. The color represents, as before, which measurements were used. On top of the ratios with Model 1 we plot the fits to Eq. (4) with dashed-dotted lines. The resulting $\theta_s$ values are 12.10, 12.80, and 13.19° for measurements 1, 2, and 3, respectively. In the case of Model 2, $\theta_s$ is greater than 20°, but the obtained ratio profiles do not behave like Eq. (4).

Using the same procedure in Model 1 (ideal antenna gain) for a MAARSY–MAARSY configuration (monostatic), we found that the expected power ratio of MAARSY measurements over KAIRA’s measurements is 27 dB. Comparing this difference to the empirically determined difference of 30 dB, the difference in power with respect to isotropic scattering at 33° zenith angle is $-3$ dB, i.e., an equivalent $\theta_s \sim 27.55^\circ$. In the case of MAARSY–MAARSY configuration using Model 2 (imperfect antenna gain), the expected ratio is 21.39 dB, i.e., a difference of 8.61 dB at 33° and $\theta_s \sim 15.87^\circ$. In both cases, the actual values could be a few dB less if the real antenna pattern of the KAIRA dipoles were included.

As one can see, we obtained different values of $\theta_s$ depending on what portion of the data we use and which assumptions we make. From a simple inspection, Model 2 qualitatively has a better agreement with observations, i.e., power levels are almost constant at large zenith angles. However, when compared to the angular dependence of Eq. (4), the agreement is better with Model 1. We have assumed that the same PMSE structure drifts without changing much from KAIRA to MAARSY. Moreover, the PMSE clouds are elongated in the north–south direction and drift mainly in the zonal direction. In reality this might not be the case, since we cannot measure the horizontal velocity transverse to the KAIRA–MAARSY direction, and PMSE RCSs might have changed, spatially and temporarily, during the drifting process. Typically, correlation times of 2.8 m PMSE irregularities are on the order of seconds, while the observed kilometer-scale drifting structures appear to be frozen for a few tens of minutes. The deviation from our assumptions, i.e., the spatial and temporal evolution of PMSE RCS, might be the main reason for the lack of consistency of the angular dependence using different methodologies.

In general, the results are not perfectly consistent; i.e., we cannot explain all the observations with the simple Gaussian model of Eq. (4). However, we can conservatively conclude that our measurements indicate that by using the simple Gaussian model, the true $\theta_s$ for this event is greater than 12°; i.e., the scattering cannot be considered highly aspect sensitive. These results are in general consistent not only with previous multi-beam experiments but also with the suggestion by Sommer et al. (2016); i.e., PMSE scattering is in general not highly aspect sensitive as previously reported, but instead the scattering is due to limited-volume (localized) isotropic structures.

The small differences between our estimates and the suggestion of Sommer et al. (2016), i.e., between slightly isotropic and isotropic, might be due to (a) unknown behavior of the antennas at the side lobe levels and/or (b) selection of PMSEs with high $S_c$. For the former, estimating the actual gain of side lobes is not trivial given that the mutual coupling of closely located neighboring antennas is hard to characterize. In case of the latter, Sommer et al. (2016) included all PMSE measurements during a month, with varying $S_c$; therefore the structures with larger $S_c$ could be less isotropic than structures with lower $S_c$.

**Other features and future plans**

In our results, we have used existing PMSE scattering theories, all of them showing a well-defined $k_B^{-3}$ for the meter-scale irregularities at high $S_c$ (viscous–convective subrange) and an exponential decay at smaller scales (viscous–diffusive subrange) (see Eq. 1). In the viscous–diffusive subrange all theories show that RCS increases with turbulence intensity. However, in the viscous–convective subrange, our simulations show that PMSE RCS decreases with increasing turbulence intensity (see Fig. 1b) in the viscous–convective subrange. Such behavior is not reproductive using the expressions provided by Rapp et al. (2008) and Varney et al. (2011). Although difficult to validate observationally, unless the other parameters are measured (e.g., electron density, density and ice gradients), we think it is worth investigating such behavior, both theoretically and experimentally.

In Fig. 6c, we show two well-separated populations of polar mesospheric echoes in the summer based on their SNR vs. spectral width behavior, i.e., RCS vs. turbulence intensity. The ice-dominated population belongs to the majority of PMSE events previously reported. The turbulence-dominated echoes correspond to (a) echoes occurring below the typical PMSE altitudes, in our case around 75 km, and (b) echoes occurring at the top of PMSEs, presumably with small particles sizes, i.e., small $S_c$. A similar behavior has been shown using EISCAT 224 MHz by Rapp and Hoppe (2006). In the case of the echoes occurring around 75 km, they might not strictly speaking be called PMSEs, but their existence, besides enhanced turbulence, might require a way to reduce their diffusion time. The altitude is too low for ice, though. Its existence might be related to some of the mesospheric echoes observed at equatorial latitudes (e.g., Lehmacher et al., 2009) and polar mesospheric echoes observed in winter (e.g., Latteck and Strelniкова, 2015) that cannot be explained by pure turbulence arguments.

In future experiments, we plan to improve the measurements by focusing on PMSEs and making better use of MAARSY and KAIRA capabilities. For example, we plan to...
steer MAARSY in different directions towards KAIRA and generate also different KAIRA beams towards MAARSY simultaneously. In this way, we would improve the quality of the observations, the spatial coverage, and the angular dependence. This type of observations would be a good complement to current NLC studies from the ground, since they can be done independently of weather conditions as long as there are some electrons and sufficient ice particles with relative large radius (i.e., high $S_c$). Moreover, the MAARSY observations close to overhead bring the additional advantage that it allows for the observations of echoes due to ice particles with smaller sizes than those responsible of NLCs. Besides the improved PMSE characteristics, the proposed improved experiments would also allow wind field measurements around the summer polar mesopause with unprecedented temporal and spatial resolutions. Instead of specular meteor echoes, one could applied the MMARIA approach (e.g., Stober and Chau, 2015; Chau et al., 2017) to PMSE observations at multiple locations and from different observing angles.

6 Conclusions

We show for the first time direct evidence of PMSE limited-volume structures drifting with the background atmospheric wind using a combination of monostatic and bistatic observations. The observed structures have horizontal sizes between 10 and 20 km, separations between 20 and 60 km, and vertical widths of less than 1 km. These features have been observed on PMSEs with high $S_c$ and are consistent with previously reported features of NLCs.

We have also investigated the angular dependence of these PMSEs with high $S_c$. We find that during this event, PMSE scattering is in general not highly sensitive to its aspect. A conservative lower bound estimate for the aspect sensitivity parameter is $\theta_s = 12^\circ$. Depending on the measurements and assumptions we make, the estimate gets closer to isotropic. Our results are consistent with most recent works on PMSE angular sensitivity that indicate that PMSE scattering is mainly composed of localized (limited-volume) isotropic structures.

Improved experiments using the full beam steering and beam forming capabilities of MAARSY and KAIRA, respectively, will be helpful to (a) better resolve the PMSE spatial and temporal characteristics at 10–100 km scales and (b) improve the angular dependence of PMSEs, at least at large $S_c$. Besides studying the spatial–temporal features of PMSEs, the results of improved experiments could be used to get wind field estimates with unprecedented spatial and temporal resolutions using PMSEs as tracers in an MMARIA approach, which utilizes a multi-static network of low power all-sky illuminating radars.

References


Data availability. The MAARSY and KAIRA spectra data are available; interested users can contact the main author for the MAARSY and KIRA spectral data. MAARSY raw data may be requested from Ralph Latteck.

Competing interests. The authors declare that they have no conflict of interest.

Special issue statement. This article is part of the special issue “Layered phenomena in the mesopause region (ACP/AMT international SI)”. It is a result of the LPMR workshop 2017 (LPMR-2017), Kühlungsborn, Germany, 18–22 September 2017.

Acknowledgements. We would like to thank Irina Strelnikova for her suggestions for improvements and for providing suitable references. We would also thank Kiara Chau for preparing the MAARSY–KAIRA sketch. This work was partially supported by the WATILA Project (SAW-2015-IAP-1). KAIRA was funded by the University of Oulu and the FP7 European Regional Development Fund and is operated by Sodankylä Geophysical Observatory with assistance from the University of Tromsø.

Edited by: Martin Dameris
Reviewed by: three anonymous referees


McKee, J. L. Chau et al.: PMSE drifting structures 9559


