Joint Client Scheduling and Resource Allocation under Channel Uncertainty in Federated Learning

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Abstract—The performance of federated learning (FL) over wireless networks depend on the reliability of the client-server connectivity and clients’ local computation capabilities. In this article we investigate the problem of client scheduling and resource block (RB) allocation to enhance the performance of model training using FL, over a pre-defined training duration under imperfect channel state information (CSI) and limited local computing resources. First, we analytically derive the gap between the training losses of FL with clients scheduling and a centralized training method for a given training duration. Then, we formulate the gap of the training loss minimization over client scheduling and RB allocation as a stochastic optimization problem and solve it using Lyapunov optimization. A Gaussian process regression-based channel prediction method is leveraged to learn and track the wireless channel, in which, the clients’ CSI predictions and computing power are incorporated into the scheduling decision. Using an extensive set of simulations, we validate the robustness of the proposed method under both perfect and imperfect CSI over an array of diverse data distributions. Results show that the proposed method reduces the gap of the training accuracy loss by up to 40.7 % compared to state-of-the-art client scheduling and RB allocation methods.

Index Terms—Federated learning, channel prediction, Gaussian process regression (GPR), resource allocation, scheduling, 5G and beyond

I. INTRODUCTION

The staggering growth of data generated at the edge of wireless networks sparked a huge interest in machine learning (ML) at the network edge, coined *edge ML* [3]. In edge ML, training data is unevenly distributed over a large number of devices, and every device has a tiny fraction of the data. One of the most popular model training methods in edge ML is *federated learning (FL)* [4], [5]. The goal of FL is to train a high-quality centralized model in a decentralized manner, based on local model training and client-server communication while training data remains private [3], [4], [6]. Recently, FL over wireless networks gained much attention in communication and networking with applications spanning a wide range of domains and verticals ranging from vehicular communication to ,blockchain and healthcare [5]–[7]. The performance of FL highly depends on the communication and link connectivity in addition to the model size and the number of clients engaged in training. The quality of the trained model (inference accuracy)

also depends on the training data distributions over devices which generally is non-independent and identically distributed (IID) [8], [9]. Hence, the impact of training data distribution in terms of balanced-unbalancedness and IID versus non-IIDness on model training is analyzed in few works [5], [10], [11]. In [10], the authors have analyzed the effect of non-IID data distribution through numerical simulations for a visual classification task. Likewise in [11], authors have empirically analyzed the impact of non-IID data distribution on the performance of FL.

Except a handful of works [4], [12]–[17], the vast majority of the existing literature assumes ideal client-server communication conditions, overlooking channel dynamics and uncertainties. In [12], communication overhead is reduced by using the *lazily aggregate gradients (LAG)* based on reusing outdated gradient updates. Due to the limitations in communication resources, scheduling the most informative clients is one possible solution [13], [14], [17]. In [13] authors propose a client-scheduling algorithm for FL to maximize the number of scheduled clients assuming that communication and computation delays are less than a predefined threshold but, the impact of client scheduling was not studied. In [14], the authors study the impact of conventional scheduling policies (e.g., random, round robin, and proportional fairness) on the accuracy of FL over wireless networks relying on known channel statistics. In [15], the training loss of FL is minimized by joint power allocation and client scheduling. A probabilistic scheduling framework is proposed in [18], seeking the optimal trade-off between channel quality and importance of model update considering the impact of channel uncertainty in scheduling. Moreover, the impact of dynamic channel conditions on FL is analyzed only in few works [4], [14], [19]. In [4], authors propose over-the-air computation-based approach leveraging the ideas of [20] to speed-up the global model aggregation utilizing the superposition property of a wireless multiple-access channels with scheduling and beamforming. In addition to channel prediction, clients’ computing power are utilized for their local models updates. Stochastic gradient decent (SGD) is widely used for updating their local models, in which the computation is executed sample by sample [21]. In [19], the authors proposed the compressed analog distributed stochastic gradient descent (CA-DSGD) method, which is shown to be robust against imperfect channel state information (CSI) at the devices. While interestingly the communication aspects in FL such as optimal client scheduling and resource allocation in the absence of perfect CSI along with the limitations in processing

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power for SGD-based local computations are neglected in all these aforementioned works.

Acquiring CSI through pilot sequence exchanges introduces an additional signaling overhead that scales with the number of devices. There are a handful of works dealing with wireless channel uncertainties [22], [23]. Authors in [22] demonstrated the importance of reliable fading prediction for adaptive transmission in wireless communication systems. Channel prediction via fully connected recurrent neural networks are proposed in [23]. Among channel prediction methods, Gaussian process regression (GPR) is a light weight online technique where the objective is to approximate a function with a non-parametric Bayesian approach under the presence of nonlinear and unknown relationships between variables [24], [25]. A Gaussian process (GP) is a stochastic process with a collection of random variables indexed by time or space. Any subset of these random variables forms multidimensional joint Gaussian distributions, in which GP can be completely described by their mean and covariance matrices. The foundation of the GPR-approach is Bayesian inference, where a priori model is chosen and updated with observed experimental data [24]. In the literature, GPR is used for a wide array of practical applications including communication systems [26]–[28]. In [26] GPR is used to estimate Rayleigh channel. In [27], a problem of localization in a cellular network is investigated with GPR-based position predictions. In [28], GPR is used to predict the channel quality index (CQI) to reduce CQI signaling overhead. In our prior works, [1], [2], GPR-based channel prediction is used to derive a client scheduling and resource block (RB) allocation policy under imperfect channel conditions assuming unlimited computational power availability per client. Investigating the performance of FL under clients' limited computation power under both IID and non-IID data distributions remains an unsolved problem.

The main contributions of this work over [1], [2] are the derivation of a joint client scheduling and RB allocation policy for FL under communication and computation power limitations and a comprehensive analysis of the performance of model training as a function of (i) system model parameters, (ii) available computation and communication resources, (iii) non-IID data distribution over the clients in terms of the heterogeneity of dataset sizes and available classes. In this work, we consider a set of clients that communicate with a server over wireless links to train a neural network (NN) model within a predefined training duration. First, we derive an analytical expression for the loss of accuracy in FL with scheduling compared to a centralized training method. In order to reduce the signaling overhead in pilot transmission for channel estimation, we consider the communication scenario with imperfect CSI and we leverage GPR to learn and track the wireless channel while quantifying the information on the unexplored CSI over the network. To do so, we formulate the client scheduling and RB allocation problem as a trade-off between optimal client scheduling, RB allocation, and CSI exploration under both communication and computation resource constraints. Due to the stochastic nature of the aforementioned problem, we resort to the dual-plus-penalty (DPP) technique from the Lyapunov optimization framework to recast

the problem into a set of linear problems that are solved at each time slot [29]. In this view, we present the joint client scheduling and RB allocation algorithm that simultaneously explore and predict CSI to improve the accuracy of FL over wireless links. With an extensive set of simulations we validate the proposed methods over an array of IID and non-IID data distributions capturing the heterogeneity in dataset sizes and available classes. In addition, we compare the feasibility of the proposed methods in terms of fairness of the trained global model and accuracy. Simulation results show that the proposed method achieves up to 40.7% reduction in the loss of accuracy compared to the state-of-the-art client scheduling and RB allocation methods.

The rest of this paper is structured as follows. Section II presents the system model and formulates the problem of model training over wireless links under imperfect CSI. In Section III, the problem is first recast in terms of the loss of accuracy due to client scheduling compared to a centralized training method. Subsequently, GPR-based CSI prediction is proposed followed by the derivation of Lyapunov optimization-based client scheduling and RB allocation policies under both perfect and imperfect CSI. Section IV numerically evaluates the proposed scheduling policies over state-of-the-art client scheduling techniques. Finally, conclusions are drawn in Section V.

II. SYSTEM MODEL AND PROBLEM FORMULATION

Consider a system consisting of a set $\mathcal{K}$ of K clients that communicate with a parameter server (PS) over wireless links. Therein, the k -th client has a private dataset $\mathcal{D}_k$ of size D_k , which is a partition of the global dataset $\mathcal{D}$ of size $D = \sum_k D_k$. For communication with the server for local model updating, a set $\mathcal{B}$ of $B(\leq K)$ RBs is shared among those clients¹.

A. Scheduling, resource block allocation, and channel estimation

Let $s_k(t) \in \{0, 1\}$ be an indicator where $s_k(t) = 1$ indicates that the client k is scheduled by the PS for uplink communication at time t and $s_k(t) = 0$, otherwise. Multiple clients are simultaneously scheduled by allocating each at most with one RB. Hence, we define the RB allocation vector $\lambda_k(t) = [\lambda_{k,b}(t)]_{\forall b \in \mathcal{B}}$ for client k with $\lambda_{k,b}(t) = 1$ when RB b is allocated to client k at time t , and $\lambda_{k,b}(t) = 0$, otherwise. The client scheduling and RB allocation are constrained as follows:

$$s_k(t) \leq \mathbf{1}^\dagger \lambda_k(t) \leq 1 \quad \forall k, t, \quad (1)$$

where $\mathbf{1}^\dagger$ is the transpose of the all-one vector. The rate at which the k -th client communicates in the uplink with the PS at time t is given by,

$$r_k(t) = \sum_{b \in \mathcal{B}} \lambda_{k,b}(t) \log_2 \left(1 + \frac{p|h_{k,b}(t)|^2}{I_{k,b}(t) + N_0} \right), \quad (2)$$

where p is a fixed transmit power of client k , $h_{k,b}(t)$ is the channel between client k and the PS over RB b at time t ,

¹For $B > K$, all clients simultaneously communicate their local models to the PS.

$I_{k,b}(t)$ represents the uplink interference on client k imposed by other clients over RB b , and N_0 is the noise power spectral density. Note that, a successful communication between a scheduled client and the server within a channel coherence time is defined by satisfying a target minimum rate. In this regard, a rate constraint is imposed on the RB allocation in terms of a target signal to interference plus noise ratio (SINR) γ_0 as follows:

$$\lambda_{k,b}(t) \leq \mathbb{I}(\hat{\gamma}_{k,b}(t) \geq \gamma_0) \quad \forall k, b, t, \quad (3)$$

where $\hat{\gamma}_{k,b}(t) = \frac{p|h_{k,b}(t)|^2}{I_{k,b}(t) + N_0}$ and the indicator $\mathbb{I}(\hat{\gamma} \geq \gamma_0) = 1$ only if $\hat{\gamma} \geq \gamma_0$.

B. Computational power consumption and computational time

Most of the clients in wireless systems are mobile devices operated by power-limited energy sources, with limited computational capabilities. As demonstrated in [30] the dynamic power consumption P_c of a processor with clock frequency of ω is proportional to the product of $V^2\omega$. Here, V is the supply voltage of the computing, which is approximately linearly proportional to ω [31]. Motivated by [30] and [31], in this work, we adopt the model $P_c \propto \omega^3$ to capture the computational power consumption per client. Due to the concurrent tasks handled by the clients in addition to local model training, the dynamics of the available computing power P_c at a client is modeled as a Poisson arrival process [32]. Therefore, we assume that the computing power $P_c^k(t)$ of client k at time t follows an independent and identically distributed exponential distribution with mean μ_c . As a result, the minimum computational time required for client k is given by,

$$\tau_{c,k}(t) = \frac{\mu_c D_k M_k}{\sqrt[3]{P_c^k(t)/b}}, \quad (4)$$

where M_k is the number of SGD iterations computed over D_k . The constants μ_c and b are the number of clock cycles required to process a single sample and power utilized per number of computation cycles, respectively. To avoid unnecessary delays in the overall training that are caused by clients' local computations, we impose a constraint on the computational time, with threshold τ_0 over the scheduled clients as follows:

$$s_k(t) \leq \mathbb{I}(\tau_{\min,k}(t) \leq \tau_0) \quad \forall k, t. \quad (5)$$

C. Model training using FL

The goal in FL is to minimize a regularized loss function $F(\mathbf{w}, \mathcal{D}) = \frac{1}{D} \sum_{\mathbf{x}_i \in \mathcal{D}} f(\mathbf{x}_i^\dagger \mathbf{w}) + \xi \varrho(\mathbf{w})$, which is parametrized by a weight vector $\mathbf{w}$ (referred as the *model*) over the global dataset within a predefined communication duration T . Here, $f(\cdot)$ captures a loss of either regression or classification task, $\varrho(\cdot)$ is a regularization function such as Tikhonov, $\mathbf{x}_i$ is the input vector, and $\xi(> 0)$ is the regularization coefficient. It is assumed that, clients do not share their data and instead, compute their models over the local datasets.

For distributed model training in FL, clients share their local models that are computed by solving $F(\mathbf{w}, \mathcal{D})$ over their local

Fig. 1: FL with client scheduling under limited wireless resources and imperfect CSI.

datasets using SGD using the PS, which in return does model averaging and shares the global model with all the clients.

Under imperfect CSI, prior to transmission the channels need to be estimated via sampling. Instead of performing channel measurements beforehand the inferred channels between clients and the PS over each RB are as $\hat{h}(t) = J(t, \{\tau, h(\tau)\}_{\tau \in \mathcal{N}(t)})$ using past N channel observations. Under channel prediction, $h_{k,b}(t) = \hat{h}_{k,b}(t)$ is used as signal to interference plus noise ratio (SINR) in (2) and (3). The choice of small N ensures low computation complexity of the inference task. Here, the set $\mathcal{N}(t)$ consists of N most recent time instances satisfying $s(\tau) = 1$ and $\tau < t$. With $\lambda_{k,b}(t) = 1$, the channel $h_{k,b}(t)$ is sampled and used as an observation for the future, i.e., the RB allocation and channel sampling are carried out simultaneously. In this regard, we define the information on the channel between client k and the server at time t as $\mathbf{j}_k(t) = [j_{k,b}(t)]_{b \in \mathcal{B}}$. For accurate CSI predictions, it is essential to acquire as much information about the CSI over the network [33]. This is done by exploring new information by maximizing $\sum_k \mathbf{j}_k^\dagger(t) \lambda_k(t)$ at each time t while minimizing the loss $F(\mathbf{w}, \mathcal{D})$. Therefore, the empirical loss minimization problem over the training duration is formally defined as follows:

$$\underset{\mathbf{w}(t), \mathbf{s}(t), \mathbf{\Lambda}(t), \forall t}{\text{minimize}} \quad F(\mathbf{w}(T), \mathcal{D}) - \frac{\varphi}{T} \sum_{k,t} \mathbf{j}_k^\dagger(t) \lambda_k(t), \quad (6a)$$

$$\text{subject to} \quad (1)-(3), (5), \quad (6b)$$

$$\mathbf{A} \mathbf{\Lambda}^\dagger(t) \preceq \mathbf{1} \quad \forall t, \quad (6c)$$

$$\mathbf{1}^\dagger \mathbf{s}(t) \leq B \quad \forall t, \quad (6d)$$

$$\mathbf{s}(t) \in \{0, 1\}^K, \lambda_k(t) \in \{0, 1\}^B \quad \forall t, \quad (6e)$$

$$\mathbf{w}_k(t) = \underset{\mathbf{w}'}{\text{argmin}} F(\mathbf{w}' | \mathbf{w}(t-1), \mathcal{D}_k) \quad \forall k, t \quad (6f)$$

$$\mathbf{w}(t) = \sum_k \frac{D_k}{D} s_k(t) \mathbf{w}_k(t) \quad \forall t, \quad (6g)$$

where $\mathbf{\Lambda}^\dagger(t) = [\lambda_k^\dagger(t)]_{k \in \mathcal{K}}$, $\varphi(> 0)$ controls the impact of the CSI exploration, and $\mathbf{A}$ is a $B \times K$ all-one matrix. The orthogonal channel allocation in (6c) ensures collision-free client uplink transmission with $I_{k,b}(t) = 0$ and constraint (6d) defines the maximum allowable clients to be scheduled. The SGD based local model calculation at client k is defined in

(6f). The choice of SINR target γ_0 in (3) ensures that local models are uploaded within a single coherence time interval².

III. OPTIMAL CLIENT-SCHEDULING AND RB ALLOCATION POLICY VIA LYAPUNOV OPTIMIZATION

The optimization problem (6) is coupled over all clients hence, in what follows, we elaborate on the decoupling of (6) over clients and the server, and derive the optimal client scheduling and RB allocation policy.

A. Decoupling loss function of (6) via dual formulation

Let us consider an ideal unconstrained scenario where the server gathers all the data samples and trains a global model in a *centralized* manner. Let $F_0 = \min_{\mathbf{w}} F(\mathbf{w}, \mathcal{D})$ be the minimum loss under centralized training. By the end of the training duration T , we define the gap between the proposed FL under communication constraints and centralized training as $\varepsilon(T) = F(\mathbf{w}(T), \mathcal{D}) - F_0$. In other words, $\varepsilon(T)$ is the accuracy loss of FL with scheduling compared to centralized training. Since F_0 is independent of the optimization variables in (6a), replacing $F(\mathbf{w}, \mathcal{D})$ by $\varepsilon(T)$ does not affect optimality under the same set of constraints.

To analyse the loss of FL with scheduling, we consider the dual function of (6a) with the dual variable $\boldsymbol{\theta} = [\theta_1, \dots, \theta_D]$, $\mathbf{X} = [\mathbf{X}_k]_{k \in \mathcal{K}}$ with $\mathbf{X}_k = [\mathbf{x}_i]_{i=1}^{D_k}$, and $\mathbf{z} = \mathbf{X}^T \mathbf{w}$ as follows:

$$\psi(\boldsymbol{\theta}) = \min_{\mathbf{w}, \mathbf{z}} \left(\sum_{\mathbf{x}_i \in \mathcal{D}} \frac{1}{D} f_i(\mathbf{x}_i^T \mathbf{w}) + \xi \varrho(\mathbf{w}) + \frac{\boldsymbol{\theta}^T (\mathbf{z} - \mathbf{X}^T \mathbf{w})}{D} \right) \quad (7a)$$

$$\stackrel{a}{=} \frac{1}{D} \inf_{\mathbf{w}} \{ D \xi \varrho(\mathbf{w}) - \boldsymbol{\theta}^T \mathbf{X}^T \mathbf{w} \} + \sum_{i=1}^D \inf_{z_i} \{ -\theta_i z_i - f_i(z_i) \} \quad (7b)$$

$$\stackrel{b}{=} \xi \sup_{\mathbf{w}} \{ \mathbf{w}^T \mathbf{v} - \varrho(\mathbf{w}) \} + \sum_{k=1}^K \sum_{i=1}^{D_k} \sup_{z_i} \{ f_i(z_i) + \theta_i z_i \} \quad (7c)$$

$$\stackrel{c}{=} - \underbrace{\sum_{k=1}^K \sum_{i=1}^{D_k} \frac{1}{D} f_i^*(-\theta_i)}_{\#1} - \underbrace{\xi \varrho^*(\mathbf{v})}_{\#2}. \quad (7d)$$

Here, step (a) rearranges the terms, (b) converts the infimum operations to supremum while substituting $\mathbf{v} = \mathbf{X}\boldsymbol{\theta}/\xi D$, and (c) uses the definition of conjugate function $f_i^*(-\theta_i) = \inf_{z_i} \{ -\theta_i z_i - f_i(z_i) \}$ and $\varrho^*(\mathbf{v}) = \sup_{\mathbf{w}} \{ \mathbf{w}^T \mathbf{v} - \varrho(\mathbf{w}) \}$ [34]. With the dual formulation, the relation between the primal and dual variables is $\mathbf{w} = \nabla \varrho^*(\mathbf{v})$ [14]. Based on the dual formulation, the loss FL with scheduling is $\varepsilon(T) = \psi_0 - \psi(\boldsymbol{\theta}(T))$ where ψ_0 is the maximum dual function value obtained from the centralized method.

Note that the first term of (7d) decouples per client and thus, can be computed locally. In contrast, the second term in (7d) cannot be decoupled per client. To compute $\varrho^*(\mathbf{v})$, first, each client k locally computes $\Delta \mathbf{v}_k(t) = \frac{1}{\xi D} \mathbf{X}_k \Delta \boldsymbol{\theta}_k(t)$ at

time t . Here, $\Delta \boldsymbol{\theta}_k(t)$ is the change in the dual variable $\boldsymbol{\theta}_k(t)$ for client k at time t given as below,

$$\Delta \boldsymbol{\theta}_k(t) \approx \operatorname{argmax}_{\boldsymbol{\delta} \in \mathbb{R}^{D_k}} \left(-\frac{1}{D} \mathbf{1}^\dagger [f_i^*(-\boldsymbol{\theta}_k(t) - \boldsymbol{\delta})]_{i=1}^{D_k} - \frac{\xi}{K} \varrho^*(\mathbf{v}(t)) - \frac{1}{D} \boldsymbol{\delta}^\dagger \mathbf{X}_k \varrho^*(\mathbf{v}(t)) - \frac{\eta/\xi}{2D^2} \|\mathbf{X}_k \boldsymbol{\delta}\|^2 \right), \quad (8)$$

where η depends on the partitioning of $\mathcal{D}$ [35]. It is worth noting that $\Delta \boldsymbol{\theta}_k(t)$ in (8) is computed based on the previous global value $\mathbf{v}(t)$ received by the server. Then, the scheduled clients upload $\Delta \mathbf{v}_k(t)$ to the server. Following the dual formulation, the model aggregation and update in (6g) at the server is modified as follows:

$$\mathbf{v}(t+1) := \mathbf{v}(t) + \sum_{k \in \mathcal{K}} s_k(t) \Delta \mathbf{v}_k(t). \quad (9)$$

Using (9), the server computes the coupled term $\varrho^*(\mathbf{v}(t+1))$ in (7d).

It is worth noting that from the t -th update, $\Delta \boldsymbol{\theta}_k(t)$ in (8) maximizes $\Delta \psi(\boldsymbol{\theta}_k(t))$, which is the change in the dual function $\psi(\boldsymbol{\theta}(t))$ corresponding to client k . Let $\boldsymbol{\theta}_k^*(t)$ be the local optimal dual variable at time t , in which $\Delta \psi(\boldsymbol{\theta}_k^*(t)) \geq \Delta \psi(\boldsymbol{\theta}_k(t))$ is held. Then for a given accuracy $\beta_k(t) \in (0, 1)$ of local SGD updates, the following condition is satisfied:

$$\frac{\Delta \psi_k(\boldsymbol{\theta}_k^*(t)) - \Delta \psi_k(\boldsymbol{\theta}_k(t))}{\Delta \psi_k(\boldsymbol{\theta}_k(t)) - \Delta \psi_k(0)} \leq \beta_k(t), \quad (10)$$

where $\Delta \psi_k(0)$ is the change in ψ with a null update from the k -th client. For simplicity, we assume that $\beta_{k,t} = \beta$ for all $k \in \mathcal{K}$ and t , hereinafter. With (10), the gap between FL with scheduling and the centralized method is bounded as shown in Theorem 1:

Theorem 1. *The upper bound of $\varepsilon(T)$ after T communication rounds is given by,*

$$\varepsilon(T) \leq D \left(1 - (1 - \beta) \sum_{t \leq T} \sum_{k \leq K} \frac{D_k}{TD} s_k(t) \right)^T.$$

Proof: See Appendix A. ■

This yields that the minimization of $\varepsilon(T)$ can be achieved by minimizing its upper bound defined in Theorem 1. Henceforth, the equivalent form of (6) is given as follows:

$$\begin{aligned} & \underset{[\Delta \boldsymbol{\theta}_k(t)]_k, \mathbf{s}(t), \boldsymbol{\Lambda}(t), \forall t}{\text{minimize}} \quad D \left(1 - (1 - \beta) \sum_{t,k} \frac{D_k}{TD} s_k(t) \right)^T \\ & \quad - \frac{\varphi}{T} \sum_{k,t} \mathbf{j}_k^\dagger(t) \boldsymbol{\Lambda}_k(t), \end{aligned} \quad (11a)$$

$$\text{subject to} \quad (6b)-(6e), (8), (9). \quad (11b)$$

B. GPR-based information metric $J(\cdot)$ for unexplored CSI

For CSI prediction, we use GPR with a Gaussian kernel function to estimate the nonlinear relation of $J(\cdot)$ with a GP prior. For a finite data set $\{t_n, h(t_n)\}_{n \in \mathcal{N}}$, the aforementioned GP becomes a multi-dimensional Gaussian distribution, with zero mean and covariance $\mathbf{C} = [c(t_m, t_n)]_{m,n \in \mathcal{N}}$ given by,

$$c(t_m, t_n) = \exp \left(-\frac{1}{\zeta_1} \sin^2 \left(\frac{\pi}{\zeta_2} (t_m - t_n) \right) \right), \quad (12)$$

²The prior knowledge on channel statics, model size, transmit power, and bandwidth is used to choose γ_0 .

where ζ_1 and ζ_2 are the length and period hyper-parameters, respectively [36]. Henceforth, the CSI prediction at time t and its uncertainty/variance is given by [37],

$$\hat{h}(t) = c^\dagger(t)C^{-1}[h(t_n)]_{n \in \mathcal{N}}, \quad (13)$$

$$\Upsilon(t) = c(t, t) - c^\dagger(t)C^{-1}c(t), \quad (14)$$

where $c(t) = [c(t, t_n)]_{n \in \mathcal{N}}$. The client and RB dependence is omitted in the discussion above for notation simplicity. The uncertainty measure $\Upsilon(\cdot)$ of the predicted channel $\hat{h}$ calculated using GPR framework is used as $j(\cdot)$ in (6a) which in turn allowing to exploring and sampling channels with high uncertainty towards improving the prediction accuracy. Finally, it is worth nothing that under *perfect CSI* $\hat{h}(t) = h(t)$ and $j(t) = 0$.

C. Joint client scheduling and RB allocation

Due to the time average objective in (11a), the problem (11) gives rise to a stochastic optimization problem defined over $t = \{1, \dots, T\}$. Therefore, we resort to the *drift plus penalty* (DPP) technique from Lyapunov optimization framework to derive the optimal scheduling policy [29]. Therein, the Lyapunov framework allows us to transform the original stochastic optimization problem into a series of optimizations problems that are solved at each time t , as discussed next.

First, we denote $u(t) = (1 - \beta) \sum_k s_k(t) D_k / D$ and define its time average $\bar{u} = \sum_{t \leq T} u(t) / T$. Then, we introduce auxiliary variables $\nu(t)$ and $l(t)$ with time average lower bounds $\bar{\nu} \leq \bar{u}$ and $\bar{l} \leq \frac{1}{T} \sum_{k,t} j_k^\dagger(t) \lambda_k(t) \leq l_0$, respectively. To track the time average lower bounds, we introduce virtual queues $q(t)$ and $g(t)$ with the following dynamics [29], [38], [39]:

$$q(t+1) = \max(0, q(t) + \nu(t) - u(t)), \quad (15a)$$

$$g(t+1) = \max(0, g(t) + l(t) - \sum_k j_k^\dagger(t) \lambda_k(t)). \quad (15b)$$

Therefore, (11) can be recast as follows:

$$\underset{[\Delta \theta_k(t)]_k, s(t), \Lambda(t), \nu(t), l(t) \forall t}{\text{minimize}} \quad D(1 - \bar{\nu})^T - \varphi \bar{l}, \quad (16a)$$

$$\text{subject to} \quad (11b), (15), \quad (16b)$$

$$0 \leq \nu(t) \leq 1 - \beta \quad \forall t, \quad (16c)$$

$$0 \leq l(t) \leq l_0 \quad \forall t, \quad (16d)$$

$$u(t) = \sum_k \frac{(1-\beta)D_k}{D} s_k(t) \quad \forall t. \quad (16e)$$

The quadratic Lyapunov function of $(q(t), g(t))$ is $L(t) = (q(t)^2 + g(t)^2)/2$. Given $(q(t), g(t))$, the expected conditional Lyapunov one slot drift at time t is $\Delta L = \mathbb{E}[L(t+1) - L(t) | q(t), g(t)]$. Weighted by a trade-off parameter $\phi (\geq 0)$, we add a penalty term to penalize a deviation from the optimal solution to obtain the Lyapunov DPP [29],

$$\phi \left(\frac{\partial}{\partial \nu} [(1 - \nu)^T D]_{\nu=\bar{\nu}(t)} \mathbb{E}[\nu(t) | q(t)] - \varphi \mathbb{E}[l(t) | g(t)] \right) = -\phi \left(DT(1 - \bar{\nu}(t))^{T-1} \mathbb{E}[\nu(t) | q(t)] + \varphi \mathbb{E}[l(t) | g(t)] \right), \quad (17)$$

Here, $\bar{\nu}(t) = \frac{1}{t} \sum_{\tau=1}^t \nu(\tau)$ and $\bar{l}(t) = \frac{1}{t} \sum_{\tau=1}^t l(\tau)$ are the running time averages of the auxiliary variables at time t .

Theorem 2. *The upper bound of the Lyapunov DPP is given by,*

$$\Delta L - \phi \left(DT(1 - \bar{\nu}(t))^{T-1} \mathbb{E}[\nu(t) | q(t)] + \varphi \mathbb{E}[l(t) | g(t)] \right) \leq \mathbb{E}[q(t)(\nu(t) - u(t)) + g(t)(l(t) - \sum_k j_k^\dagger(t) \lambda_k(t)) + L_0 - \phi \left(DT(1 - \bar{\nu}(t))^{T-1} \nu(t) + \varphi l(t) \right) | q(t), g(t)], \quad (18)$$

Proof: See Appendix B. ■

The motivation behind deriving the Lyapunov DPP is that minimizing the upper bound of the expected conditional Lyapunov DPP at each iteration t with a predefined ϕ yields the tradeoff between the virtual queue stability and the optimality of the solution for (16) [29]. In this regard, the stochastic optimization problem of (16) is solved via minimizing the upper bound in (18) at each time t as follows:

$$\underset{s(t), \Lambda(t), \nu(t), l(t)}{\text{maximize}} \quad \sum_k \left(\frac{q(t)(1-\beta)D_k}{D} s_k(t) + g(t) j_k^\dagger(t) \lambda_k(t) \right) - \chi(t) \nu(t) - (g(t) - \phi \varphi) l(t), \quad (19a)$$

$$\text{subject to} \quad (6b)-(6d), (16c), (16d), \quad (19b)$$

$$s(t) \in \{0, 1\}^K, \lambda_k(t) \in \{0, 1\}^b \quad \forall t, \quad (19c)$$

where $\chi(t) = q(t) - \phi DT(1 - \bar{\nu}(t))^{T-1}$ and the variables $\Delta \theta_k(t)$ with constraints (8) and (9) are decoupled from (19). By relaxing the integer (more specifically, boolean) variables in (19c) as linear variables, the objective and constraints become affine, in which, (19) is recast as a linear program (LP) as follows:

$$\underset{s(t), \Lambda(t), \nu(t), l(t)}{\text{maximize}} \quad \sum_k \left(\frac{q(t)(1-\beta)D_k}{D} s_k(t) + g(t) j_k^\dagger(t) \lambda_k(t) \right) - \chi(t) \nu(t) - (g(t) - \phi \varphi) l(t), \quad (20a)$$

$$\text{subject to} \quad (6b)-(6d), (16c), (16d), \quad (20b)$$

$$0 \leq s(t), \lambda_k(t) \leq 1. \quad (20c)$$

Due to the independence, the optimal auxiliary variables are derived by decoupling (16a), (16c), and (16d) as follows:

$$\nu^*(t) = \begin{cases} 1 - \beta & \text{if } \chi(t) \geq 0, \\ 0 & \text{otherwise,} \end{cases} \quad l^*(t) = \begin{cases} l_0 & \text{if } g(t) \geq \phi \varphi, \\ 0 & \text{otherwise.} \end{cases} \quad (21)$$

Theorem 3. *The optimal scheduling $s^*(t)$ and RB allocation variables $\Lambda^*(t)$ are found using an interior point method (IPM).*

Proof: See Appendix C. ■

The joint client scheduling and RB allocation is summarized in Algorithm 1 and the iterative procedure is illustrated in Fig. 2. First, all clients compute their local models using local SGD iterations with available computation power and upload the models to the PS. Parallely, at the PS, the channels are predicted using GPR based on prior CSI samples and clients are scheduled following the scheduling policy shown in Algorithm 1. Scheduled clients upload their local models to the PS, then at the PS the received models are averaged out to obtain a new global model and broadcast back to all K clients.

Algorithm 1 Joint Client Scheduling and RB Allocation

Input: $\mathcal{D}, \gamma_0, \beta, p, B, \xi$

Output: $\mathbf{s}^*(t), \mathbf{\Lambda}^*(t)$ for all t

- 1: $q(0) = g(0) = 0, \nu(0) = l(0) = 0, \mathbf{v}(0) = \mathbf{0}$
- 2: **for** $t = 1$ to T **do**
- 3: Each client update PS with computing power state information (CPSI)
- 4: Each client computes $\Delta\theta_k(t)$ using (8)
- 5: Channel prediction using GPR with (13)
- 6: Calculate $\nu^*(t)$ and $l^*(t)$ using (21)
- 7: Derive $\mathbf{s}^*(t)$ and $\mathbf{\Lambda}^*(t)$ by solving (20) using an IPM
- 8: Local model state information (MSI) ($\Delta\mathbf{v}_k(t), \Delta\theta_k(t)$) uploading to the server
- 9: Update $\tilde{\nu}(t), q(t)$ via (15), $\mathbf{v}(t)$ and $\theta(t)$ with (9)
- 10: Global model $\mathbf{v}(t)$ broadcasting
- 11: $t \rightarrow t + 1$
- 12: **end for**

In this setting, by sampling the scheduled clients, the PS gets additional information on the CSI. In the example presented in Fig. 2, the dashed arrows correspond to non-scheduled clients due to the lack of computational resources and/or poor channel conditions. This strategy allows the proposed scheduling method to avoid unnecessary computation and communication delays.

Fig. 2: Illustration of the flow of the operation per client and PS over the iterative training process.

D. Convergence, optimality, and complexity of the proposed solution

Towards solving (6a), the main objective (6a) is decoupled over clients and server using a dual formulation. Then, the upper bound of $\varepsilon(T)$, which is the accuracy loss using scheduling compared to a centralized training, is derived in Theorem 1, in which, solving (11) is equivalent to solving (6). It is worth noting that minimizing $\varepsilon(T)$, guarantees convergence to the minimum training loss, which is achieved as $T \rightarrow \infty$ [14, Appendix B]. In (11), the minimization of the analytical expression of $\varepsilon(T)$ with a finite T boils down to a stochastic

TABLE I: Simulation parameters

Parameter	Value
Number of clients (K)	10
Number of RB (B)	6
Local model solving optimality (β)	0.7
Transmit Power (in Watts) (p)	1
Model training and scheduling	
Training duration (T)	100
Number of local SGD iterations (M)	10
Learning rate (η)	0.2
Regularizer parameter (ξ)	1
Lyapunov trade-off parameter (ϕ)	1
Tradeoff weight (φ)	1
SINR threshold (γ_0)	1.2
Computation time threshold (τ_0)	1.2
Channel prediction (GPR)	
length parameter (ζ_1)	2
period parameter (ζ_2)	5
Number of past observations (N)	20

optimization problem with a nonlinear time average objective. The stochastic optimization problem (11) is decoupled into a sequence of optimization problems (19) that are solved at each time iteration t using the Lyapunov DPP technique with guaranteed convergence [40, Section 4]. Following Remark 1, the solution of (20) yields the optimality of (19) ensuring that the convergence guarantees are held under the Lyapunov DPP method. Since the optimal solution of (20) is optimal for (19), the optimality of the proposed solution depends on the recasted problem (16) that relies on the Lyapunov DPP technique. Moreover, the optimality of the Lyapunov DPP-based solution is in the order of $\mathcal{O}(\frac{1}{\varphi})$ [40, Section 7.4].

Finally, the complexity of Algorithm 1 depends on the complexity of the IPM used to solve the LP. Specifically, the complexity of the proposed solution at each iteration is given by the computational complexity of solving the LP which is in the order of $\mathcal{O}(n^3L)$ [41] with $n = (D + B + 1)K + 2$ variables, each of which is represented by a L -bits code.

IV. SIMULATION RESULTS

In this section, we evaluate the proposed client scheduling method and RB allocation using MNIST and CIFAR-10 datasets assuming $f(\cdot)$ and $\varrho(\cdot)$ as the cross entropy loss function and Tikhonov regularizer, respectively. A subset of the MNIST dataset with 6000 samples consisting of equal sizes of ten classes of 0-9 digits are distributed over $K = 10$ clients, whereas for CIFAR-10 data samples are from ten different categories but following the same data distribution. In addition, the wireless channel follows a correlated Rayleigh distribution [42] with mean to noise ratio equal to γ_0 . For perfect CSI, a single RB is dedicated for channel estimation. The remaining parameters are presented in Table I.

For IID datasets, training data is partitioned into K subsets of equal sizes with each consisting of equal number of samples from all 10 classes, which are randomly distributed over the K clients. The impact of the non-IID on the performance is studied for i) *heterogeneous dataset sizes*: clients having training datasets with different number of samples and ii) *heterogeneous class availability*: clients' datasets contain different number of samples per class. The dataset size heterogeneity is

Fig. 3: From IID datasets to non-IID datasets under different choices of Zipf parameter (σ) and Dirichlet parameter (α). The performance of the proposed algorithms are evaluated under the choices highlighted with the four regions A, B, C, and D.

modeled by partitioning the training dataset over clients using the Zipf distribution, in which, the dataset of client k is composed of $D_k = Dk^{-\sigma} / \sum_{k \in \mathcal{K}} k^{-\sigma}$ number of samples [43]. Here, the Zipf's parameter $\sigma = 0$ yields uniform/homogeneous data distribution over clients (600 samples per client), whereas increasing σ results in heterogeneous dataset sizes among clients as shown in Fig. 3. To control the heterogeneity in class availability over clients, we adopt the Dirichlet distribution, which is parameterized by a concentration parameter $\alpha \in (0, \infty]$ to distribute data samples from each class among clients [44]. With $\alpha = 0$, each client's dataset consists of samples from a single class in which increasing alpha yields datasets with training data from several classes but the majority of data is from few classes. As $\alpha \rightarrow \infty$, each client receives a dataset with samples drawn uniformly from all classes as illustrated in Fig. 3.

Throughout the discussion, *centralized training* refers to training that takes place at the PS with access to the entire dataset. In addition, how well the global model generalizes for individual clients is termed as “generalization” in this discussion. Training data samples are distributed among clients except in centralized training. In the proposed approach data samples are drawn from ten classes of handwritten digits. We compare several proposed RB allocation and client scheduling policies as well as other baseline methods. Under perfect CSI, two variants of the proposed methods named *quantity-aware* scheduling QAW and *quantity-unaware* scheduling QUNAW are compared, whose difference stems from either accounting or neglecting the local dataset size in model updates during scheduling. Under imperfect CSI, GPR-based channel prediction is combined together with QAW yielding the QAW-GPR method. For comparison, we adopt two baselines: a random scheduling technique RANDOM and a proportional fair PF method where fairness is expressed in terms of successful model uploading. In addition, we use the vanilla FL method [6] without RB constraints, denoted as IDEAL hereinafter. All proposed scheduling policies as well as baseline methods are

summarized in Table II.

TABLE II: Proposed Algorithms and benchmark algorithm

	Model	Description
Proposed Methods	QAW-GPR	PS uses dataset sizes to prioritize clients and GPR-based CSI predictions for scheduling.
	QAW	PS uses pilot-based CSI estimation and dataset sizes to prioritize clients.
	QUNAW	PS uses pilot-based CSI estimation without accounting dataset size of clients.
Baselines	RANDOM	Clients are scheduled randomly.
	PF	Clients are scheduled with fairness in terms of successful model uploading.
Ideal setup	IDEAL	All clients are scheduled assuming no communication or computation constraints.

A. Loss of accuracy

Fig. 4 compares the loss of accuracy in all FL methods at each model aggregation round with respect to the centralized model training. Here, we have considered the unbalanced dataset distribution ($\sigma = 1.017$) among clients to analyze the impact of dataset size in scheduling. It can be noted that IDEAL has the lowest loss of accuracy $\varepsilon(100) = 0.03$ due to the absence of both communication and computation constraints. Under perfect CSI, Fig. 4a plots QAW and QUNAW for two different RB values $B \in \{3, 6\}$. With a $2\times$ increase in RBs, the gain of the gap in loss in both QAW and QUNAW is almost the same. For $B = 6$, Fig. 4a shows that the QAW reduces the gap in loss by 22.8% compared to QUNAW. The reason for that is that QAW cleverly schedules clients with higher data samples compared to QUNAW when the dataset distribution among clients is unbalanced. Under imperfect CSI, QAW-GPR, PF, and RANDOM are compared in Fig. 4b alongside IDEAL and QAW. While RANDOM and PF show a poor performance, QAW-GPR outperforms QAW by reducing the gap in loss by 23.6%. The main reason for this improvement is that QAW needs to sacrifice some of its RBs for channel measurements while CSI prediction in QAW-GPR leverages all RBs.

B. Impact of system parameters

Fig. 5 shows the impact of the available communication resources (RBs) on the performance of the trained models $F(w(100), \mathcal{D})$. Without computing and communication constraints, IDEAL shows the lowest loss while RANDOM and PF exhibit the highest losses due to client scheduling with limited RBs. On the other hand the proposed methods QAW-GPR, performs better than QAW and QUNAW for $B \leq 10$ thanks to additional RBs when CSI measurements are missing. Beyond $B = 10$, the available number of RBs exceeds K , and thus, channel sampling in QAW-GPR is limited to at most K samples. Hence, increasing B beyond $K = 10$ results in increased number of under-sampled RBs

(a) FL with perfect CSI and $B = \{3, 6\}$.

(b) FL with imperfect CSI and $B = 6$.

Fig. 4: Comparison of the loss of accuracy in all FL methods for each model aggregation round vs. centralized training, Zipf parameter $\sigma = 1.017$ and $\alpha \rightarrow \infty$ (region C of Fig. 3).

yielding high uncertainty in GPR and poor CSI predictions. Inaccurate CSI prediction leads to scheduling clients with weak channels (stragglers), which consequently provides a loss of performance in QAW-GPR.

The impact of the number of clients (K) in the system with fixed RBs ($B = 5$) on the trained models performance and under different training policies is shown in Fig. 6. It can be noted that all methods exhibit higher losses when increasing K due to: i) local training with fewer data samples ($2500/K$) which deteriorates in the non-IID regime, ii) the limited fraction of clients ($5/K$) that are scheduled at once (except for the IDEAL method). The choice of equal number of samples per clients (balanced data sets with $\sigma = 0$) results highlights that QAW and QUNAW exhibit identical performance as shown in Fig. 6. Under limited resources, QAW-GPR outperforms all other proposed methods and baselines by reaping the benefits of additional RBs for GPR-based channel prediction. The baseline methods PF and RANDOM are oblivious to both

Fig. 5: Impact of the available RBs on the gap of loss $\varepsilon(100)$ for $K = 10$ clients for $\sigma = 0$ and $\alpha \rightarrow \infty$ dataset distribution (region A of Fig. 3).

Fig. 6: Impact of the number of clients on the gap of accuracy loss $\varepsilon(100)$ for $B = 5$ RBs for $\sigma = 0$ and $\alpha \rightarrow \infty$ dataset distribution (region A of Fig. 3).

CSI and training performance, giving rise to higher losses compared to the proposed methods.

Fig. 7 analyzes the performance as the network scales uniformly with the number of RBs and users, i.e., $K = B$. Under ideal conditions, the loss in performance when increasing K shown in Fig. 7 follows the same reasoning presented under Fig. 6. The GPR-based CSI prediction allows QAW-GPR to allocate all RBs for client scheduling yielding the best performance out of the proposed and baseline methods. It is also shown that the worst performance among all methods except IDEAL is at $K = B = 2$, owing to the dynamics of CSI leading to scheduling stragglers over limited RBs. With increasing K and B , the number of possibilities that clients can be successfully scheduled increases, leading to improved performance in all baseline and proposed methods. In contrast to the baseline methods, the proposed methods optimize client

Fig. 7: The analysis of the loss of accuracy $\varepsilon(100)$ as the system scales with fixed clients to RBs ratio, (i.e., $B = K$), with $\sigma = 0$ and $\alpha \rightarrow \infty$ dataset distribution (region A of Fig. 3).

scheduling to reduce the loss of accuracy, achieving closer performance to IDEAL with increasing K and B . However, beyond $K = B = 5$, the performance loss due to smaller local datasets outweighs the performance gains coming from an increasing number of scheduled clients, and thus, all three proposed methods follow the trend of IDEAL as illustrated in Fig. 7. Compared to the PF baseline with $K = B = 15$, QAW-GPR shows a reduction in the loss of accuracy by 20%.

C. Impact of dataset distribution

Fig. 8 plots the impact of data distribution in terms of balanced-unbalancedness in terms of training sample size per client on the loss of accuracy $\varepsilon(100)$. Here, the x -axis represents the local dataset size of the client having the lowest number of training data, i.e., the dataset size of the 10th client D_{10} as per the Zipf distribution with $\alpha \rightarrow \infty$. With balanced datasets, all clients equally contribute to model training, hence scheduling a fraction of the clients results in a significant loss in performance. In contrast, differences in dataset sizes reflect the importance of clients with large datasets. Therefore, scheduling important clients yields lower gaps in performance, even for methods that are oblivious to dataset sizes but fairly schedule all clients, as shown in Fig. 8. Among the proposed methods, QAW-GPR outperforms the others thanks to using additional RBs with the absence of CSI measurement. Compared to the baselines PF and QAW, QAW-GPR shows a reduction of loss of accuracy by 76.3%, for the highest skewed data distribution ($D_{10} = 40$). In contrast, QUNAW yields higher losses compared to QAW, QAW-GPR when training data is unevenly distributed among clients. As an example, the reduction of the loss of accuracy in QAW at $D_{10} = 40$ is 25.72% compared to 40.7% for QUNAW. The reason behind these lower losses is that client scheduling takes into account the training dataset size. For $D_{10} = 600$, due to the equal dataset sizes per client, the accuracy loss provided by QAW

Fig. 8: Impact of dataset distribution balanced-unbalancedness on the loss of accuracy $\varepsilon(100)$ for $B = 5$, $K = 10$, with $\alpha \rightarrow \infty$.

and QUNAW are identical. Therein, both QAW and QUNAW exhibit about 43.6% reduction in accuracy loss compared to RANDOM.

Next in Fig. 9, we analyze the impact of non-IID data in terms of the available number of training data from all classes on the accuracy of the trained model. Here, we compare the performance of the proposed methods with the baselines for several choices of α with $D_k = 250$ for all $k \in \mathcal{K}$ (i.e., $\sigma = 0$). Fig. 3 shows the class distribution over clients for different choices of α with equal dataset size $D_k = 250$. Fig. 9 illustrates that the training performance degrades as the samples data distribution becomes class wise heterogeneous. For instance from the IID case ($\alpha = 0$) to the case with $\alpha \rightarrow \infty$ case, QAW achieves a loss of accuracy reduction by 86.5% compared to $\alpha = 0$. However, QAW, QAW-GPR and QUNAW perform better than RANDOM and PF. Finally, it can be noticed that from $\alpha = 0.01$ to $\alpha = 10$ the gap in terms of accuracy loss performance of the trained model increases rapidly for all methods. Beyond those points, changes are small comparably to the inner points.

D. Impact of computing resources

The impact of the limitations in computation resources in model training and client scheduling is analyzed in Fig. 10. Since allocating RBs to stragglers results in poor RB utilization, we define the RB utilization metric as the percentage of RBs used for a successful model upload over the allocated RBs. Then we compare two variants of QAW with and without considering the computation constraint (5) referred to as CAW (original QAW in the previous discussions) and CUAW, respectively. It is worth highlighting that the computation threshold is inversely proportional to the average computing power availability as per (4), i.e. lower τ_0 corresponds to higher $\varepsilon(t)$ and vice versa. Fig. 10 indicates that the use of CPSI for client scheduling in CAW reduces the number of scheduled computation stragglers resulting in a lower accuracy

Fig. 9: Impact of the class-wise data heterogeneity on the loss of accuracy with $\sigma = 0$.

Fig. 11: Impact of number of local SGD iterations for loss of accuracy $\epsilon(100)$

Fig. 10: Impact of CPSI for QAW scheduling

loss, in addition to higher RB utilization over CUAW. Overall, CAW with QAW scheduling performs better than CUAW with QAW scheduling. For instance, compared to CUAW, CAW achieves 11.6% reduction in loss of accuracy with $\tau_0 = 0.6$ which increases to 43.1% with $\tau_0 = 1.4$. When τ_0 is small, the number of stragglers increases leading to poor performance for both CAW and CUAW. It is worth nothing that considering CPSI in the scheduling, CAW achieves at least 18.2% increase in RB utilization in addition to the loss of accuracy reduction by at least 11.6%.

The impact of local SGD iterations under limited computing power availability is analyzed in Fig. 11. Due to the assumption of unlimited computing power availability, IDEAL performs well with the increasing local SGD iterations. Similarly, gradual reductions in the loss of accuracy for both QAW and PF can be seen as M increases from two to eight. However, further increasing M results in longer delays for some clients in local computing under limited processing power as per (4). Such computation stragglers do not contribute to the training

in both PF (drops out due to the computation constraint) and QAW (not scheduled). Hence, increasing local SGD iterations beyond $M = 8$ results in fewer clients to contribute for the training, in which, increased losses of accuracy with QAW and PF are observed as shown in Fig. 11.

E. Fairness

Fig.12 indicates how well the global model generalizes for individual clients. Therein, the global model is used at the client side for inference, and the per client histogram of model accuracy is presented. It can be seen that, the global model in IDEAL generalizes well over the clients yielding the highest accuracy on average (96.8%) over all clients and the lowest variance with 5.6. With QAW-GPR, 96.1% average accuracy and variance of 7.8 is observed. It is also seen that QAW and QUNAW have almost equal means (95.2%) and variances of 15.2 and 16.3, respectively. Scheduling clients with a larger dataset in QAW provides a lower variance in accuracy compared to QUNAW. Although RANDOM and PF are CSI-agnostic, they yield an average accuracy of 93.4% and 94.1% respectively with the highest variance of 18.2 and 17.6. This indicates that client scheduling without any insight on datasize distribution and CSI fails to provide high training accuracy or fairness under communication constraints.

Finally, Fig. 13 compares the generalization performance of one of the proposed methods, QAW, for CIFAR-10 dataset instead of MNIST under both IID and non-IID data. In contrast to MNIST, CIFAR-10 consists of color images of physical objects from ten distinct classes [45]. For training, we adopt a 3-layer convolutional neural network (CNN) with $K = 10$ clients training over $T = 1000$ iterations. A total of 2500 data samples are distributed over the clients under four settings corresponding to the four regions in Fig. 3: i) IID data with $\alpha \rightarrow \infty$ and $\sigma = 0$ in region A, ii) equal dataset sizes ($\alpha = 0$) under heterogeneous class availability ($\alpha = 0$) in region B, iii) homogeneous class availability ($\alpha \rightarrow \infty$) with heterogeneous dataset sizes ($\sigma = 1.017$) in region C, and iv) heterogeneity

Fig. 12: Fairness comparison of the training accuracy among clients, Zipf parameter $\sigma = 1.071$ and $\alpha \rightarrow \infty$ (region C of Fig. 3).

in both ($\sigma = 1.017$) and ($\alpha = 0$) under region D. Fig. 13a indicates that the training performance with CIFAR-10 dataset significantly suffers from non-IID data under IDEAL communication and computation conditions. Interestingly, the proposed QAW yields identical performance than IDEAL under balanced datasets disregarding the identicalness of the data. However, with unbalanced datasets, the training performance of QAW is degraded as illustrated in Fig. 13b. The underlying reason is that the unbalanced datasets induce non-IID data at each client, and scheduling fewer clients is insufficient to obtain higher training performance.

V. CONCLUSION

In this work, FL over wireless networks with limited computational and communication resources, and under imperfect CSI is investigated. To achieve a training performance close to a centralized training setting, a novel client scheduling and RB allocation policy leveraging GPR-based channel prediction is proposed. Through extensive sets of simulations the benefits of FL using the proposed client scheduling and RB allocation policy are validated and analyzed in terms of (i) system parameters, model performance and computation resource limitations (number of RBs, number of clients) and (ii) heterogeneity of data distribution over clients (balanced-unbalanced, IID and non-IID). Results show that the proposed methods reduce the gap of the accuracy by up to 40.7% compared to state-of-the-art client scheduling and RB allocation methods.

APPENDIX

A. Proof of Theorem 1

After t and $t + 1$ communication rounds, the expected increment in the dual function of (6a) is,

$$\mathbb{E}[\psi(\boldsymbol{\theta}(t+1)) - \psi(\boldsymbol{\theta}(t))] \geq \mathbb{E}[\psi(\boldsymbol{\theta}(t+1))] - \mathbb{E}[\psi(\boldsymbol{\theta}(t))].$$

This inequality holds since the expectations of difference is greater than the difference of the expectations of a convex

(a) IDEAL scheduling

(b) QAW scheduling

Fig. 13: Performance comparison of the proposed QAW scheduling approach on CIFAR-10 trained with CNN vs. the IDEAL scheduling scheme.

function. By adding and subtracting the optimal dual function value to the R.H.S. :

$$\begin{aligned} \mathbb{E}[\psi(\boldsymbol{\theta}(t+1)) - \psi(\boldsymbol{\theta}(t))] &\geq \mathbb{E}[\psi(\boldsymbol{\theta}^*)] - \mathbb{E}[\psi(\boldsymbol{\theta}(t))] \\ &\quad + \mathbb{E}[\psi(\boldsymbol{\theta}(t+1))] - \mathbb{E}[\psi(\boldsymbol{\theta}^*)] \\ &= \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k^*(t)) - \mathbb{E}[\psi(\boldsymbol{\theta}(t))] + \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k(t)) \\ &\quad - \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k^*(t)). \end{aligned}$$

From (10) and following definition $\mathbb{E}[\psi(\boldsymbol{\theta}(t))] = \sum_{i=0}^K \Delta\psi(0)$,

$$\begin{aligned} &\mathbb{E}[\psi(\boldsymbol{\theta}(t+1)) - \psi(\boldsymbol{\theta}(t))] \\ &\geq \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k^*(t)) - \mathbb{E}[\psi(\boldsymbol{\theta}(t))] \\ &\quad - \beta \left\{ \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k^*(t)) - \mathbb{E}[\psi(\boldsymbol{\theta}(t))] \right\} \\ &= (1 - \beta) \left\{ \sum_{k=1}^K \Delta\psi(\Delta\boldsymbol{\theta}_k^*(t)) - \mathbb{E}[\psi(\boldsymbol{\theta}(t))] \right\}. \end{aligned}$$

However by selecting subset of users per iteration and repeating up to only t number of communication iterations the bound is lower bounded as below,

$$\begin{aligned} & \mathbb{E}[\psi(\theta(t+1)) - \psi(\theta(t))] \\ & \geq (1-\beta) \left\{ \sum_{k=1}^K \Delta\psi(\Delta\theta_k^*(t)) - \mathbb{E}[\psi(\theta(t))] \right\} \\ & \geq (1-\beta) \left(\sum_{\tau=1}^t \sum_{i=1}^K \frac{D_k}{tD} s_k(t) \right) \left\{ \sum_{k=1}^K \Delta\psi(\Delta\theta_k^*(t)) \right. \\ & \quad \left. - \mathbb{E}[\psi(\theta(t))] \right\} \end{aligned}$$

Now, following [14, Appendix B], $\{\sum_{k=1}^K \Delta\psi(\Delta\theta_k^*(t)) - \mathbb{E}[\psi(\theta(t))]\} \geq \bar{s}\{\psi(\theta^*) - \mathbb{E}[\psi(\theta(t))]\}$, where $\bar{s} \in (0, 1)$, we can have,

$$\begin{aligned} \varepsilon(T) &= \mathbb{E}[\psi(\theta^*) - \psi(\theta(T+1))] \\ &= \mathbb{E}[\psi(\theta^*) - \psi(\theta(T))] - \mathbb{E}[\psi(\theta(T+1)) - \psi(\theta(T))] \\ &\leq \mathbb{E}[\psi(\theta^*) - \psi(\theta(T))] - \\ &\quad (1-\beta) \left(\sum_{\tau=1}^T \sum_{i=1}^K \frac{D_k}{TD} s_k(t) \right) \left\{ \psi(\theta^*) - \mathbb{E}[\psi(\theta(T))] \right\} \\ &= (1 - (1-\beta) \sum_{\tau=1}^T \sum_{i=1}^K \frac{D_k}{TD} s_k(t)) \left\{ \psi(\theta^*) \right. \\ &\quad \left. - \mathbb{E}[\psi(\theta(T))] \right\} \\ &\leq (1 - (1-\beta) \sum_{\tau=1}^T \sum_{i=1}^K \frac{D_k}{TD} s_k(t))^T \left\{ \psi(\theta^*) \right. \\ &\quad \left. - \mathbb{E}[\psi(\theta(0))] \right\} \end{aligned}$$

In [46], it is proved that $\{\psi(\theta^*) - \mathbb{E}[\psi(\theta(0))]\} < D$. Following that,

$$\varepsilon(T) \leq \left(1 - (1-\beta) \sum_{\tau=1}^T \sum_{i=1}^K \frac{D_k}{TD} s_k(t) \right)^T D.$$

B. Proof of Theorem 2

Using the inequality $\max(0, x)^2 \leq x^2$, on (15) we have,

$$\frac{g^2(t+1)}{2} \leq \frac{g^2(t)}{2} + \frac{(\nu(t)-u(t))^2}{2} + g(t)(\nu(t)-u(t)), \quad (22a)$$

$$\begin{aligned} \frac{g^2(t+1)}{2} &\leq \frac{g^2(t)}{2} + \frac{(l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t))^2}{2} + g(t)(l(t) \\ &\quad - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t)). \end{aligned} \quad (22b)$$

With $L(t) = (g(t)^2 + g(t)^2)/2$, one slot drift ΔL can be expressed as follows:

$$\begin{aligned} \Delta L &\leq \mathbb{E}[g(t)(\nu(t)-u(t)) + g(t)(l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t)) \\ &\quad + (\nu(t)-u(t))^2/2 + (l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t))^2/2 | g(t), g(t)]. \end{aligned} \quad (23)$$

L_0 is a uniform bound on $(\nu(t)-u(t))^2/2 + (l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t))^2/2$ for all t , thus (23) can be expressed as follows:

$$\Delta L \leq \mathbb{E}[g(t)(\nu(t)-u(t)) + g(t)(l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t)) + L_0 | g(t), g(t)]. \quad (24)$$

Adding penalty term (17), upper bound of DPP can be expressed as,

$$\begin{aligned} \Delta L &- \phi \left(DT(1 - \tilde{\nu}(t))^{T-1} \mathbb{E}[\nu(t) | g(t)] + \varphi \mathbb{E}[l(t) | g(t)] \right) \leq \\ &\mathbb{E}[g(t)(\nu(t)-u(t)) + g(t)(l(t) - \sum_k \mathbf{j}_k^\dagger(t) \boldsymbol{\lambda}_k(t)) + L_0 \\ &\quad - \phi \left(DT(1 - \tilde{\nu}(t))^{T-1} \nu(t) + \varphi l(t) \right) | g(t), g(t)], \end{aligned} \quad (25)$$

C. Proof of Theorem 3

Let $\Theta_k = \frac{q(t)(1-\beta)D_k}{D}$, $\Omega_{k,b} = g(t)j_{k,b}(t)$, and $\mathcal{B}'$ and $\mathcal{K}'$ be the sets of allocated resource blocks and scheduled clients respectively.

Consider a scenario with non-integer solutions at optimality, i.e., $\lambda_{k,b}^* \in (0, 1]$ for $b \in \mathcal{B}'$ and $s_k^* \in (0, 1]$ for $k \in \mathcal{K}'$. Note that for all $b \in \mathcal{B}'$, $\Omega_{k,b} = \Phi$ for some $\Phi (\geq 0)$ is held ($\because$ if $\Omega_{k,b'} > \Phi$ for some $b' \in \mathcal{B}'$, then optimality holds only when $\lambda_{k,b'} = 1$ and $\lambda_{k,b} = 0$ for all $b \notin \mathcal{B}' \setminus \{b'\}$). Moreover, optimality satisfies $\mathbf{1}^\dagger \boldsymbol{\lambda}_k = 1$. With the constraint (1), this yields $\sum_{b \in \mathcal{B}} \Omega_{k,b} \lambda_{k,b} = \sum_{b \in \mathcal{B}'} \Phi \lambda_{k,b} = \Phi$. Hence, assigning $\lambda_{k,b'} = 1$ for any $b' \in \mathcal{B}'$ with $\lambda_{k,b''} = 0$ for all $b'' \notin \mathcal{B}' \setminus \{b'\}$ satisfies all constraints while resulting in the same optimal value, i.e., $\mathbf{1}^\dagger \boldsymbol{\lambda}_k = \Phi$. Hence, it can be noted that a solution with non-integer $\boldsymbol{\lambda}_k^*$ is not unique and there exists a corresponding integer solution for $\boldsymbol{\lambda}_k^*$ [claim A].

Substituting the above result in (1) yields $s_k \leq 1$ and hence, (1) and (20c) overlap. Following the same argument as for $\boldsymbol{\lambda}_k^*$, it can be shown that there exists an integer solution for s_k^* that yields the same optimal value as with $s_k^* \in (0, 1]$ for $k \in \mathcal{K}'$ [claim B].

Based on the claims A and B, it can be noted that any non-integer optimal solution is not unique, and there exists at least one integer solution for $\mathbf{S}^*$ and $\boldsymbol{\Lambda}^*$. Hence, by solving (20) using IPM and then selecting integer values for $\mathbf{S}^*$ and $\boldsymbol{\Lambda}^*$, the optimal solution of (19) is obtained.

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