Analyzing Families of Experiments in SE: A Systematic Mapping Study

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Abstract—Context: Families of experiments (i.e., groups of experiments with the same goal) are on the rise in Software Engineering (SE). Selecting unsuitable aggregation techniques to analyze families may undermine their potential to provide in-depth insights from experiments’ results.

Objectives: Identifying the techniques used to aggregate experiments’ results within families in SE. Raising awareness on the importance of applying suitable aggregation techniques to reach reliable conclusions within families.

Method: We conduct a systematic mapping study (SMS) to identify the aggregation techniques used to analyze families in SE. We outline the advantages and disadvantages of each technique according to mature experimental disciplines such as medicine. We provide preliminary recommendations to analyze and report families in view of families’ joint data analysis common limitations.

Results: Several aggregation techniques have been used to analyze SE families: Narrative synthesis, Aggregated Data (AD), Individual Participant Data (IPD) mega-trial or stratified, and Aggregation of p-values. The rationale to select aggregation techniques is rarely discussed within families. Families are commonly analyzed with unsuitable aggregation techniques according to mature experimental disciplines.

Conclusion: Data analysis’ reporting practices should be improved to increase the reliability and transparency of joint results. AD and IPD stratified seem suitable to analyze SE families.

Index Terms—Family of experiments, Meta-Analysis, Narrative Synthesis, IPD, AD.

1 INTRODUCTION

In 1999, Basili et al. used the term family of experiments to refer to a group of experiments that pursue the same goal and whose results can be combined into joint —and potentially more mature— findings than those that can be achieved in isolated experiments [1]. In particular, families of experiments allow to increase the reliability of the findings [2], increase the statistical power and precision of results [3], and assess the impact of experimental changes (i.e., moderators) on results [4], [5], [6].

However, Basili et al.’s definition of family of experiments does not set apart two types of groups of experiments: those gathered by means of Systematic Literature Reviews (i.e., SLRs, a type of secondary study) that aims to bring together all the available empirical evidence on a particular topic in a systematic way [7]), and those gathered by means of experimental replication —where replications are either conducted by the same researcher or a group of collaborating researchers that share experimental materials, assist to each other during the design, execution and analysis phase of the experiments, etc. [8], [9], [10]. In our opinion, such groups of experiments should be set apart as they grant access to different information and in turn, they may serve to fit different purposes.

For example, while researchers in groups of replications have access to the raw-data of all the experiments (as after all, they have conducted the experiments), this is not guaranteed in SLRs (unless the raw-data are requested to primary studies’ authors and they are willing to share them). Thus, while researchers in the prior can apply consistent data-cleaning, data-processing and data-analysis techniques to ensure that differences across experiments’ results are just caused by differences in the data gathered, this is not feasible in SLRs —as potentially different data processing and analysis techniques may have been followed to analyze each individual experiment [11]. This may be detrimental to the reliability of SLRs’ joint results.

Also, while researchers in groups of replications are fully aware of the settings and the characteristics of the participants across all the experiments, just the information reported in research articles is available in SLRs. If this information is scarce or incomplete due to reporting inconsistencies or length restrictions, this may limit SLRs’ appropriateness to elicit moderator variables (as some moderators may pass unnoticed to the researchers aggregating results).

Another key difference between groups of experiments built by means of replication and those gathered by means of SLRs is that researchers in the prior may opt to introduce isolated changes across experiments with the aim of studying their effects on results. In contrast, experiments gathered by means of SLRs have already set conditions, and thus, differences across experiments’ results may be coming from a potential “amalgamation” of effects due to the multiple elements changed across the experiments. So, researchers building groups of replications can avoid the potential impact of introducing multiple simultaneous changes across experiments and thus, minimize the amount
of confounding variables impacting results. In turn, this would not just reduce the bias of joint results, but also the bias of moderator effects [12], [13], [14].

Finally, as groups of experiments gathered by means of replication do not rely on published data to provide joint results (contrary to groups of experiments in SLRs), they do not suffer from the bias introduced in results due to selective publication [11]. Thus, groups of replications may provide potentially less biased conclusions—albeit less generalizable results, as they typically involve fewer experiments—than those provided by SLRs.

To distinguish between groups of experiments gathered by means of SLRs and those gathered by means of replication, we refine Basili et al.’s definition of family of experiments and consider a family as a group of experiments where researchers have first-hand knowledge of all experiments’ settings and have full access to their raw-data. Along this research we focus just on the techniques that have been used to aggregate experiments’ results within families and not on those applied in SLRs—where the de facto aggregation technique is meta-analysis of effect sizes [7].

This investigation starts from the observation that not much research, if any, seems to have been conducted about the aggregation techniques that have been used in SE to analyze families. Selecting inappropriate aggregation techniques may lead to misleading findings, and in turn, to undermine all the effort involved in conducting a family (e.g., coordinating different research groups for conducting replications across multiple sites, having face-to-face and internet meetings, preparing and translating experimental materials to share among researchers from different countries, etc.).

In this article we conduct a Systematic Mapping Study (i.e., SMS, a type of secondary study where an overview of a specific research area is obtained [15]) with the aim of identifying the techniques that have been used to aggregate experiments’ results within families in SE. In addition, we conduct a literature review in mature experimental disciplines such as medicine and pharmacology to learn about the advantages and disadvantages of each technique. Finally, we tailor a preliminary set of recommendations to analyze and report families based on the common limitations that we found with regard to joint data analysis in SE families. Along the way, we made the following findings:

- Families of experiments in SE are commonly constituted by three to five experiments with small and dissimilar sample sizes and multiple changes across experiments. Families usually involve different types of subjects (e.g., professionals and students), and tend to provide heterogeneous results.
- From most to least used, Narrative synthesis, Aggregated Data (AD), Individual Participant Data (IPD) mega-trial or stratified, and Aggregation of p-values have been used to analyze families in SE. Each technique seems appropriate in different circumstances and those shall be understood before aggregating results.
- SE researchers rarely justify the aggregation technique/s used within their families. Narrative synthesis and IPD mega-trial are commonly used to aggregate experiments’ results within families despite their numerous shortcomings according to the literature of mature experimental disciplines.
- SE researchers rarely account for the heterogeneity of results that may have materialized as a consequence of the experimental changes introduced across experiments within families. SE researchers rarely acknowledge that differences across experiments’ results may have emerged just because of natural variation of results, and not because of the changes introduced across experiments.

The main contributions of this research are a map and classification of the techniques used in SE to aggregate experiments’ results within families, a list of advantages and disadvantages of each aggregation technique according to the literature of mature experimental disciplines, and a set of recommendations to analyze and report families of experiments in view of families’ common limitations with regard to joint data analysis. Along this article we argue that it is crucial to understand the advantages and disadvantages of each technique before applying them, and that also, the suitability of each technique may be influenced by the characteristics of the family undertaken. Blindly applying aggregation techniques without considering their advantages and disadvantages for the specific conditions of the family may lead to misleading conclusions, and in turn, to miss a valuable opportunity to extract in-depth insights from experiments’ results. In view of this, we suggest:

### Take-away messages

- The aggregation technique/s used within families should be justified to increase the transparency and reliability of joint results. Common justifications include the availability of the raw-data, the presence of changes across experimental designs or response variable operationalizations, the ability to convey heterogeneity of results in intuitive units, the availability of informative plots to summarize results, or the necessity of interpreting results in natural units.
- We discourage the use of Narrative synthesis to analyze families since it does not provide a quantitative summary of results and does not take advantage of the raw-data to provide joint results or investigate moderators.
- IPD mega-trial seems unsuitable to analyze families of experiments if different types of subjects (e.g., professionals and students) are evaluated within families, or if both missing data—due to protocol deviators or drop-outs—and experiments with dissimilar sample sizes are present within families.
- AD or IPD stratified seem suitable to analyze families of experiments. If multiple changes are introduced across experiments within families (as it is commonly the case in SE), random-effects models may be more suitable than fixed-effects models.
Paper organization. In Section 2 we outline the research method and the research questions of our study. In Section 3, 4, 5 and 6 we provide an answer to each of the research questions of our study. In Section 7 we provide a series of recommendations to analyze families. In Section 8 we provide a series of recommendations to report families. We outline the threats to validity of this study in Section 9. Finally, we outline the conclusions of our study in Section 10.

2 RESEARCH METHOD
We follow the guidelines proposed by Kitchenham and Charters [16] and those proposed by Petersen et al. [15] for conducting our SMS.

2.1 Objectives and Research Questions
The main objective of this study is to systematically identify relevant scientific literature and map the techniques that have been used to aggregate experiments’ results within families from the viewpoint of researchers in the context of SE. We propose four different research questions to meet our objective:

- RQ1. How are families of experiments defined and characterized?
- RQ2. What techniques have been applied to aggregate experiments’ results within families?
- RQ3. How do the changes introduced across experiments within families influence the aggregation technique/s used?
- RQ4. What limitations with regard to joint data analysis are common across families?

2.2 Search and Selection Processes
We iteratively built a search string to identify as many families of experiments as possible. The rationale behind the selection of our final search string is outlined in Appendix A.1. Our final search string was: (experiment*) AND (famil* OR serie* OR group*). A total of 1213 documents were retrieved on the 14 October 2016 from four databases: IEEE Xplore, ISI Web of Science, Science Direct and Scopus.

We needed to decide on when to consider a group of experiments as a family and exercise such decision to define our exclusion criteria. This exclusion criteria would serve us to separate families from other pieces of research. However, we had certain difficulties for this. In particular, we noticed that the distinction between replications and families was not clearly set in SE. This made us aware that family was an ill-defined term and so, we included an extra research question (RQ1) to tackle such issue. In Section 3 we provide an answer to RQ1 and motivate why we regard three experiments as the low boundary for considering a group of experiments as a family.

Eventually, we defined the following exclusion criteria:

- The article aggregates fewer than three experiments.
- The article does not compare at least two treatments (e.g., Technology A vs. Technology B) on the same response variable (e.g., quality).

1. Find Appendixes in the supplementary material.

Whenever at least one point of the exclusion criteria was met by an article, then this article was dismissed. Table 1 offers a summary of the selection process that we undertook to select families of experiments. In particular, at Stage 0 the first author went through the list of articles —by sorting them by title, year and author/s—to eliminate duplicates and non-relevant documents. The number of remaining articles at the end of this stage was 572.

In Stage 1, 2 and 3, the first two authors excluded articles by title, abstract reading or in-depth reading, respectively. In case of disagreements, the third author helped to make the decision on whether the article would make it to the next stage. Table 1 shows the number of disagreements and the number of articles making it to the next stage. At the end of Stage 3, 36 articles were considered as relevant. These 36 articles comprised our initial set of primary studies. Such primary studies were used during Stage 4 to perform a backward snowballing process (i.e., a procedure where relevant studies are gathered from primary studies’ reference lists [17]). During Stage 4, three new articles were selected as relevant. These articles were not indexed in the previous search because: (1) they referred to a group of experiments as a “set”; (2) they contained the “meta-analysis” keyword but no term for referring to the set of experiments; (3) they used the term “replication” in order to refer to a family of experiments. After all stages, we identified a total of 39 primary studies.

2.3 Extraction Process
We designed a data extraction form (Appendix B) to extract all the relevant data from each primary study. We extracted a total of 13 fields of information. We improved each field of information after a first round of screening made by the first author. The purpose of this first screening was to establish categories to classify the aggregation techniques used in families and also the different characteristics that may have influenced the selection of such techniques.

The first and second authors gathered the information of each primary study independently using the final data extraction form. 12 out of 39 articles contained at least one field where a conflict materialized. The third author was consulted to reach a final agreement in those cases. Conflicts materialized mostly with regard to experiments’ sample sizes (some articles reported the final number of subjects after data pre-processing and not others) and on the dimensions changed across experiments (e.g., in cases where it was not clear whether response variables or protocols were changed across experiments). As an example, to solve the inconsistencies in the case of sample sizes, a decision on just using the final number of subjects after pre-processing was made. In case of doubts on whether certain changes had been introduced across experiments within families, a guess could be made by the aggregation technique/s used.
3 RQ1: FAMILY DEFINITION AND ATTRIBUTES

We started this research following Basili et al’s definition of family of experiments [1]: a group of experiments that pursue the same goal in order to extract mature conclusions. However, we soon realized that this definition did not provide clear cut-off points between groups of replications and groups of experiments gathered by means of SLRs. In particular, while the scope of a SLR is likely to be wide (as all available research on a particular topic is aimed to be brought together into a joint result), in groups of replications, the goal tends to be narrower (since a small set of hypotheses on a limited set of response variables is usually aimed to be assessed). Besides, in SLRs, just what is reported in primary studies is known. Thus, some relevant information (e.g., characteristics of the participants or some characteristics of the experimental settings) may pass unnoticed if not entirely reported due to length restrictions or reporting inconsistencies —unless experimenters are contacted to share more detailed information or even to share the raw-data. Conversely, in groups of replications —either conducted by the same researcher or a group of collaborating researchers from the same or different groups and/or institutions— access to more detailed information on the experiments is guaranteed. For example, it is typical that in groups of replications researchers share among them laboratory packages, instructional material to ease the execution of experiments [18], assist each other via in-person or internet meetings during the experiment’s plan or design phase, assist each other during the execution of replications, etc. [19]. In turn, this close collaboration leads to greater knowledge about all experiments’ settings and guarantees full access to all experiments’ raw-data. Eventually, this may increase the reliability of the joint results, and in case results differ across experiments, ease the elicitation of moderators. Thus, for us, a main difference between groups of replications gathered by SLRs and those gathered by means of coordinated replications is the first-hand knowledge of all experiments’ settings and access to the raw-data.

As a consequence of the search that we conducted, we also realized that there was no exact cut-off point to discern between: (1) families of experiments; (2) a series of planned, coordinated, or opportunistic replications conducted by a sole researcher —or group of collaborating researchers—and; (3) isolated replications conducted by researchers that neither interact nor collaborate with those who run the baseline experiments.

To start answering RQ1, we consider a group of replications as a family if:

- **At least two treatments** (e.g., Technology A vs. Technology B) are explicitly exercised and compared within all experiments on a common response variable (e.g., quality). Three or more treatments may be compared, but two is the minimum. Studies where a treatment is compared with the results reported in literature (e.g., reported industry averages) are excluded. This way, we ensure that the statistical assumptions required by some aggregation techniques (e.g., normality or equality of variances assumption [20]) can be thoroughly checked before providing joint results.

- **At least three experiments** are included within the family —so it is possible providing joint results and study experiment-level moderators (e.g., programing language, testing tool, etc.). In particular, if experiment-level moderators are aimed to be assessed within families with less than three experiments, some techniques such as meta-regression (i.e., one of the procedures for studying moderators with meta-analysis of effect sizes [21]) cannot be applied—as meta-regression requires a minimum of a least three experiments because otherwise, a regression line fitted on just two data-points would explain all the variability in the data. By using this lower bound of three experiments: (1) we avoid the problem of considering an isolated replication of a baseline experiment as a family of experiments, and (2) we ensure that all aggregation techniques can be applied within families irrespective of whether it is aimed at providing joint results or investigating moderators.

- **Full access to all experiments’ raw-data** is guaranteed to ensure that homogeneous data processing, cleaning and analysis procedures can be applied to each experiment before providing a joint result. Thus, sets of replications gathered from the literature are omitted from the definition of family we propose here.

- **First-hand knowledge of the settings** is guaranteed in all experiments so it is possible minimizing the impact of potentially unknown factors on results, and in case results differ, hypothesize on which moderators may have influenced results.

- **Different subjects participate in each experiment** within the family so data are independent across experiments, as otherwise, results might be biased. In particular, if the same subjects participate across experiments, subjects’ scores may be correlated across experiments [22]. If such correlation is not accounted for within the aggregation technique, this issue may invalidate joint results [22].

<table>
<thead>
<tr>
<th>Stage</th>
<th>Goal</th>
<th>Total</th>
<th>Excluded</th>
<th>Disagree</th>
<th>Included</th>
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<tbody>
<tr>
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<td>Remove duplicates</td>
<td>1213</td>
<td>633</td>
<td>-</td>
<td>580</td>
</tr>
<tr>
<td></td>
<td>Remove non-relevant documents</td>
<td>580</td>
<td>7</td>
<td>-</td>
<td>573</td>
</tr>
<tr>
<td>Stage 1</td>
<td>Exclude studies by title</td>
<td>572</td>
<td>383</td>
<td>23</td>
<td>189</td>
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<tr>
<td>Stage 2</td>
<td>Exclude studies by abstract</td>
<td>189</td>
<td>139</td>
<td>15</td>
<td>50</td>
</tr>
<tr>
<td>Stage 3</td>
<td>In-depth reading</td>
<td>30</td>
<td>14</td>
<td>7</td>
<td>36</td>
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<tr>
<td>Stage 4</td>
<td>Snowballing process</td>
<td>36</td>
<td>-</td>
<td>-</td>
<td>3</td>
</tr>
</tbody>
</table>

TABLE 1
Summary of results across stages.
Table 2 shows the 39 families of experiments that we identified. Families are ordered in Table 2 according to family size (i.e., number of experiments). Table 2’s columns show respectively: the sample sizes of the experiment, the types of subjects participating in the family, whether the raw-data and laboratory package were provided, the publishing venue of the family, publication date and reference.2

With regard to the number of experiments within families (first column), 48% of the families include three experiments, followed by four experiments (23%) and five experiments (20%). There are just three larger families comprised by six, eight and 12 experiments, respectively. The average number of experiments included within families has increased over the years. This may suggest an improvement in the maturity of the area (since the larger the number of experiments within families, the larger the sample size, and thus, the potentially larger the reliability of joint results). However, the increase was slight: around three experiments were included within families between 1998 and 2006, while the average number of experiments in the latest years increased to four and peaked at five in 2015.

In regard to the number of subjects within families (second column), out of 39 families, 12% contained fewer than 50 subjects, whereas 48% contained between 50 and 100 subjects. The larger the number of subjects, the fewer the number of families. 12% of the families included more than 100 subjects but fewer than 150. With regard to experiments’ sample sizes (second column in parentheses), most of the experiments identified within families are comprised by between 10 to 30 subjects. The number of experiments containing between 1 and 9 subjects appears to be roughly equal to the number of experiments with 30 to 39 subjects (16 experiments and 19 experiments, respectively). As recent families have on average five experiments and around 25 subjects participate in each experiment, a rise in the total number of subjects is observable over the latest years.

Regarding to the type of subjects involved within families (third column), 38% of the families involve both graduate and undergraduate students, 25% involve both students and professionals, whereas 18% involve just undergraduates. 66% of the families were carried out just with students and professionals. Only 7% of the families were conducted entirely with professionals. The number of professionals involved across families along the years seems not to follow any pattern: the latest years increased to four and peaked at five in 2015.

With regard to whether the raw-data (fourth column)
or the laboratory package were provided in families (fifth column), the raw-data were just provided in 15% of the families (even though only 7.5% are accessible as of March 2018) and the laboratory package in 43% of the families (even though most are not accessible as of March 2018). Experimental packages seem to be provided more often from 2012 onwards, what may in turn facilitate replication of experiments. Raw-data provision seems not to have increased over the years. Unfortunately, this prevents re-analysis by third researchers with perhaps more appropriate aggregation techniques than those applied in the original articles.

Regarding publishing venues (sixth column), IST published 25% (10 out of 39) of the families, EMSE published 20% (8 out of 39), TSE published 13% (5 out of 39) and TOSEM published 10% (4 out of 39). The rest of primary studies were published in other venues.

With regard to publication date (seventh column), a steady number of families is observed between 1998 and 2004, whereas a sharp increase is observable from 2008 onwards. This increase is possibly the result of the growing interest in experimentation and the recent calls towards replication in SE. Again, the SE experimentation area might be increasing its maturity.

Finally, we want to make a last observation. In mature experimental disciplines such as medicine, the closest representative of families of experiments (i.e., multicenter clinical trials [20]) are run with pre-stablished protocols defining the experimental settings and the set of procedures that shall be strictly adhered to during the execution and analysis of experiments [23], [24], [25]. Besides, in multicenter clinical trials aiming at assessing the efficacy of new drugs, the populations under assessment across all the centers are specifically defined to ensure consistency of results and avoiding confounding effects [20], [26], [24]. In contrast, in most families of experiments in SE, families are formed without any a-priori plan, and changes are commonly introduced across experiments opportunistically, to either increase the generalizability of results, or to assess moderators. Besides, analysis decisions within SE families seem commonly driven by statistical tests’ results (e.g., normality tests’ results [27]), the example from other researchers or personal preferences (as when some authors conduct similar analyses to those undertaken in previous families). This conforms to the findings reported in medicine years ago [28].

Summarizing, families of experiments in SE tend to have the following characteristics:

- Most families are comprised by **three to five experiments** with dissimilar and small sample sizes (i.e., less than 30 subjects per experiment) and **involve around 100 participants**.
- Most families are **entirely conducted with students**. However, different types of students are commonly involved. In just three out of 39 families, professionals are the only participants.
- Almost no family provided the raw-data. Less than half of the families provided a laboratory package. **Up to date, almost none is accessible**.
- **Families seem happenstance**. In other words, families do not account with a pre-specified protocol outlining the procedures for either conducting experiments, analyzing each of them, or aggregating their results.
- Most families are published in **journals (IST, EMSE, TSE, TOSEM)**.

## 4 RQ2: Analysis Techniques Applied

Table 3 shows the techniques that have been used to aggregate experiments’ results within families (from most to least used), the amount of families that apply each technique, and the references of the families.

### TABLE 3

<table>
<thead>
<tr>
<th>Technique</th>
<th>N</th>
<th>Primary Studies</th>
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<tbody>
<tr>
<td>Narrative synthesis</td>
<td>18</td>
<td>[P21], [P25], [P4], [P12], [P14], [P13], [P29], [P2], [P32], [P35], [P37], [P10], [P16], [P9], [P36], [P11], [P19], [P20]</td>
</tr>
<tr>
<td>AD</td>
<td>15</td>
<td>[P22], [P24], [P5], [P6], [P28], [P30], [P35], [P8], [P23], [P17], [P9], [P39], [P18], [P1], [P38], [P20]</td>
</tr>
<tr>
<td>IPD mega-trial</td>
<td>13</td>
<td>[P23], [P26], [P27], [P14], [P28], [P15], [P7], [P30], [P34], [P33], [P10], [P39], [P11]</td>
</tr>
<tr>
<td>IPD stratified</td>
<td>6</td>
<td>[P21], [P25], [P31], [P16], [P36], [P3]</td>
</tr>
<tr>
<td>Aggregation of p-values</td>
<td>3</td>
<td>[P22], [P24], [P29]</td>
</tr>
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</table>

**Narrative synthesis** was used in 46% of the families. Narrative synthesis is an aggregation technique that provides a **textual summary of results as a joint conclusion** [29]. Families applying Narrative synthesis do not explicitly mention any term to refer to this aggregation technique (even though some use the term “global analysis” [P13], [P4]). In general, it is hard to distinguish whether authors are aggregating experiments’ results or just comparing them. For example, Scanniello et al. [P1] summarizes results as “...this is true of all the experiments, the only exception being [experiment X] on the [response variable] GD, where the statistical test returned a p-value equal to 0.39...”, and Staron et al. [P12] as “...in general the stereotypes improve... and half of the results were statistically significant...”. The main advantage of Narrative synthesis is that, as just a textual summary of results needs to be provided, Narrative synthesis allows to combine the findings of experiments with wildly different experimental designs, response variables or statistical tests into joint results [30], [29]. Besides, in Narrative synthesis, discordance across experiments’ results are not seen as a threat to the validity of joint results, but instead, as an opportunity to study the effect of moderators on results [6]. For example, in view that results differ across experiments, Ali et al. [P37] claim “...one plausible explanation is that participants had more experience with standard UML state machines before the experiment than Aspect state machines and hence their understandability...”, and Ricca et al. [P26] claim “...the use of stereotypes does not always introduce significant benefits... the provided material is different, and this can be the reason for different results...”.

3. We map primary studies to analysis technique/s in Section 5.
Even though using Narrative synthesis is straightforward, it has some relevant shortcomings. In particular, Narrative synthesis does not provide a joint effect size or p-value. In turn, this hinders the incorporation of results in prospective studies. Another of its main shortcomings is that a subjective weight (i.e., dependent upon the analyst) is commonly assigned to each experiment towards the overall conclusion [21] (e.g., should all experiments be weighted identically regardless of their sample size? should experiments with professionals be weighted more than those with students—as after all, professionals are more representative of what may happen in reality?). In turn, the reliability and reproducibility of results is hindered with Narrative synthesis [21].

**Aggregated Data** meta-analysis (i.e., AD) was used in 38% of the families. AD is commonly known in SE as meta-analysis of effect sizes, and is the de facto aggregation technique to aggregate experiments’ results in SLRs [7]. Families’ authors refer to AD simply as meta-analysis: “the set of statistical techniques used to combine the different effect sizes of the experiments” [P8]. Effect sizes quantify the relationship between two groups (or more generally, between two variables: the dependent and the independent variable [21]). Effect sizes can be computed from experiment’s summary statistics (e.g., means, standard deviations and sample sizes [31]) or from statistical tests’ results (e.g., t-test’s t-value and degrees of freedom [27]).

Effect sizes are commonly divided into two big families [32]: the r family and the d family. The r family’s effect sizes quantify the strength of relationship between two variables. The strength of this relationship is usually provided as a Pearson correlation [27]. For example, Gonzalez et al. [P18] calculated the Pearson correlation between two variables in each experiment and then aggregated them using AD. Manso et al. [P5] followed an identical procedure but this time, they used the Spearman correlation instead (a non-parametric correlation coefficient [27]). The d family’s effect sizes quantify the difference between the means of two groups. The size of the difference is usually conveyed in standardized terms as to rule out differences across experiments’ response variable scales. Cohen’s d or Hedge’s g [33], [34] are common representatives of the d family in SE [35]. For example, Fernandez et al. [P35] analyzed each experiment with the U-Mann Whitney (the non-parametric counterpart of the independent t-test) and aggregated all experiments’ Hedge’s gs into a joint result by means of AD.

AD is a statistical technique that delivers a weighted average of all experiments’ effect sizes as a joint effect size [21]. Generally speaking, the weight given to each experiment towards the joint result with AD is directly proportional to the sample size of the experiment—if a fixed-effects model is used [21]— or to the sample size of the experiment and the total heterogeneity of results (i.e., the variability of results that cannot be explained by natural variation) —if a random-effects model is used [21].

One of the main advantages of AD is that it can be used to combine the results of experiments with different designs and response variable scales into a joint conclusion —as long as a suitable standardized effect size can be calculated [21], [36]. In addition, AD can easily handle heterogeneity of results (by simply fitting a random-effects model instead of a fixed-effects model [21]) or elicit experiment-level moderators (e.g., by using meta-regression or sub-group meta-analysis [21]). Other advantages of AD are its intuitive visualizations (i.e., forest-plots [21]) and its straightforward statistics to quantify heterogeneity (e.g., I^2 [21]).

Figure 1 shows an example of forest-plot. As it can be seen in Figure 1, the effect size of each experiment is represented by a square. The size of each square represents the weight of the effect size in the overall result (see the black diamond at the bottom) and the width of the line crossing each square represents the uncertainty of the effect size in each experiment (i.e., its 95% confidence interval [36]). Furthermore, the assessment of the heterogeneity is straightforward by means of the I^2 statistic (e.g., the heterogeneity can be small, medium or large if the I^2 statistic is larger than 25%, 50% or 75% respectively [21]).

Even though appealing, AD has among its main limitations that it cannot assess at the same time the effect of multiple factors on results (e.g., the effects of the treatments, experimental tasks and their interactions) and instead, AD is commonly applied to just aggregate experiments with relatively simple designs [21]. Another shortcoming of AD is that effect sizes’ statistical assumptions need to be checked before providing joint results (e.g., normality or homogeneity of variances for Cohen’s d [37][38][39]).

**Individual Participant Data mega-trial** (i.e., IPD mega-trial) was used in 33% of the families. In IPD mega-trial, the raw-data of all experiments are pooled together into a joint data-set and then analyzed as if the raw-data were coming from a single “big” experiment [P27]. Families’ authors in SE name IPD mega-trial after the statistical model being applied (e.g., ANOVA, GLM, etc. [P11]). As an example of its application, Cruz et al. [P28] analyzed individually each experiment by means of the Kruskal-Wallis test (i.e., the non-parametric counterpart of the one-way ANOVA [27]) and then pooled together all experiments’ raw-data into a joint data-set to analyze them jointly with the same test. Ricca et al. [P26] followed an identical procedure, but this time with the Wilcoxon test (i.e., the non-parametric counterpart of the dependent t-test [27]). Table 4 shows the IPD mega-trial

Fig. 1. Forest-plot: AD example.
Despite its intuitiveness, IPD mega-trial may provide biased results if experiments are unbalanced across treatments (e.g., due to missing data because of protocol deviations or drop-outs) and have different sample sizes, or if subjects resemble more to each other within the same experiment than across experiments [41, 42, 43] (e.g., what may happen when experiments with either professionals or students are run within families). As a result, the use of IPD mega-trial is commonly discouraged [41, 42, 43].

Another disadvantage of IPD mega-trial is that some statistical tests cannot analyze jointly experiments with different designs. For example, if within-subjects experiments (i.e., repeated-measures experiments) and between-subjects experiments need to be analyzed together by means of a repeated-measures ANOVA [27], the repeated-measures ANOVA “throws away” all the data coming from between-subjects experiments (because data in such experiments are not repeated within subjects). Another shortcomings of IPD mega-trial are that it needs all experiments to use identical response variable scales—as otherwise, the joint effect provided may be biased depending upon their operationalizations [11]—and that IPD mega-trial statistical models are built on top of some statistical assumptions (e.g., normality or homogeneity of variances assumption [27]) that need to be checked before interpreting results. Finally, heterogeneity of results across experiments cannot be included within IPD mega-trial statistical models (as the experiment where the raw-data come from is not accounted for in IPD mega-trial). However, IPD mega-trial’s statistical flexibility is a plus: some statistical models (e.g., ANOVA [27]) allow to include as many factors as desired to model the relationship between the data and the characteristics of the family. For example, Ricca et al. [P14] fitted an IPD mega-trial ANOVA model with experience (i.e., undergraduate, graduate, research assistant), and separately another ANOVA with ability (high and low) with the aim of checking the effect of experience and ability on results, respectively.

Individual Participant Data stratified (i.e., IPD stratified) was applied in 15% of the families. As in IPD mega-trial, IPD stratified involves the central collection and processing of all experiments’ raw-data into a joint data-set. However, instead of analyzing the raw-data jointly as coming from a single “big” experiment, in IPD stratified, a factor representing the experiment where the raw-data come from is included within the statistical test [28]. This relationship is considered within statistical models by including an extra factor within statistical models: “Experiment”. As an example, commonly applied IPD stratified statistical tests are ANOVAs accounting for two factors: “Treatment” and “Experiment”. Again, families’ authors using IPD stratified refer to it after the name of the technique applied (e.g., ANOVA [P21], linear regression [P3], etc.)—even though some have called it comprehensive analysis [P16]. As an example of its application, Runeson et al. [P31] analyzed individually each experiment with a Wilcoxon test and then the family as a whole with an ANOVA model including “Treatment” and “Experiment” as factors. Table 5 shows the IPD stratified statistical models applied within families. Table 5 shows that ANOVAs are the most used in IPD stratified [27].

Contrary to IPD mega-trial, IPD stratified allows to include heterogeneity of results across experiments. In addition, IPD stratified allows to include flexible statistical assumptions within statistical models (e.g., different variances across experiments vs. identical variance across experiments, etc.) so as to increase the reliability of joint results [20]. IPD stratified is considered as the gold-standard in medicine to analyze groups of interrelated experiments when the raw-data are accessible [44, 45, 28].

The main shortcomings of IPD stratified are its complexity for assessing heterogeneity of results (as no straightforward statistic such as $I^2$ is yielded by IPD stratified models), its reliance on identical response variables across experiments for providing joint results, and the difficulty of fitting and checking the statistical assumptions of some relatively complicated statistical models (e.g., Linear Mixed Models [20]).

Finally, Aggregation of $p$-values was used in just 7% of the families. In Aggregation of $p$-values, all one-sided experiment’s $p$-values are pooled together by means of a statistical model such as Fisher’s or Stouffer’s method [21]. For example, Laitenberger et al. [P22] analyzed each experiment with a one-sided dependent $t$-test and then pooled their $p$-values into a joint $p$-value by means of the Fisher method. Aggregation of $p$-values main advantage is that it can aggregate the $p$-values of experiments with whatever design, response variables or statistical tests into joint results [46], [47], [20]. Unfortunately, among Aggregation of $p$-values’ main advantages are that it cannot provide a joint effect size - but just a joint $p$-value. In turn, as $p$-values confound effect size and sample size (i.e., a small $p$-value may emerge because of a large and relevant effect size, or due to a huge sample size and an almost negligible effect size [36]), the interpretability of results is not straightforward [21], [20]. Another of the main disadvantages of Aggregation of $p$-values is that in its basic procedures (e.g., Fisher or Stouffer’s methods [21]) an identical weight is assigned to each experiment regardless of its quality or sample size. This may affect the reliability joint results [20].

6. Even though more advanced Aggregation of $p$-values techniques exist also [20], just the Fisher’s and Stouffer’s methods [21] have been used in SE.
Table 6 shows a summary of the advantages and disadvantages of each technique to analyze families of experiments.

5 RQ3: Technique Selection Within Families

The changes introduced across experiments within families may impact the suitability of the aggregation technique/s applied. For example, Runeson et al. [P36] claimed that as many changes were made in the third experiment, its results could not be aggregated [P36]. This argument was also used previously in SE to prevent aggregation of experiments’ results [P36]. Thus, we thought it would be sensible to investigate whether certain changes across experiments within families hindered or benefited the application of certain aggregation techniques.

According to Gomez et al. [2], different dimensions can be changed across experiments:

- **Operationalization**: refers to the operationalization of the treatments, metrics and measurement procedures used within the experiments (e.g., response variable scales, the use of test cases or experts to score participants’ solutions, etc.)
- **Population**: refers to the characteristics of the participants within the experiments (e.g., students vs. professionals, different skills and backgrounds, etc.)
- **Protocol**: refers to the “apparatus, materials, experimental objects, forms and procedures” used within the experiments (e.g., experimental tasks, experimental session length, training duration, etc.)
- **Experimenter**: refers to the personnel involved within the experiments (e.g., the trainer, the measurer, the analyst, etc.)

Table 7 shows a map between the families that we identified (first column), the aggregation techniques that they used (second column, where the aggregation techniques may be [Narrative synthesis], [Aggregation of [P]-values, [AD], [IPD Mega-trial or IPD Stratified]], the dimensions that changed across their experiments (third column, where the dimensions changed may be the [O]perationalization, [P]opulation, [P]rotocol or [E]xperimenters), and other information that we will discuss later.

The population dimension is the one that varies the most within families. Populations are commonly changed across experiments to increase the external validity of results [P21], [P13], [P1]. For example, Porter and Votta [P21] claimed that one of the goals of their family was to “...extend the external credibility of our results by studying professionals developers...”. Unfortunately, introducing population changes across experiments may potentially affect the effect size being estimated and thus, impact conclusion validity [2]. For example, a treatment could be effective for students but not for professionals (or vice versa). In such circumstance, as each experiment is estimating a potentially different effect size, and as experiments’ sample sizes are usually small in SE, an “amalgamation” of potentially unreliable effect size estimates is being offered as a joint result within families—if a fixed-effects model such as ANOVAs, linear regressions or fixed-effects meta-analysis models are used [21], [20], [49] (as it is commonly the case within families). This issue becomes more relevant the larger the number of changes introduced across experiments [2] and the smaller the sample sizes [50].

Judging by the number of dimensions changed within families and the frequencies of use of each aggregation technique, we cannot observe any relationship between the number of changes introduced and the aggregation technique/s used. For example, it would have been expected to find the more strict techniques (i.e., IPD mega-trial or stratified) being applied less often than others such as Narrative synthesis in families with many dimension changes. Even though the number of IPD mega-trial analyses conducted in such cases seems small (only five families with three or four dimension changes used IPD mega-trial), almost all IPD stratified analyses have been conducted in families introducing three to four dimension changes across the experiments. We read this as preliminary evidence suggesting that researchers seem not to follow a procedure for selecting aggregation techniques driven by the characteristics of the family. This agrees with the findings made in medicine years ago [28].

We identified several other elements that may have also influenced the selection of the aggregation technique/s. The
rest of the columns of Table 7 go over such elements. Let us examine them one by one.

Response variable changes appear in the fourth column of Table 7. As IPD cannot accommodate different response variables across experiments, changing response variables’ operationalizations may hinder the application of IPD and at the same time, increase the appeal of other techniques (e.g., AD with standardized effect sizes such as Cohen’s d). According to Table 7, response variables’ operationalizations rarely change across experiments (only in 20% of the families, including families where we lack information). As expected, whenever response variables’ operationalizations change, either AD, Narrative synthesis or Aggregation of p-values were used to aggregate experiments’ results. Even though Narrative synthesis and Aggregation of p-values seem appealing in this circumstance, we recommend to use AD instead (e.g., as Scanniello et al. did [P1]), as AD weights transparently each experiment towards the joint result and thus, increases the reliability and transparency of results, and at the same time, provides an effect size and a p-value, and thus, allows to assess both the relevance and the significance of results [35] —contrary to Aggregation of p-values that just provides a p-value and Narrative synthesis that provides no quantitative summary of results.

Experimental design changes appear in the fifth column of Table 7. As some IPD models cannot accommodate groups of experiments with different experimental designs (e.g., repeated-measures ANOVA can only analyze experiments with within-subjects designs [27]), introducing changes across experiments’ designs may hinder the application of IPD and favour the application of other techniques such as Narrative synthesis, AD or Aggregation of p-values. As shown in Table 7, design changes were rarely introduced across experiments within families (in only 15% of the families). In 66% of those families, Narrative synthesis was used. For example, Juristo et al. [P2] analyzed independently each experiment with an ANOVA model with four factors (i.e., Technique, Program, Version and Fault) and then categorized each factor into three categories (i.e., non-significant, significant or “doubtful”), depending on the number of times each factor was significant across experiments. In spite of its appeal, Narrative synthesis may be specially dangerous given the small sample sizes common in SE experiments [51] and thus, the large variability of results expected because of natural variation of results [52]. For example, if two exact replications, each with a statistical power of 30% are conducted (and thus, there is a 30% probability of obtaining statistically significant results in each), there is a 0.09 (i.e., 0.30 * 0.3) probability of achieving two statistically significant results and a 0.49 (i.e., 0.70 * 0.70) probability of obtaining two non-significant results. Thus, there is a 0.42 (i.e., 1 - 0.49 - 0.09) probability of obtaining one significant and one non-significant result and thus claiming conflicting results -when in reality both experiments’ estimate exactly the same population effect size [36], [14]. In addition, finding two non-significant results across two different experiments does not imply that the joint result is not statistically significant [21]; simply that larger sample sizes would have been required to achieve statistical significance in each individual experiment [36].

The analysis technique/s used to analyze each experiment individually within families are shown in the last column of Table 7 (i.e., [A]NOVA, [N]on-parametric, [T]test, [C]orrelation, [R]egression, [O]thers or None (-)). We assessed the techniques used for analyzing each experiment individually as it may be “tempting” to use the same technique for analyzing the family as a whole if all experiments are identical (e.g., by pooling the raw-data of all experiments together and then analyzing them as coming from a “big” experiment).

As it can be seen in Table 7, non-parametric statistical tests (e.g., U-Mann Whitney, Wilcoxon, etc. [27]) have been largely used to analyze individual experiments within families (in 51% of the families). The most common reason for using non-parametric tests seems the lack of normality of the data. For example, Fernandez et al. [P20] claimed that they used the Wilcoxon test to analyze each experiment individually as “...in most cases the data were not normal...”, while Cruz-Lemus et al. [P28] claimed that they used the Kruskall-Wallis test as “...Kruskal-Wallis is the most appropriate test... when there is non-normal distribution of the data...”.

Among those families relying on non-parametric tests to analyze individual experiments, 62% rely on the same test to analyze the family as a whole (and thus, use IPD mega-trial), regardless of the overall sample size achieved at the family level. For example, Hadar et al. [P33] used the Mann-Whitney test to analyze each individual experiment and then the family as a whole —despite having achieved a sample size of around 80 whenever pooling the raw-data together.

Even though such procedure seems consistent, this may not be optimal, as traditional statistical tests such as ANOVA are robust to departures from normality [53] (especially when sample sizes get larger, as what happens when pooling the raw-data of all experiments together [54]), and they should be preferred over their non-parametric counterparts when sample sizes get larger [55]. We suggest that this large reliance on IPD mega-trial in SE may be caused by the lack of normality of the data, the common use of non-parametric tests to analyze individual experiments, and the impossibility of accommodating more factors apart from “treatment” within traditionally used non-parametric tests (e.g., the U-Mann Whitney, the Wilcoxon, etc. [27]).

### 6 RQ4: FAMILIES LIMITATIONS

We found a series of common limitations with regard to joint data analysis in the families that we identified.

For example, there is an over-reliance on Narrative synthesis to provide joint results. Narrative synthesis has been discouraged in mature fields such as medicine or pharmacology due to its inability to provide a quantitative summary of results and its subjectivity when providing joint results [11], [21]. Apart from the above, and as we saw previously, Narrative synthesis fails to take into account the natural variation of results [21]. This issue may be specially relevant in SE, where small sample sizes are the norm rather than the exception [51], and thus, a large variability of results is expected [56]. As an example, and perhaps unknowingly, Narrative synthesis may have tricked Ceccato et al. [P10] into thinking that conflicting results materialized across two small experiments (with sample sizes of 13 each)
TABLE 7
Changes introduced within families (ordered by total number of changes).

<table>
<thead>
<tr>
<th>ID</th>
<th>Techniques</th>
<th>Changes</th>
<th>Response</th>
<th>Design</th>
<th>Individual</th>
</tr>
</thead>
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<tr>
<td>[P2]</td>
<td>N,-,-,-,-</td>
<td>O,P ,PR,E</td>
<td>?</td>
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<td>A</td>
</tr>
<tr>
<td>[P4]</td>
<td>N,-,-,-,-</td>
<td>O,P ,PR,E</td>
<td>✓</td>
<td>✓</td>
<td>C</td>
</tr>
<tr>
<td>[P5]</td>
<td>-,-,A,-,-</td>
<td>O,P ,PR,E</td>
<td>✓</td>
<td>✓</td>
<td>C</td>
</tr>
<tr>
<td>[P6]</td>
<td>-,-,A,-,-</td>
<td>O,P ,PR,E</td>
<td>?</td>
<td>✓</td>
<td>A</td>
</tr>
<tr>
<td>[P31]</td>
<td>-,-,-,-,S</td>
<td>O,P ,PR,E</td>
<td>✓</td>
<td>✓</td>
<td>N</td>
</tr>
<tr>
<td>[P36]</td>
<td>N,-,-,-,-</td>
<td>O,P ,PR,E</td>
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<td>✓</td>
<td>N</td>
</tr>
<tr>
<td>[P1]</td>
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<td>-,-,P,R,E</td>
<td>✓</td>
<td>✓</td>
<td>T</td>
</tr>
<tr>
<td>[P8]</td>
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<td>O,P ,PR,E</td>
<td>?</td>
<td>✓</td>
<td>N</td>
</tr>
<tr>
<td>[P18]</td>
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<td>-,-,P,R,E</td>
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<td>✓</td>
<td>N</td>
</tr>
<tr>
<td>[P29]</td>
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<td>O,P ,PR,-</td>
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<td>N</td>
</tr>
<tr>
<td>[P35]</td>
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<td>O,P ,PR,-</td>
<td>✓</td>
<td>✓</td>
<td>T</td>
</tr>
<tr>
<td>[P37]</td>
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<td>-,-,P,R,E</td>
<td>✓</td>
<td>✓</td>
<td>N</td>
</tr>
<tr>
<td>[P38]</td>
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<td>O,P ,PR,-</td>
<td>✓</td>
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<td>C</td>
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</tr>
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<td>C</td>
</tr>
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<td>T</td>
</tr>
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<td>[P30]</td>
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<td>-,-,P,E</td>
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<td>✓</td>
<td>A</td>
</tr>
<tr>
<td>[P34]</td>
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<td>-,-,P,R,E</td>
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<td>✓</td>
<td>N,T</td>
</tr>
<tr>
<td>[P21]</td>
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<td>✓</td>
<td>✓</td>
<td>A</td>
</tr>
<tr>
<td>[P39]</td>
<td>-,-,A,M,-</td>
<td>-,-,P,E</td>
<td>✓</td>
<td>✓</td>
<td>N,A</td>
</tr>
</tbody>
</table>

when they claimed that "...strangely enough, the trend observed... in Exp IV and V has alternating directions" or Runeson et al. [P36] when they claimed that "...the first replication was designed to be as exact as possible... Despite an attempt at an exact replication, the outcomes were not the same..." in two experiments with sample sizes 33 and 18, respectively. In particular, conflicting results (in either p-value terms or effect size terms) may materialize just because of the presence of small sample sizes, and thus, the large variation of results expected, and not because experiments observe different realities [50], [14].

Narrative synthesis has also been used to assess moderator effects in 15% of the families. Again, and despite its appeal, Narrative synthesis may be unreliable to detect moderators, specially when experiments are small. In particular, as a large variability of results is expected in small sample sizes [50], [14], there is a high risk of claiming that differences across experiments’ results are due to moderator effects —when in reality, differences across experiments’ results could have just emerged by natural variation of results. For example, in view that one experiment provided different results than the rest, Ali et al. [P37] claimed that "...One plausible explanation is that participants had more experience with standard UML state machines...". On its side, after noticing that different results were achieved across two experiments within the family, Juristo et al. [P2] claimed that "subjects might swap information about the programs and their faults at the end of each session. As a result of copying, the techniques applied... could be more effective at UdS and UPV than at other sites". Even though such claims may add to the discussion, they may also be misleading. Unfortunately, Narrative synthesis does not allow to distinguish how much variability in the results comes from natural variation and how much does not [50], [14]. This may impact the reliability of the conclusions reached within families using Narrative synthesis to elicit moderators.

With regard to the use of AD to provide joint results, we have noticed some inconsistencies in its use. For example, in some families non-parametric statistical tests (e.g., U-Mann Whitney [27]) were used to analyze individual experiments as data did not follow normality. Then, parametric effect sizes (such as Cohen’s d or Hedge’s g) were calculated for each experiment to integrate them with AD. As an example, Fernandez et al. [P39] analyzed each individual experiment by means of the U-Mann-Whitney (as data did not follow normality), and then computed the Hedge’s g of each experiment to provide a joint result by means of AD. Unfortunately, the use of parametric effect sizes (such as
Cohen’s d or Hedge’s g) also comes at the cost of checking the statistical assumptions on which they are built onto (e.g., normality and homogeneity of variances [39], [38], [57]). This becomes more relevant the smaller the sample sizes [38] as otherwise, there is a risk of providing biased results due to the a-priori unknown shape of the sampling distribution of each experiment’s effect size [39]. Thus, we suggest that if non-parametric tests are used to analyze individual experiments, at least for consistency’s sake, non-parametric effect sizes such as Cliff’s delta should be used to provide joint results with AD [39], [38], [57].

Also with regard to the use of AD, we have noticed that despite the multiple changes usually introduced across experiments within families (and thus, the potential heterogeneity of results inadvertently introduced within families), fixed-effects models are commonly preferred over random-effects models —perhaps because of their generally smaller p-values [21], [20], and in turn, their more “significant” results. For example, Scanniello et al. [P1] analyzed a group of five different replications with a fixed-effects meta-analysis model (despite obtaining a relatively large and statistically significant heterogeneity of results) and Cruz et al. [P6] analyzed a group of nine effect sizes with fixed-effects models despite the observable heterogeneity in the forest-plot. Unfortunately, not acknowledging heterogeneity of results during the statistical analysis may limit the reliability of joint results [21]. This may be worrying, specially if a large number of changes have been introduced across experiments.

With regard to the use of IPD mega-trial to analyze families, and as previously discussed in medicine [43], [42], IPD mega-trial may provide biased results if subjects resemble more to each other within experiments than across experiments (e.g., when some experiments are run with professionals and others with students), or if data are unbalanced across treatments and experiments (e.g., when some experiments are larger than others, and missing data materializes in some experiments but not in others). Given that missing-data is common in SE due to protocol deviators or drop-outs [58], that families commonly conduct experiments with professionals and students, and that experiments run with professionals tend to be smaller than those run with students, we are skeptical about the suitability of IPD mega-trial to analyze SE families.

IPD mega-trial has been also used to elicit moderators in 18% of the families [P10], [P11], [P28], [P26], [P33], [P30], [P15]. It is common in such families running experiments with different types of subjects, and then, using a certain "tag" to represent each type of subject as if it was the “Experiment” factor in an IPD stratified analysis. For example, experience (i.e., PhD, master, undergraduate) was used by Ricca et al. and Ceccato et al. [P26], [P14] to represent the “Experiment” factor in an IPD stratified model. In spite of its intuitiveness, such approach may be misleading: differences across experiments’ results may not come from sole moderators, specially because other unknown variables (e.g., age, motivation, skills, treatment conformance, the materialization of some threats to validity in some experiments and not in others, etc. [59]), or confounding factors (e.g., if more than one change were purposefully introduced simultaneously across the experiments) may be also behind differences of results [60], [61].

Finally, we would also like to comment on the ability of families to increase statistical power [3], and the extent to which this is dependent upon the “severity” of the changes introduced across the experiments within families. In particular, if a certain dimension—or dimensions—are changed across experiments, this may introduce heterogeneity of results [62]. Under such circumstance, random-effects models should be preferred over fixed-effects models [21], [20]. This may have a noticeable impact on statistical power (as random-effects models are known to be more conservative than their fixed-effects counterparts [12], [21], [63]). Thus, if changes are introduced across experiments, larger sample sizes, and a potentially larger number of experiments may be needed to reach to the same significance levels that would have been achieved with a fixed-effects model [21].

In turn, introducing many changes across experiments may be detrimental towards families’ statistical power.

### 7 Good Practices Analyzing Families

We have elaborated a preliminary list of recommendations to analyze families after the common limitations that we observed with regard to joint data analysis. These recommendations follow:

- **Avoid Narrative synthesis if possible.** Despite its appealing, the application of Narrative synthesis is dangerous given current sample size limitations in SE experiments —and thus, the large variability of results expected. In addition, Narrative synthesis just provides a textual summary of results instead of quantitative summary (such as a p-value or effect size). Thus, the application of Narrative synthesis to aggregate experiments’ results goes against the best practices of SE experimentation [17], [64], [65], [66], [7], where p-values and effect sizes are encouraged to be reported to summarize results.

- **Avoid IPD mega-trial if possible.** Even though intuitive, IPD mega-trial fails to account for heterogeneity of results across experiments. Unfortunately, heterogeneity may materialize if changes are introduced deliberately —or inadvertently— across experiments. IPD mega-trial also fails to account for the plausible correlation of participants’ scores within experiments (as subjects may resemble more to each other within experiments than across experiments) and the existence of experiments with different sample sizes and missing-data [43], [42].

- **Avoid Aggregation of p-values if possible.** Mainly because with its use each experiment contributes identically to the overall conclusion independently of its quality, effect size or sample size, and because it does not provide any effect size, and thus, hinders the assessment of the relevance of results (e.g., how large is the joint effect? [21], [20]).

- **When data do not follow normality.** The robustness of traditional parametric statistical tests such as ANOVA or the t-test to departures from normality has been assessed over and over again even in smaller sample sizes than those typical in SE
experiments [67], [53], [55], [68], [69]. The robustness of traditionally used parametric statistical tests to departures from normality is even greater with sample sizes in the hundreds [54]—as those resulting when pooling together the raw-data of all the experiments within families. The superiority of parametric statistical tests over non-parametric tests such as the U-Mann Whitney or Wilcoxon has been widely acknowledged [70], [67], [53], specially with regard to their interpretability of results (as results can be provided in natural units—oneg., differences between means—instead of differences between mean ranks) and statistical flexibility (e.g., as multiple factors such as type of subject, experiment, etc. can be included). Even though we concede that defenders of both sides (i.e., parametric vs. non-parametric) can be found scattered along the literature [71], [72], [70], [67], [53], [55], [68], [69], we think that a good compromise is that followed by some families’ authors (e.g., Laitenberger et al. [P22] or Pfahl et al. [P24]). In particular, in view that the Wilcoxon signed rank test and the dependent t-test provided similar results, Laitenberger et al. [P22] used the results of the t-test. If in spite of the robustness of parametric statistical tests to departures from normality it is still wanted to proceed with non-parametric tests, we recommend to use one of the following approaches to aggregate results:

- **AD.** Use either (1) non-parametric effect sizes (e.g., Cliff’s delta or Probability of Superiority, etc. [39]) or (2) bootstrap to elicit the standard error of the parametric effect size selected (e.g., Cohen’s d or Hedge’s g) [73].
- **IPD stratified.** Use either (1) a permutation test (by following a similar approach to that followed by Ricca et al. [P16]); (2) a Generalized Linear Model to accommodate the distribution of the data (e.g., by means of logistic regressions [74], [75]); (3) use bootstrap [76], [77].

- **Check AD and IPD statistical assumptions.** If sample sizes are small and data are not normal or have different variances, parametric effect sizes (such as Cohen’s d or Hedge’s g [21]) may be unreliable [39], [38], [57]. Similarly, if an IPD stratified statistical model is used (e.g., ANOVA), check its assumptions (e.g., normality and equality of variances) or consult specialized literature on the topic to investigate about their robustness to departures from statistical assumptions [72], [70], [53], [55], [68], [69].

- **Acknowledge heterogeneity of results** when providing joint results. If changes are introduced across experiments (e.g., different populations, experimental designs, etc.), such changes may impact the effect size being estimated in each experiment [21]. As others did before, we recommend to apply by default random-effects models over fixed-effects models as the prior reduce to the later if no heterogeneity of results has materialized [21].

- **Plan ahead the analysis procedure to follow.** We encourage researchers conducting families to plan ahead at least the pre-processing steps that are going to be undertaken (e.g., which procedure is going to be followed to remove outliers and graph data?), the statistical tests that are going to be used (e.g., are researchers interested in differences between means (and thus parametric tests?), and the aggregation techniques to be used (e.g., are researchers interested in providing intuitive visualizations of results such as with AD? are researchers interested in evaluating results in natural units, such as with IPD?). If the application of such procedures, tests or aggregation techniques was unfeasible after conducting the experiments within the family (e.g., due to unexpected data-losses, experimental restrictions that forced design changes, etc.), such rationale should be discussed before providing joint results or eliciting moderators.

### 8 Good Practices Reporting Families

While conducting this SMS we found that assessing the appropriateness of the aggregation technique/s used within families was not straightforward. This was in part because the articles missed some relevant information (e.g., are the raw-data of all the experiments available?, are the response variables’ operationalizations and scales identical across the experiments?), and in part because the raw-data of the families were not made public—and thus, re-analyzing the family with all the techniques to check the suitability of the technique/s used was unfeasible. In view of this, we have extracted a series of elements that we think are relevant for assessing the reliability of results and the suitability of the aggregation technique/s applied. We suggest to report at least the following elements in research articles reporting families:

- **Raw-data availability.** Report whether the raw-data are available at the time of analyzing the family. If the raw-data are available, techniques such as IPD stratified or AD may be preferred over the other techniques to provide joint results or elicit moderators.

- **Response variable changes.** Report whether the same response variable operationalization is used across experiments, as if this is the case, there is no need to compute standardized effect sizes (e.g., Cohen’s d) to conduct AD. In this situation, unstandardized units can be used instead to increase the interpretability of results with AD [21], [40]. IPD stratified can be safely used either [44].

- **Experiments’ sample sizes.** Report the number of subjects that participated in each experiment, since this information is useful for computing various effect sizes [21], and arguing about the generalizability of results.

- **The relationship between the participants across experiments.** Report if different subjects participated across the experiments, as otherwise, if they are the same, and this was not accounted for by the aggregation technique used, joint results may be misleading.

- **The technique/s used to analyze the family.** Motivate the selection of the aggregation technique/s
used, and why such technique/s were selected instead of others given the characteristics of the family.

- **The elements that changed across experiments.** Make explicit the changes introduced across the experiments, so it is possible assessing the suitability of the aggregation technique/s applied.

Finally, we have observed that the raw-data (i.e., a spreadsheet with the response variables and the assignment of subjects to treatments across the experiments) of the families were not accessible in most families of experiments—despite that 6 out of 39 families claimed to have published them [P14], [P35][P8], [P17], [P19], [P1]. This precludes re-analysis with other—perhaps more suitable—analysis techniques to double-check the robustness of results to different aggregation techniques, and eventually, hinders the reproducibility of results. Thus, if possible, we encourage researchers reporting families to make their raw-data available.

### 9 Threats to Validity

In this section we discuss the main threats to validity of our SMS according to Petersen et al.’s guidelines [15].

When conducting a secondary study, the search terms should identify as many relevant papers as possible to provide an accurate overview of the topic and its structure [15]. We piloted different terms and search strings along the way to reduce the risk of missing relevant primary studies. Due to the inconsistency in the terms used to refer to families of experiments in SE, we used synonyms of the term obtained from a reference set of five articles [P38], [P14], [P8], [P2], [P36]. This helped us to broaden the results of our SMS and increase the reliability of the findings.

We had to trade off the complexity of the search string (in order not to be too restrictive) against the looseness of the terms (due to the acute reduction in accuracy of the search). In particular, the words “experiment” and “aggregation”, “group of studies” or “series of experiments” appeared in many different disciplines unrelated to the scope of our research, which added a large amount of noise to our results. In turn, we had no option but restrict the search space to relevant venues on SE experimentation. Still, we do not think this had a major impact on results, as the techniques that we found in our primary studies were similar to those used in other disciplines such as medicine or pharmacology [20], [21], [62].

In order to increase the precision of the results, we confined the search space to the venues surveyed in a well-known secondary study on SE experiments [78]. We acknowledge the possibility of publication bias on results (as we restricted our search to well-known venues for publishing empirical research). Even though this might have conditioned our results, we complemented the search with a backward snowballing process [17].

After identifying relevant articles, the selection of primary studies within the scope of research is crucial for achieving relevant conclusions. The protocol included the definition of explicit exclusion criteria to minimize subjectivity and prevent the omission of valid articles. Exclusion criteria were applied by two researchers in order to select valid primary studies. In the event of disagreement, a third researcher helped with the inclusion or exclusion of the article.

We acknowledge that other researchers may have gathered a different list of references for portraying the advantages and disadvantages of the aggregation techniques that we identified. Unfortunately, it was unfeasible for us to gather references systematically due the enormous list of references prompted in online databases with the terms “aggregation”, “experiments”, “data” or “effect sizes”. However, with the aim of minimizing this shortcoming we tried to recur to well-known references in mature experimental disciplines such as medicine and pharmacology [62], [79], seminal works on vote-counting and narrative synthesis [80], [81], and meta-analysis and reproducibility of results [21], [56], [14] to make our findings representative of the current state of knowledge.

Even though we used the same naming conventions used in medicine to categorize the aggregation techniques used in SE (e.g., AD, IPD, etc.), this does not imply that those techniques were just applied in medicine: the same aggregation techniques—albeit with different names—have been also applied in other disciplines such as econometrics, ecology, biology, or the social sciences, just to name a few [21], [20], [82]. Instead, in this article we just recurred to the naming conventions used in medicine as a way of categorizing the techniques applied in SE into broad groups, and as SE experimental research has previously imported from medicine much of the data analysis procedures used to analyze individual experiments [83], [64], and the research methods followed to come up with empirical evidence (e.g., the procedures for conducting SLRs [7] or Evidence Based Software Engineering [66] among others).

Finally, in only 7% of the identified families of experiments the raw-data were accessible. This hindered re-analysis, and thus, a formal assessment on the suitability of the techniques applied to analyze both individual experiments and the families as whole. As a result, providing fine tailored recommendations to each family on the suitability of the techniques applied was unfeasible.

### 10 Conclusion

Families of experiments (i.e., groups of interrelated experiments with the same goal [1]) are on the rise in SE. Characteristics, implications and particularities of families over other study types (such as groups of experiments gathered by means of SLRs) are to be defined yet in SE. Fine-tuning the term family of experiments may help SE researchers to apply consistent techniques to analyze them.

We define a family of experiments as a group of replications where access to the raw-data is guaranteed, the settings of the experiments are known by researchers, and at least three experiments are conducted to assess the performance of at least two different technologies on the same response variable. Several techniques have been used to aggregate experiments’ results within families in SE: Narrative synthesis, AD, IPD mega-trial, IPD stratified and Aggregation of $p$-values. The rationale to select aggregation techniques within families is rarely discussed in research articles. This may impact the reliability of joint results and undermine their potential to elicit moderators.
46% of the families used Narrative synthesis to provide joint conclusions or study moderators. SE experiments’ small sample sizes may impact the reliability of such families’ results. 38% of the families used AD. Some of the families applying AD resorted to parametric effect sizes (e.g., Cohen’s d or Hedge’s g) despite acknowledging small sample sizes and that data did not follow normality. This may have impacted the reliability of such families’ findings. 33% of the identified families used IPD mega-trial. Data unbalance, and the multiple changes commonly introduced across experiments within families may have lead to unreliable results. 15% of the families used IPD stratified to aggregate experimental results following similar procedures to those followed in medicine [20]. Finally, Aggregation of p-values was used in just 7% of the families. Aggregation of p-values weights identically each experiment towards the joint result and does not provide a joint effect size. This may limit the interpretability of results in such families.

The aggregation technique/s used within families may impact the reliability of joint results. Transparent and reliable aggregation techniques such as AD or IPD stratified seem suitable to analyze SE families. However, the reliability of AD and IPD stratified comes at a cost: their statistical assumptions need to be checked before interpreting results. We recommend to minimize the use of Narrative synthesis as it does not provide a quantitative summary of results, involves subjective judgment, and does not take advantage of the raw-data when providing joint results or eliciting moderators. We recommend to minimize the use of Aggregation of p-values as it does not provide any way of assessing the relevance of results, and in its basic form, weights identically each experiment towards the joint conclusion—regardless of their effect sizes, sample sizes, quality or experimental designs. IPD mega-trial should be avoided as it may provide biased results if data is unbalanced across or within experiments or if subjects resemble more to each other within-experiments than across experiments.

Finally, increasing numbers of experiments are being included within families (an average of five per family). This could lead SE to a next stage of maturity. However, reporting deficiencies and the blind application of unsuitable aggregation techniques could limit the reliability of joint results. Researchers should assess the suitability of the aggregation techniques used, and provide a rationale on why such techniques were used to analyze their respective families. Finally, we urge researchers conducting families of experiments in SE to plan ahead their data analyses, and improve reporting transparency with respect to data, statistical assumptions and data analysis techniques.

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PRIMARY STUDIES


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